
MNO: MULTISCALE NEURAL OPERATOR FOR COMPUTATIONAL FLUID DYNAMICS WITH 3D POINT CLOUD DATA

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ABSTRACT

Neural operators have emerged as a powerful data-driven paradigm for solving Partial Differential Equations (PDEs), offering orders-of-magnitude acceleration over traditional solvers. However, existing approaches still suffer from limited accuracy and scalability, particularly on irregular domains where fluid flows exhibit rich multiscale structures. In this work, we introduce the Multiscale Neural Operator (MNO), a new architecture for Computational Fluid Dynamics (CFD) on three-dimensional (3D) unstructured point clouds. MNO explicitly decomposes information across three scales: a global dimension-shrinkage attention module for long-range dependencies, a local graph attention module for neighborhood-level interactions, and a micro point-wise attention module for fine-grained details. This design preserves multiscale inductive biases while remaining computationally efficient. We evaluate MNO on four diverse benchmarks, covering both steady-state and unsteady flow scenarios with up to 300K points. Across all tasks, MNO consistently outperforms state-of-the-art baselines, reducing prediction errors by 5% to 40% and demonstrating improved robustness in challenging 3D CFD problems. Our results highlight the importance of explicit multiscale design for neural operators and establish MNO as a scalable framework for learning complex fluid dynamics on irregular domains.

1 INTRODUCTION

Neural operators (Lu et al., 2021), as a data-driven approach for solving Partial Differential Equations (PDEs), have attracted increasing attention in accelerating Computational Fluid Dynamics (CFD) (Lin et al., 2009). They provide approximate solutions within seconds (Sun et al., 2024), achieving inference speeds orders of magnitude faster than traditional numerical methods, e.g., FEM or FVM, enabling real-time computation and design exploration for complex fluid dynamics tasks.

Despite this remarkable efficiency, neural operators still fall short of traditional solvers in accuracy (typically 10^{-3} versus 10^{-7} relative error). Recent works have sought to close this gap through carefully-designed feature transformations, including spectral mappings FNO (Li et al., 2021), global latent space learning LNO (Wang & Wang, 2024), and Transformer-stacked approach with multiple physical space transformations Transolver (Wu et al., 2024), etc. Yet the intrinsic multiscale nature of fluid flow remains (Rahman et al., 2023; Wen et al., 2022) largely underexplored in architectural design, particularly on irregular and unstructured domains. In addition, sole reliance on global modeling often sacrifices local details, while fine-grained attention mechanisms incur prohibitive computational costs. These challenges highlight the need for architectures that explicitly disentangle and integrate information across multiple spatial scales.

In this work, we propose a Multiscale Neural Operator (MNO) to tackle typical CFD tasks on irregular domains. The motivation stems from the observation that physical quantities in flow fields exhibit

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strong multiscale effects: large-scale global trends, localized interactions near object surfaces, and fine-grained pointwise variations. Our goal is to develop a general framework that can faithfully represent objects in three-dimensional (3D) flow fields and accurately predict critical physical quantities such as pressure and velocity.

At the core of MNO is a sequence of three-scale blocks, each combining three complementary, parallel modules: (1) a **Global Dimension-Shrinkage Attention** module, which projects N points into a compact set of M modes to capture long-range dependencies; (2) a **Local Graph Attention** module, which encodes k -nearest-neighbor interactions to model mid-scale neighborhood dynamics; and (3) a **Micro Point-wise Attention** module, which evolves each point’s features independently to retain high-frequency variations. The outputs of these modules are fused after each block, enabling MNO to integrate receptive fields across scales and capture a broad spectrum of physical phenomena. Built directly on 3D point clouds, this design avoids mesh constraints and provides a unified framework for extracting global, local, and fine-grained flow representations.

We validate MNO across multiple benchmarks, spanning both steady-state and unsteady flow tasks with point resolutions ranging from 15K to 300K. Compared to state-of-the-art methods, MNO reduces prediction errors by 5% to 40%, demonstrating consistent improvements in accuracy and robustness on challenging 3D CFD problems.

In summary, the main contributions of this paper are as follows:

- We **propose a Multiscale Neural Operator (MNO)** for CFD on unstructured point clouds. Unlike prior multiscale methods restricted to regular grids, MNO directly processes 3D point data, removing mesh constraints and enabling flexible modeling of complex geometries and dynamic domains.
- We **introduce an explicit multiscale decomposition** with three complementary modules: global dimension-reduction attention for long-range dependencies, local graph attention for neighborhood interactions, and micro point-wise attention for fine-grained details, ensuring balanced representation across scales.
- We evaluate MNO on four diverse datasets, covering both steady and unsteady CFD tasks, and show that it consistently outperforms state-of-the-art baselines, reducing prediction errors by 5% to 40%.

2 RELATED WORK

Deep learning for PDEs has mainly progressed along two paths: physics-informed networks that enforce PDE constraints during training, and neural operators that learn solution mappings directly from data. We briefly review both directions, emphasizing their use in fluid dynamics and their limitations in modeling multiscale predictions on irregular domains.

2.1 PHYSICS-INFORMED NEURAL NETWORKS

Physics-Informed Neural Networks (PINNs) (Raissi et al., 2019) embed PDE constraints into the loss function, enabling solution learning without labeled data. Despite inspiring many extensions (Wang et al., 2021; 2022; Karlbauer et al., 2022; Rao et al., 2023), PINNs require task-specific loss design, struggle with unstructured point clouds, and is hard to scale to high-dimensional or stiff PDEs, limiting their applicability to complex CFD tasks.

2.2 NEURAL OPERATORS

Neural operators learn mappings from initial or boundary conditions, or equation parameters, to PDE solutions in a data-driven manner. Depending on the data representation, existing approaches can be broadly divided into regular-domain and irregular-domain methods.

Regular Domain Neural Operators CNO (Raonic et al., 2023) approximates integral operators with convolutional layers, enabling function-to-function mappings on regular grids. FNO (Li et al., 2021) extends this idea by learning PDE operators in Fourier space, efficiently capturing long-range

dependencies. AM-FNO (Xiao et al., 2024) further reduces FNO’s parameter cost through an amortized kernel that adapts to varying frequency modes. While effective, these models are restricted to structured geometries (e.g., rectangles or cubes) and is hard to transfer to domains with complex or varying shapes.

Irregular Domain Neural Operators PointNet (Qi et al., 2017a) and PointNet++ (Qi et al., 2017b) introduce point-based learning with global pooling and hierarchical neighbor search, respectively, though the latter often incurs high cost and may lose fine-scale details. Geo-FNO (Li et al., 2023a) maps irregular meshes into a uniform latent space for FFT-based FNO operations. LNO (Wang & Wang, 2024) encodes point clouds into compact latent tokens and applies Transformer layers for global modeling, while Transolver (Wu et al., 2024) compresses tokens into physical slices for Transformer-based feature extraction. PCNO (Zeng et al., 2025) combines FNO-style global features with residual and gradient-based local features. Despite these advances, most irregular-domain operators emphasize global features, paying limited attention to the coupling between local and global scales.

Multiscale Neural Operators U-NO (Rahman et al., 2023) integrates U-Net with neural operators, enabling multiscale PDE mapping. U-FNO (Wen et al., 2022) enhances FNO with local convolutions, while MscaleFNO (You et al., 2024) employs multiple FNO branches to extract features at different scales. These methods improve multiscale representation but remain tied to regular grids, limiting their ability to handle geometric deformations and dynamic flow fields. This motivates the development of multiscale neural operators tailored to point clouds, where scale interactions can be explicitly modeled in unstructured domains.

3 METHOD

The proposed Multiscale Neural Operator (MNO) is designed to solve CFD problems directly on unstructured point clouds by integrating global, local, and micro-scale feature learning. The overall architecture follows an Encoder–MNO–Decoder pipeline: the Encoder embeds spatial coordinates and associated attributes of the input points into latent tokens, a sequence of MNO blocks progressively enriches these representations through multiscale attention mechanisms, and the Decoder maps the processed features back to the target physical quantities. This design allows MNO to capture long-range dependencies, neighborhood-level interactions, and fine-grained details simultaneously, providing an efficient and accurate framework for modeling complex fluid dynamics.

In what follows, we first describe the overall model and the input–output format, then introduce the global, local, and micro modules in detail. Finally, we discuss the differences between MNO and existing multiscale approaches for point cloud learning.

3.1 OVERVIEW OF THE MNO MODEL

The proposed MNO model, illustrated in Figure 1, is composed of an Encoder, a sequence of MNO blocks, and a Decoder. The input is represented as an array of points, where each point is described by its 3D spatial coordinates and task-specific auxiliary attributes.

The Encoder, implemented as an MLP, embeds these inputs into a latent token space,

$$X = \text{Encoder}(\text{concat}(\text{pos}_{in}, \text{feature}_{in})), \quad (1)$$

where $\text{pos}_{in} \in \mathbb{R}^{N \times 3}$ denotes the 3D coordinates, feature_{in} represents auxiliary features, and $X \in \mathbb{R}^{N \times D}$ are the latent tokens, with $D = 128$ by default. Since the positional information is explicitly included, no additional positional encoding is required.

The latent tokens are then processed by a sequence of MNO blocks, which form the core of the architecture. Each block integrates global, local, and point-wise attention modules to capture multiscale dynamics, progressively enriching the latent representations with hierarchical flow features. Finally, the Decoder, which is the MLP by default, maps the enriched latent features back to the target physical quantities

$$\begin{aligned} X_p &= \text{MNO}(X), \\ X_{out} &= \text{Decoder}(X_p), \end{aligned} \quad (2)$$

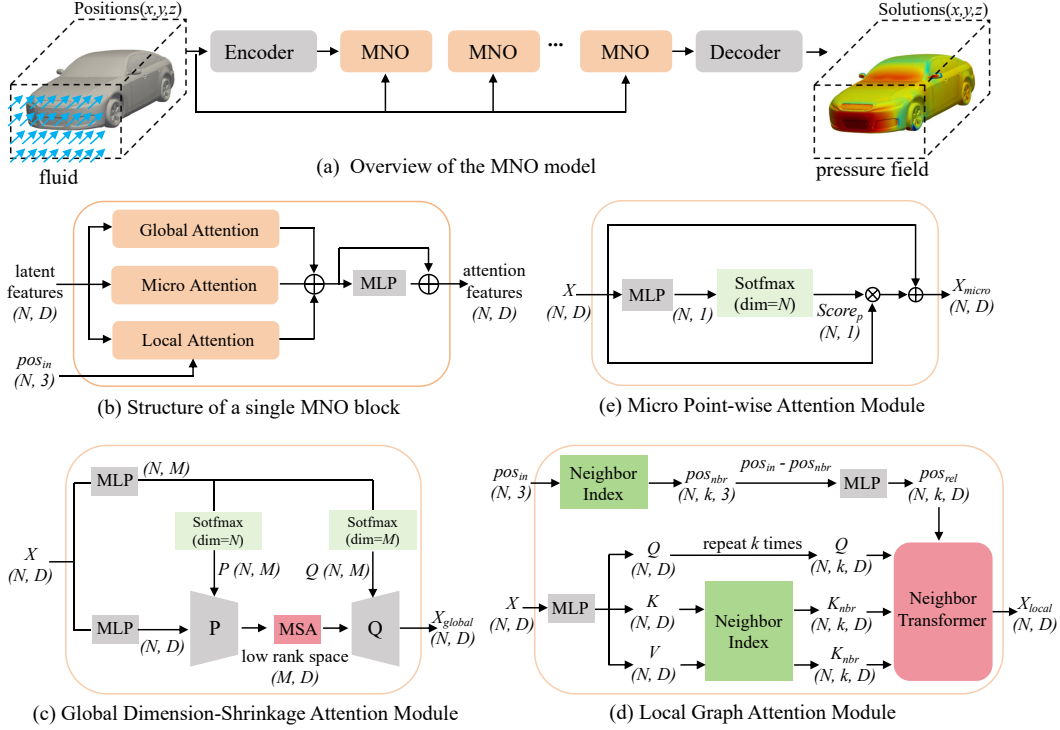


Figure 1: (a) The overview of the proposed MNO model with a sequence of three-scale blocks, and (b) each block combines three complementary, parallel modules: (c) a global dimension-shrinkage attention module for long-range dependencies, (d) a local graph attention module for neighborhood-level interactions, and (e) a micro point-wise attention module for fine-grained details.

where $X_p \in \mathbb{R}^{N \times D}$ denotes the processed latent features and $X_{out} \in \mathbb{R}^{N \times O}$ represents the predicted outputs, with O the number of physical variables.

As a concrete example, in the ShapeNet Car benchmark, after preprocessing (Deng et al., 2024; Wu et al., 2024), the input consists of N points with 3D coordinates pos_{in} and features $feature_{in}$ that include surface normals and signed distance values (Euclidean distance from each air point to the nearest surface point, positive outside the car). This results in an input dimension of $\mathbb{R}^{N \times 7}$. The output X_{out} includes the velocity vector field in the air region and the pressure scalar field on the car surface, with an output dimension of $\mathbb{R}^{N \times 4}$.

3.2 GLOBAL DIMENSION-SHRINKAGE ATTENTION MODULE

The global module captures long-range dependencies in the point cloud, enabling the model to extract global patterns such as overall shape and large-scale flow trends.

To force this module capture long-range, low-frequency feature, and to address the quadratic computational cost of applying attention on all tokens, we introduce a low rank projection strategy similar to Transolver (Wu et al., 2024) and LNO (Wang & Wang, 2024). Specifically, the latent features $X \in \mathbb{R}^{N \times D}$ are projected into a compact M -dimensional subspace ($M \ll N$) using a learnable projector P , then the feature is processed by a multi-head self-attention (MSA) in the reduced space $\mathbb{R}^{M \times D}$, and finally recover to the point feature space $\mathbb{R}^{N \times D}$ via the inverse projection Q . Formally, the global feature $X_{global} \in \mathbb{R}^{N \times D}$ is computed by

$$\begin{aligned}
 P &= \text{Softmax}_N(\text{MLP}(X)), \\
 Q &= \text{Softmax}_M(\text{MLP}(X)), \\
 X_{global} &= Q \cdot Z_{lr} = Q \cdot \text{MSA}(P^T \cdot X),
 \end{aligned} \tag{3}$$

where $P, Q \in \mathbb{R}^{N \times M}$ are the projection and inverse-projection matrices with $M = 256$ by default, and $\text{Softmax}_N(\cdot)$ and $\text{Softmax}_M(\cdot)$ denote the Softmax function along the N and M dimensions, respectively.

This mechanism removes redundant information while preserving low-frequency global components. In the reduced space, attention weights can be computed efficiently at complexity $O(M^2D)$ instead of $O(N^2D)$, and the overall cost is dominated by the projection step $O(MND)$.

3.3 LOCAL GRAPH ATTENTION MODULE

The Local Attention module is designed to restrict interactions to geographically nearby points, ensuring that local geometric structures are explicitly preserved. Specifically, a k -nearest neighbor (k-NN) graph is first constructed using the Euclidean distance of the input 3D coordinates. Each spatial point serves as a graph node, and its k nearest neighbors define the local connectivity.

Inspired by the Point Transformer (Zhao et al., 2021), originally developed for point cloud segmentation, the Local Graph Attention computes neighborhood features for each node by attending only to its k nearest neighbors. The structure of the Local Attention module is illustrated in Figure 1(d). The local features between the node and its neighboring nodes is computed following

$$X_{local} = \text{Sum}(\text{Softmax}(\text{MLP}(Q - K_{nbr} + pos_{rel})) \odot (V_{nbr} + pos_{rel})), \quad (4)$$

where $Q \in \mathbb{R}^{N \times k \times D}$ denotes the replicated features of the center node (k identical features vectors); $K_{nbr}, V_{nbr} \in \mathbb{R}^{N \times k \times D}$ are the features of neighboring nodes, and $pos_{rel} \in \mathbb{R}^{N \times k \times D}$ encodes relative positional offsets. The symbol $\odot$ indicates element-wise multiplication. The similarity kernel is parameterized by an MLP, and the weighted neighbor features are aggregated by summation along the dimension k , yielding $X_{local} \in \mathbb{R}^{N \times D}$. The computational complexity is dominated by matrix multiplication in the MLP, yielding $O(NkD^2)$.

This formulation enforces that only spatially adjacent tokens interact directly, embedding locality into the feature learning process, which ensures that fine-scale geometric and physical properties are preserved across deeper layers. In contrast, the Global Attention module complements this design by capturing long-range dependencies, and together they enable MNO to achieve both local accuracy and global coherence in flow prediction.

3.4 MICRO POINT-WISE ATTENTION MODULE

Micro-scale features correspond to the intrinsic attributes of individual spatial points. To complement the global and local attention modules, which capture long-range and neighborhood-level interactions, the micro point-wise attention module focuses on the single-point scale that could be overlooked at coarser scales.

This module implements a point-wise self-attention mechanism, where each token is reweighted solely based on its own feature vector. As illustrated in Figure 1(e), token features from the previous block are processed through an MLP followed by a softmax operation to produce point-specific weights, which indicate the relative importance of each token. The scaled features are then combined with the original input via a residual connection

$$X_{micro} = X + Score_p \odot X, \text{ with } Score_p = \text{Softmax}(\text{MLP}(X), \dim = N), \quad (5)$$

where $X \in \mathbb{R}^{N \times D}$ denotes the input token features, $Score_p \in \mathbb{R}^{N \times 1}$ represents the point-wise attention weights, and $X_{micro} \in \mathbb{R}^{N \times D}$ is the resulting micro-scale representation. The symbol $\odot$ indicates element-wise multiplication with broadcasting rule across feature dimensions.

Because each token is reweighted independently of others, this module emphasizes point-specific high-frequency variations while remaining computationally efficient, with complexity $O(ND^2)$. In combination with the global and local attentions, it ensures that MNO simultaneously preserves fine-grained details, local neighborhood patterns, and long-range flow coherence.

Remarks on other multiscale models Existing multiscale methods for point clouds primarily focus on visual tasks, e.g., segmentation (Qi et al., 2017b; Hu et al., 2020; Yu et al., 2018). These approaches typically rely on repeated downsampling and upsampling, which can discard fine-grained information and lead to suboptimal accuracy when applied to flow field prediction (Qi et al., 2017b).

Table 1: The comparison results with other methods on Ahmed body and Parachute datasets, in which $RL2_p$ denotes the relative L_2 errors (RL2) of the pressure field; $RL2_{x1\sim4}$ represent the RL2 of the displacement field at 4 time steps; $RL2_x$ denotes the total RL2 of 4 time steps; MAE is the mean absolute errors. The subscript “*” indicates the result claimed in the original article. The row titled with Improvement refers to the degree of advancement compared to the previous best method.

Methods	Ahmed body		Parachute					
	$RL2_p$	MAE_p	$RL2_{x1}$	$RL2_{x2}$	$RL2_{x3}$	$RL2_{x4}$	$RL2_x$	MAE_p
DeepONet (Lu et al., 2021)	0.3683	59.6948	1.2620	0.7243	0.7915	0.7667	0.7733	0.2864
PointNet (Qi et al., 2017a)	0.1923	35.8585	0.0955	0.0703	0.1069	0.1427	0.1035	0.0345
PointNet++ (Qi et al., 2017b)	0.3366	55.5127	0.2364	0.0923	0.1009	0.1623	0.1165	0.0371
Geo-FNO (Li et al., 2023a)	0.1400	26.3723	0.0480	0.0248	0.0353	0.0551	0.0366	0.0114
LNO (Wang & Wang, 2024)	0.1908	30.4570	0.0584	0.0431	0.0484	0.0665	0.0504	0.0147
PCNO* (Zeng et al., 2025)	0.0682	-	-	-	-	-	0.0373	-
PCNO (Zeng et al., 2025)	0.0664	12.4693	0.0238	0.0189	0.0305	0.0515	0.0316	0.0094
Ours	0.0468	7.0465	0.0216	0.0164	0.0259	0.0418	0.0266	0.0081
Improvement	29.51%	43.48%	9.24%	13.23%	15.08%	18.83%	15.82%	13.82%

In contrast, our design introduces distinct mechanisms tailored to each scale without resampling. At the global scale, a low rank projection enforces attention to long-range dependencies and low-frequency structures while reducing computational cost. At the local scale, a restricted receptive field ensures that each point interacts only with its nearest neighbors, capturing mid-frequency interactions tied to geometric adjacency. At the micro scale, point-wise modulation refines the representation by recovering high-frequency details. Together, these complementary modules provide a balanced decomposition of global, local, and fine-scale features, enabling accurate and efficient modeling of multiscale dynamics in CFD.

4 EXPERIMENTS

4.1 BENCHMARKS

We evaluate the model performance on four 3D CFD benchmarks, including steady-state flow field benchmarks, Ahmed body (Ahmed et al., 1984; Li et al., 2023b), ShapeNet Car (Umetani & Bickel, 2018), DrivAerNet++ (Elrefaie et al., 2024), and the unsteady flow field benchmark, Parachute dynamics (Zeng et al., 2025).

Ahmed body (100k/sample): A vehicle wind tunnel dataset with a bluff-body structure. Inputs consist of the vehicle surface point cloud and auxiliary conditions such as freestream velocity and Reynolds number. The output is the pressure field on the vehicle surface. **Parachute dynamics** (15k/sample): A time-dependent dataset capturing the inflation of parachutes under pressure loads. Inputs include the initial point cloud positions and markers for the umbrella surface and ropes, while outputs are displacement fields at four time steps. **ShapeNet Car** (30k/sample): A car wind tunnel dataset. Inputs include point positions, signed distance values, and surface normals. Outputs are the velocity field in the air region and the pressure field on the car surface. **DrivAerNet++** (300k/sample): A large-scale automotive wind tunnel dataset. Inputs consist of point positions and surface normals, and the output is the pressure field on the car surface. For detailed configurations, please refer to Appendix B.

4.2 COMPARISON ON ACCURACY

We reproduce several state-of-the-art open-source methods of neural operator for comparative experiments. To ensure fairness, all comparative experiments are conducted on the same protocol and executed on our identical computational hardware.

The methods we compared are commented as follows.

DeepONet (Lu et al., 2021): The first neural operator framework, primarily based on MLPs. Its representational capacity is limited, particularly when addressing highly nonlinear 3D PDEs.

Table 2: The comparison results with other advanced methods on ShapeNet Car and DrivAerNet++ datasets. $RL2_v$ denotes the RL2 of the velocity field. The subscript “*” indicates the result claimed in the original article.

Methods	ShapeNet Car				DrivAerNet++	
	$RL2_p$	MAE_p	$RL2_v$	MAE_v	$RL2_p$	MAE_p
DeepONet (Lu et al., 2021)	0.4148	11.4996	0.2075	1.2256	0.3203	27.4931
PointNet (Qi et al., 2017a)	0.0927	2.6222	0.0314	0.1723	0.4278	42.6893
PointNet++ (Qi et al., 2017b)	0.2082	5.9648	0.0771	0.3813	0.4617	41.8497
Geo-FNO (Li et al., 2023a)	0.1164	3.5748	0.0737	0.4647	0.2869	26.3732
LNO (Wang & Wang, 2024)	0.0887	2.6118	0.0267	0.1498	0.1984	18.1088
Transolver* (Wu et al., 2024)	0.0745	-	0.0207	-	-	-
Transolver (Wu et al., 2024)	0.0700	1.8151	0.0230	0.1130	0.1749	15.4372
Ours	0.0597	1.3796	0.0178	0.0845	0.1665	14.6335
Improve	14.71%	23.99%	22.61%	25.22%	4.80%	5.21%

PointNet’s (Qi et al., 2017a): Utilizes global pooling to model the overall structure of flow fields. However, it neglects local interactions among points, and in dense point clouds, the pooling mechanism may excessively compress information.

PointNet++ (Qi et al., 2017b): Extends PointNet with fixed-number downsampling to extract multi-scale features. On large-scale point clouds, this strategy may discard essential geometric structures, sometimes resulting in performance worse than PointNet. Moreover, increasing the sampled points significantly raises computational cost and parameter count, making the method less practical.

Geo-FNO (Li et al., 2023a): Maps irregular grids onto regular ones and applies FNO for global Fourier-based convolutions. Its performance is highly dependent on the quality of the mapping and lacks robustness for complex geometries.

Transolver (Wu et al., 2024): Employs a global dimension reduction and introduces residual branch between token compression and decompression to reduce information loss. However, it does not explicitly support multiscale feature learning.

LNO (Wang & Wang, 2024): Compresses point clouds into a latent space with limited tokens, where multiple Transformer layers capture global features. This approach resembles our Global Attention module but suffers from noticeable loss of fine-grained details due to heavy compression.

PCNO (Zeng et al., 2025): Extracts global, gradient, and residual features of the input point cloud. However, its global feature extraction relies on FNO without point cloud compression, limiting scalability for large datasets. Compared to PCNO, MNO provides stronger mid-scale representations through its Local Attention module.

The comparative results are summarized in Table 1 and Table 2. The proposed MNO consistently delivers higher predictive accuracy across all four benchmarks compared to recent baselines. In particular, relative to the current leading methods, Transolver and PCNO, MNO achieves error reductions of 29.51% on the Ahmed Body dataset, 15.82% on Parachute Dynamics, 14.71% on ShapeNetCar, and 4.80% on DrivAerNet++.

4.3 ATTENTION MODULES ABLATION EXPERIMENTS

In each MNO block, the three attention modules are responsible for extracting multiscale features. To better understand their contributions, we conduct ablation studies by selectively enabling different modules. Unless otherwise specified, the number of MNO blocks is fixed at four.

The results are summarized in Table 3. “Global,” “Local,” and “Micro” denote using only the corresponding attention module to learn and predict flow fields. “Global+Local” indicates the joint use of both Global and Local Attention modules, “Global+Local+Micro” represents the full MNO block, and “Global+Global+Global” refers to using three identical Global Attention modules as a control.

When used individually, the Global Attention module performs worst due to repeated low-rank projections that discard point cloud information. By contrast, the Local Attention module achieves the

Table 3: The results of the ablation experiment of Attention Modules. OOM is out of memory.

Modules	Ahmed body		Parachute		ShapeNet Car				DrivAerNet++	
	$RL2_p$	MAE_p	$RL2_x$	MAE_x	$RL2_p$	MAE_p	$RL2_v$	MAE_v	$RL2_p$	MAE_p
Global	0.8588	154.899	0.8205	0.2629	0.5117	16.9729	0.2025	1.3195	0.7853	73.3534
Local	0.1350	24.8293	0.1479	0.0314	0.0832	2.9235	0.0399	0.2042	0.1919	17.8505
Micro	0.4028	64.5137	0.2307	0.0542	0.1881	6.2470	0.0609	0.3098	0.2396	21.2415
Local+Micro	0.1267	24.0813	0.1062	0.0234	0.0807	2.7964	0.0393	0.1975	0.1908	17.6443
Global+Micro	0.0484	7.4700	0.0304	0.0095	0.0663	1.5408	0.0194	0.0980	0.1728	15.3040
Global+Local	0.0488	7.6412	0.0287	0.0090	0.0610	1.4994	0.0201	0.0983	0.1713	14.9961
Global+Global+Global	0.8591	153.907	0.8170	0.2601	0.7986	23.7095	0.3249	2.0015	0.7853	73.2887
Local+Local+Local	OOM	OOM	0.1484	0.0313	0.0800	2.7651	0.0385	0.1852	OOM	OOM
Micro+Micro+Micro	0.4328	76.6320	0.2249	0.0527	0.1893	6.1662	0.0591	0.2930	0.2420	21.5583
Global+Local+Micro	0.0468	7.0465	0.0266	0.0081	0.0597	1.3796	0.0178	0.0845	0.1665	14.6335

best performance among the three. Local Attention captures mid-scale features, i.e., mid-frequency information, which is crucial for distinguishing geometric shapes of objects.

Combining Global and Local Attention substantially improves performance, with relative gains of 63.85%, and 80.59%, 25.33%, and 10.73%, across the four datasets compared to using Local Attention alone. This highlights the strong complementarity of global and mid-scale features, showing that their combination captures most of the key physical processes in flow fields.

Adding Micro Attention on top of Global+Local yields further improvements of 4.09%, 7.32%, 2.13%, and 2.80%, across the four datasets. The Micro Attention module captures high-frequency variations that serve as fine-scale corrections to mid-frequency features. While its contribution is smaller, it refines predictions and enhances overall accuracy.

4.4 VISUALIZATION OF ATTENTION MODULES

Figure 2 visualizes the prediction errors for different attention configurations. Each row corresponds to one of the four benchmarks, while columns represent the module combinations: the first column shows predictions using only Global Attention; the second column shows Global+Local Attention; the third column repeats the second but with a different color scale for better contrast; and the fourth column shows the full combination of Global, Local, and Micro Attention. The following discussion takes Figure 2(b) as an illustrative example.

From the error map of Global Attention alone, shown in the first column of Figure 2(b), we observe that the module tends to minimize error in the larger side area of the car (the non-windward region). This reflects its capacity to capture low-frequency components: the non-windward region is subject to simpler forces and smaller pressure fluctuations, making it easier to approximate. In contrast, the windward region experiences stronger forces and larger fluctuations, resulting in higher prediction error.

Comparing Global with Global+Local, it is evident that Local Attention significantly improves performance in the windward region. Local Attention captures mid-frequency information and effectively distinguishes between windward and non-windward regions, complementing the Global Attention module.

Finally, comparing Global+Local with Global+Local+Micro shows that errors in transitional areas between the front and side regions are further reduced when Micro Attention is included. By refining predictions at specific points, Micro Attention supplements fine-grained details and corrects residual errors, demonstrating its role as a complementary high-frequency module.

5 CONCLUSIONS

In this work, we introduced the Multiscale Neural Operator (MNO), a new framework for solving CFD problems directly on unstructured point clouds. By explicitly decomposing information into global, local, and micro scales, MNO captures long-range dependencies, neighborhood interactions, and fine-grained details within a unified architecture. Besides performance gains, the ablation and visualization studies confirm the complementary roles of the three attention modules and validate the importance of explicit multiscale design. These results highlight the potential of MNO as a

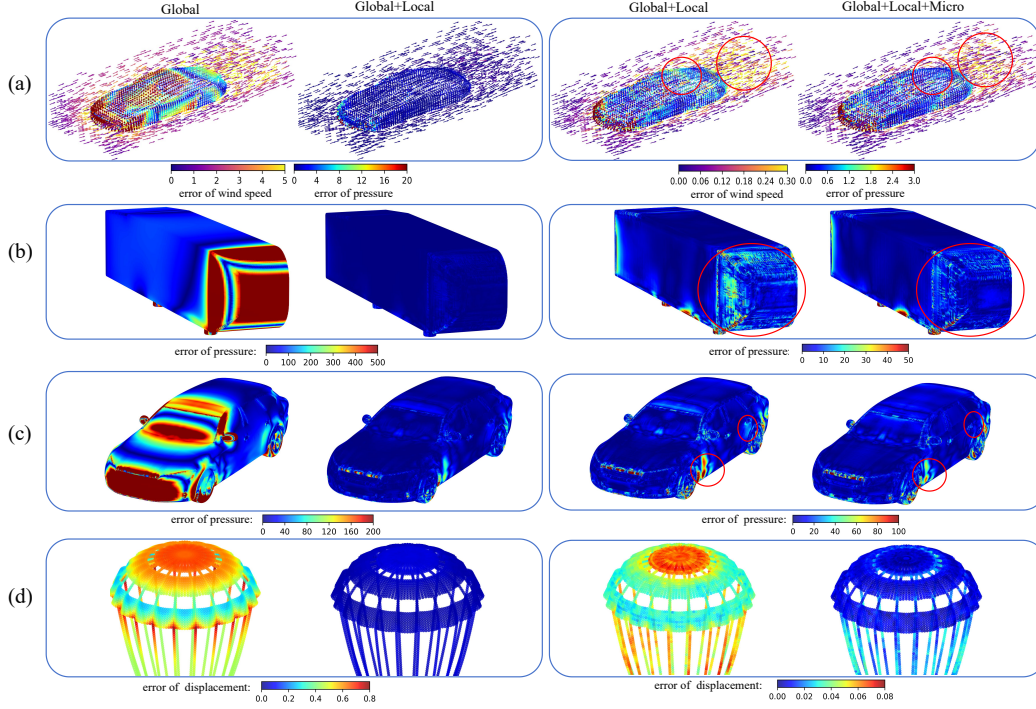


Figure 2: The visualization of Global, Local and Micro Attention modules. The red circle serves as a reference for areas with obvious differences. Rows show the error maps for different benchmarks. For each row: (a) ShapeNet Car. The arrow represents the direction of the wind, and the color denotes the prediction error; (b) Ahmed body; (c) DrivAerNet++; (d) Parachute. For each column: (first column) prediction of only Global Attention module; (second column) prediction of Global and Local Attention modules together; (third column) identical values to the second column but with a different color scale; (fourth column) prediction of the full MNO with Global, Local, and Micro Attention modules together.

general and efficient framework for learning complex fluid dynamics on irregular domains, paving the way for broader applications of neural operators in large-scale scientific computing.

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A LLMs POLISHING

The manuscript was initially drafted in Chinese and polished using Large Language Models (LLMs) of DeepSeek-R1 and ChatGPT-4.0 to improve clarity, grammar, and academic style. The authors rigorously reviewed and edited all AI-generated content to ensure accuracy and consistency with the original scientific intent. The intellectual contributions remain entirely human.

B DETAILS OF BENCHMARKS

This paper conducts a comprehensive evaluation of the model across four benchmarks. The details for each benchmark are provided below.

The ShapeNet Car (Umetani & Bickel, 2018) focuses on wind tunnel experiments for automobiles, a critical stage in automotive industrial design. This dataset contains 889 samples representing different car shapes, used to simulate driving conditions at a speed of 72 km/h. The car shapes are drawn from the "Car" category of ShapeNet (Chang et al., 2015). The surrounding space is discretized into an unstructured grid with 32,186 points, and both the airflow velocity around the car and the pressure on the car surface are recorded. The number of points on the car surface is 3,682. Following the experimental setup in Transolver (Wu et al., 2024), we use 789 samples for training and the remaining 100 samples for testing. The input point cloud of each sample is preprocessed into a combination of point positions, signed distance functions, and normal vectors. A notable difference is that the original dataset contains 96 fixed noisy points on the car surface. After our preprocessing, the point cloud data consists of 29,498 air points and 3,586 car surface points.

The DrivAerNet++ (Elrefaie et al., 2024) is a large-scale, comprehensive benchmark for automotive aerodynamic design, constructed using high-fidelity CFD simulations. It contains over 8,000 distinct car designs, covering various vehicle types, wheel configurations, and chassis layouts. The inflow air velocity is 108 km/h. We only use a subset of surface pressures for the experiment. To maintain sample diversity while improving research efficiency, we randomly select 200 samples for training and 50 samples for testing. Each point cloud sample consists of approximately 600k points, with each point described by its three-dimensional coordinates (x, y, z) and surface normal vectors (ux, uy, uz). Since the dataset was generated with y-axis symmetry, we only use the points with $y > 0$ (300k) to enhance computational efficiency.

The Ahmed Body (Li et al., 2023b) is a wind tunnel dataset for bluff-body vehicles, used to predict the pressure on the vehicle surface. The vehicle shape is based on the benchmark model designed in (Ahmed et al., 1984). The inflow velocity ranges from 10 m/s to 70 m/s, corresponding to Reynolds numbers from 4.35×10^5 to 6.82×10^6 . The dataset is generated by systematically varying the vehicle's length, width, height, ground clearance, inclination angle, and rear rounding radius, resulting in a total of 551 samples, each containing approximately 100k surface points. Among these, 500 samples are used for training and 51 samples for testing, consistent with the setup in PCNO (Zeng et al., 2025).

The Parachute Dynamics (Zeng et al., 2025) captures the inflation process of different parachutes under specific pressure loads. The pressure load increases linearly from 0 to 1000 Pa over the first 0.1 seconds and then remains constant at 1000 Pa. The learning objective is to map the initial parachute shape to the displacement fields at four specific time points during inflation: $t_1 = 0.04$, $t_2 = 0.08$, $t_3 = 0.12$, and $t_4 = 0.16$. These time points characterize the inflation process, where the parachute first rapidly expands under pressure, then over-expands, and finally rebounds. The experimental setup follows that of PCNO (Zeng et al., 2025), with 1000 samples for training and 200 samples for testing. Each sample contains approximately 15k points in the point cloud.

C THE EVALUATION METRICS

For the quantitative evaluation of point cloud prediction algorithms, this study employs the following two widely used metrics: Relative L2 Error (RL2) and Mean Absolute Error (MAE). Both metrics are calculated based on point-to-point correspondence between the predicted point cloud and the true point cloud, requiring that the point clouds be precisely aligned and point correspondences established prior to evaluation.

C.1 THE RELATIVE L2 ERROR

The RL2 measures the normalized Euclidean distance discrepancy of the predicted point cloud as a whole relative to the true point cloud. It is defined as follows:

$$RL2 = \frac{\|\hat{Y} - Y\|_2}{\|Y\|_2} = \frac{\sqrt{\sum_{i=1}^N \|\hat{y}_i - y_i\|_2}}{\sqrt{\sum_{i=1}^N \|y_i\|_2}}, \quad (6)$$

where $Y = \{y_1, y_2, \dots, y_N\}$ is the true point cloud, $\hat{Y} = \{\hat{y}_1, \hat{y}_2, \dots, \hat{y}_N\}$ is the predicted point cloud, N is the number of points, $\|\cdot\|_2$ represents the L2 norm.

A smaller RL2 value indicates lower relative error between the predicted point cloud and the true point cloud at the overall level, reflecting higher prediction accuracy. By using the norm of the true point cloud as the denominator, this metric achieves scale invariance, enabling robust performance comparisons across different scales or datasets.

C.2 THE MEAN ABSOLUTE ERROR

MAE measures the mean of the absolute deviations between the predicted point cloud and the true point cloud on a point-wise basis. It is defined as follows:

$$MAE = \frac{1}{N} \sum_{i=1}^N \|\hat{y}_i - y_i\|, \quad (7)$$

where $Y = \{y_1, y_2, \dots, y_N\}$ is the true point cloud, $\hat{Y} = \{\hat{y}_1, \hat{y}_2, \dots, \hat{y}_N\}$ is the predicted point cloud, N is the number of points, $\|\cdot\|_1$ represents the L1 norm.

A smaller MAE value indicates that the predicted point cloud aligns more closely with the ground truth along each coordinate axis, reflecting higher point-wise accuracy. Unlike Mean Squared Error (MSE), MAE is less sensitive to outliers (individual points with large errors), providing a more robust estimate of the average deviation.

The combined use of RL2 and MAE enables a more comprehensive evaluation of point cloud reconstruction algorithm performance: RL2 focuses on the fidelity of global, while MAE assesses localized accuracy. Lower values for both metrics collectively indicate superior reconstruction quality.

D FULL IMPLEMENTATION DETAILS

The implementation software of the model is mainly based on PyTorch 2.4.1, CUDA 12.1, and Python 3.9.0. The computing platform mainly includes Ubuntu 22.04.4 LTS and 4 NVIDIA H100 GPUs.

Table 4: The hyperparameters and training configuration of MNO for different benchmarks.

Benchmark	N	Block	M	D	Head	k_{nbr}	Batch	Epoch	Loss	Optimizer	Scheduler
ShapeNet Car	30k					16					
DrivAerNet++	300k					8					
Ahmed body	100k	4	256	128	8	16	4	500	RL2	AdamW	OneCycleLR
Parachute	15k					16					

Table 4 details the hyperparameter configurations used during training. Here, N denotes the scale of point clouds per sample, Block indicates the number of MNO blocks, M represents the number of tokens in the low rank space of the Global Attention module, D signifies the vector dimension per token, Head refers to the number of heads in the Multi-head Self-Attention (MSA) mechanism, and k_{nbr} specifies the number of neighboring nodes in the Local Attention module. The training

employed a relative L2 error loss function over 500 epochs. Optimization is performed using the AdamW optimizer coupled with a OneCycleLR learning rate scheduler, with the initial learning rate set to 1×10^{-3} .

E THE ABLATION EXPERIMENTS OF THE DEPTH OF MNO

This experiment aims to explore performance changes in Global Attention, Local Attention, and Micro Attention modules with varying depths of the MNO model.

Due to the large number of models requiring training in this experiment, to enhance experimental efficiency, ablation studies are performed exclusively on the smaller-scale point cloud datasets: ShapeNet Car and Parachute. ShapeNet Car necessitates simultaneous prediction of velocity and pressure fields, while Parachute incorporates temporal information, making both highly representative benchmarks.

Table 5: The ablation experimental results of depth of MNO model. Blocks refer to the number of cascaded MNO blocks in the model. $RL2_{x1\sim4}$ represent the RL2 of the displacement field at 4 time steps. $RL2_x$ denotes the total RL2 of 4 time steps.

Blocks	Modules	ShapeNet Car				Parachute					
		$RL2_v$	MAE_v	$RL2_p$	MAE_p	$RL2_{x1}$	$RL2_{x2}$	$RL2_{x3}$	$RL2_{x4}$	$RL2_x$	MAE_x
1	Global	0.0252	0.1315	0.0813	2.1268	0.0535	0.0380	0.0439	0.0615	0.0455	0.0135
	Local	0.0526	0.2637	0.1191	4.1156	0.0777	0.0872	0.1263	0.2221	0.1353	0.0315
	Micro	0.0594	0.2925	0.1924	6.3051	0.1942	0.1967	0.2504	0.3138	0.2408	0.0581
	Global+Local	0.0220	0.1130	0.0686	1.7701	0.0319	0.0250	0.0358	0.0531	0.0361	0.0110
	Global+Local+Micro	0.0196	0.0999	0.0672	1.6221	0.0310	0.0239	0.0336	0.0500	0.0340	0.0105
2	Global	0.0266	0.1481	0.0852	2.1712	0.0342	0.0236	0.0323	0.0490	0.0330	0.0102
	Local	0.0465	0.2328	0.0959	3.4201	0.0569	0.0641	0.1022	0.1671	0.1045	0.0251
	Micro	0.0586	0.0586	0.1906	0.2893	0.1813	0.1894	0.2429	0.3042	0.2335	0.0553
	Global+Local	0.0197	0.0972	0.0632	1.5172	0.0245	0.0185	0.0291	0.0453	0.0294	0.0093
	Global+Local+Micro	0.0192	0.0946	0.0612	1.4408	0.0231	0.0172	0.0276	0.0441	0.0281	0.0088
4	Global	0.2025	1.3195	0.5117	16.9729	0.7308	0.7884	0.8502	0.8143	0.8205	0.2629
	Local	0.0396	0.1965	0.0817	2.8447	0.0455	0.0911	0.1545	0.2099	0.1479	0.0314
	Micro	0.0609	0.3098	0.1881	6.2470	0.1812	0.1869	0.2402	0.3010	0.2307	0.0542
	Global+Local	0.0201	0.0983	0.0610	1.4994	0.0250	0.0183	0.0289	0.0438	0.0287	0.0090
	Global+Local+Micro	0.0178	0.0845	0.0597	1.3796	0.0216	0.0164	0.0259	0.0418	0.0266	0.0081
8	Global	0.3252	1.9870	0.7991	23.7101	0.7659	0.8413	0.8981	0.8552	0.8661	0.2713
	Local	0.0319	0.1644	0.0728	2.3717	0.1106	0.1242	0.1916	0.2549	0.1790	0.0472
	Micro	0.0584	0.2916	0.1880	6.1920	0.1727	0.1804	0.2361	0.2949	0.2254	0.0525
	Global+Local	0.0201	0.1006	0.0614	1.4902	0.0392	0.0313	0.0401	0.0558	0.0402	0.0123
	Global+Local+Micro	0.0194	0.0857	0.0604	1.3986	0.0239	0.0163	0.0235	0.0399	0.0250	0.0078

Table 5 presents the experimental results. It is evident that the MNO model incorporating all three attention modules achieves the highest prediction accuracy in most cases. A significant improvement in MNO’s predictive performance is observed as the number of blocks increases from 1 to 4. However, performance gains become marginal when the block count exceeds 4, suggesting that the model likely enters an overfitting state at this stage.

Notably, the predictive performance of Local Attention and Micro Attention modules exhibits a positive correlation with the number of blocks, whereas Global Attention module performance shows an inverse correlation. This occurs because the low rank projection within Global Attention discards certain mid-to-high frequency information. Cascading multiple MNO blocks increases the number of low rank projections, thereby amplifying the loss of detailed information. In contrast, Local Attention incorporates pos_{rel} to mitigate feature distortion caused by network deepening, and Micro Attention employs residual branches to supplement fine-grained details.

In summary, as the depth of the MNO model increases, the division of labor among different attention modules becomes more distinct. Global Attention increasingly focuses on analyzing global low-frequency features, while Local Attention and Micro Attention dedicate greater emphasis to capturing local mid-to-high-frequency details.

F THE DISPLAY AND DISCUSSION OF PREDICTION RESULTS OF MNO MODEL

In this section, we present prediction results obtained by the proposed MNO model, as illustrated in Figures 3, Figure 4, Figure 5, and Figure 6. It is evident that across all datasets, the model’s predictions exhibit strong consistency with the ground truth, with prediction errors approaching zero in most regions of the point cloud. These results confirm that the MNO model is capable of capturing the majority of physical behaviors in fluid flows, making it highly suitable for CFD tasks.

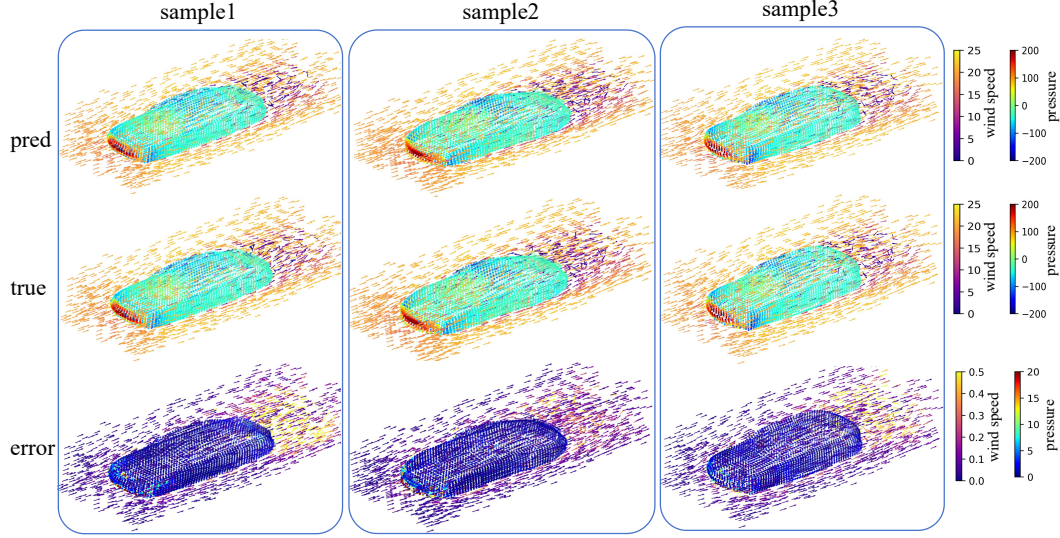


Figure 3: The display of prediction results on ShapeNet Car dataset. The pred represents the predicted velocity and pressure fields, the true denotes the ground truth, and the error stands for the absolute error of the prediction fluid fields. The arrows represent the wind direction, and the color of arrows denotes the magnitude of wind speed.

Among the benchmarks, the ShapeNet Car dataset merits particular attention, as the model is required to simultaneously predict both the velocity field of the airflow around the car and the pressure field normal to the car surface. Figure 3 presents the experimental results on this dataset. From the “true” visualization, one can observe that the windward regions of the car surface exhibit higher pressure, while the leeward and side regions experience lower pressure. As the airflow passes the vehicle body, its velocity decreases and complex wake turbulence forms downstream of the car. In the “pred” visualization, the model successfully reproduces the contrast between windward and leeward surfaces, as well as the turbulent structures in the wake, indicating that MNO has effectively learned the underlying PDEs governing wind tunnel phenomena from point cloud data. In the “error” visualization, relatively large prediction errors are observed at the front surface of the car, where the windward face encounters high-speed inflow and rapid flow variations, making the prediction more challenging. Similarly, noticeable errors appear in the downstream velocity field due to the highly complex turbulent dynamics in the wake region.

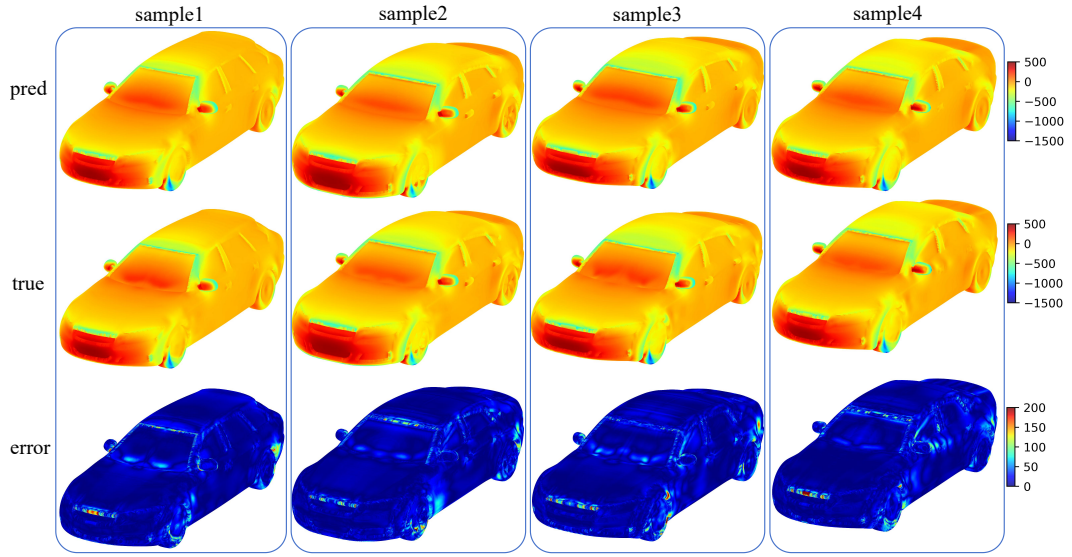


Figure 4: The display of prediction results on DrivAerNet++ dataset. The pred represents the predicted pressure fields, the true denotes the ground truth, and the error stands for the absolute error of the prediction fluid fields.

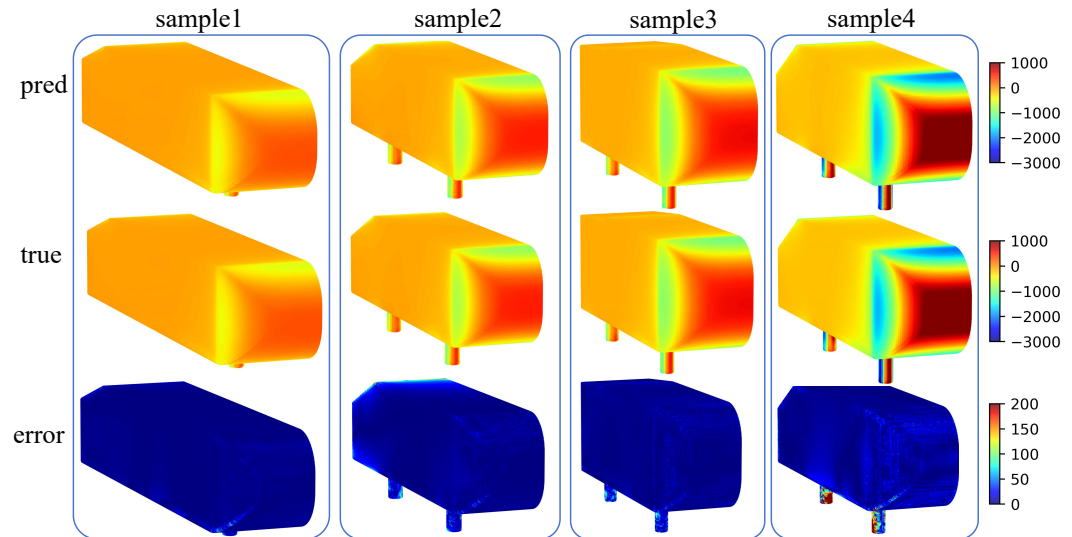


Figure 5: The display of prediction results on Ahmed body dataset. The pred represents the predicted pressure fields, the true denotes the ground truth, and the error stands for the absolute error of the prediction fluid fields.

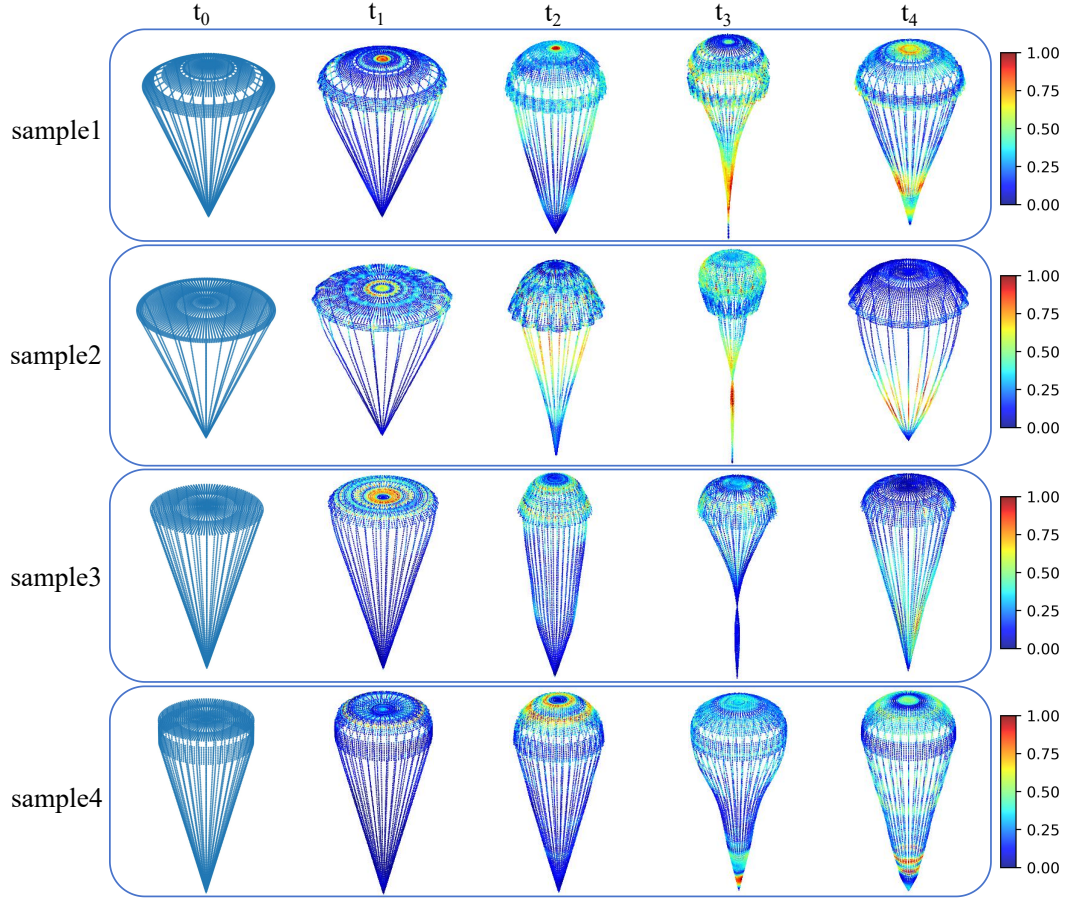


Figure 6: The display of prediction results on Parachute dataset. t_0 is the initial shape of the parachute in the air, while t_1, t_2, t_3 , and t_4 stand for the shape changes of the parachute over 4 time steps. The color of the point cloud represents the prediction error amplitude of displacement fields.