

Hydration Free Energies of Linear Alkanes: Evaluating and Correcting Classical Force Field Predictions with Different Water Models

Yalda Ramezani and Sumit Sharma^{1*}

*Department of Chemical and Biomolecular Engineering, Ohio University, Athens, OH -
45701*

E-mail: sharmas@ohio.edu

Abstract

Common force fields tend to overestimate the hydration free energies of hydrophobic solutes, leading to an exaggerated hydrophobic effect. We compute the hydration free energies of linear alkanes from methane to eicosane ($C_{20}H_{42}$) using free energy perturbation with various three-site (SPC/E, OPC3) and four-site (TIP4P/2005, OPC) water models and the TraPPE-UA force field for alkanes. All water models overestimate the hydration free energies, though the four-site models perform better than the three-site ones. By utilizing cavity free energies, we reparameterize the alkane–water well-depth to bring simulation results in agreement with experimental and group-contribution estimates. We find that the General Amber force Field (GAFF) combined with TIP4P/2005 water provides closer estimates of the hydration free energy. The HH-alkane model (a reparameterized TraPPE-UA force field) with TIP4P/2005 reproduces experimental hydration free energies. We also show that applying a shifted

¹Corresponding author: Sumit Sharma

Lennard-Jones potential leads to systematic deviations in the hydration free energy estimates.

1 Introduction

The hydrophobic effect is a fundamental driving force in many chemical and biological processes, including the self-assembly of surfactants and lipids into micelles and membranes, the folding and stability of proteins, binding of ligands into hydrophobic pockets of proteins, and coalescence of oil droplets in water.^{1,2} Recent molecular simulation works have noted that the commonly used force fields tend to exaggerate the hydrophobic effect, leading to underestimated critical micelle concentrations of surfactants and overestimated oil-water interfacial adsorption free energies.³⁻⁵ These systematic deviations highlight the need for improved parameterizations of existing force fields.

Alkanes in water serve as a model system to understand the behavior of non-polar species in aqueous environments. A key property of interest is their solubility, which can be quantified by the hydration free energy, or the change in free energy when an alkane transfers from the vapor to the aqueous phase. Hydration free energy can be estimated using molecular simulations, but the accuracy depends both on the choice of molecular force fields and the numerical implementation details. Molecular force fields are often parameterized on pure species thermodynamic properties. The inter-species force field parameters are then obtained by heuristic mixing rules. Lorentz-Berthelot being the most popular among them. The numerical implementation details refer to the chosen spatial potential cut-off and how the interactions are accounted for beyond the cut-off.⁶ In this work, we show that various water models overestimate the hydration free energies of linear alkanes (modeled via TraPPE-UA) when standard Lorentz-Berthelot mixing rules are used. Using the cavity free energies of alkanes, we provide a one-step mechanism to adjust the alkane-water well depth parameter to reproduce the experimental values. We also discuss the implications of using

shifted potentials on the absolute values of hydration free energies.

Non-polar species, like alkanes, do not strongly interact with water due to their inability to form hydrogen bonds and charge neutrality. Such species disrupt the molecular arrangement of water in their vicinity, making their dissolution in water unfavorable. Thus, non-polar species tend to aggregate in aqueous environments, which is referred to as the hydrophobic effect.¹ Hydrophobic effect is length-scale dependent.^{7,8} At small length-scales, where size of the solute is less than 1 nm, hydrophobic effect is entropically driven^{7,9,10} and the hydration free energy is proportional to solute volume.⁸ Hydration free energies of small solutes and their aggregation in water are well-described by the observation that water density fluctuations are Gaussian in small observation volumes.¹¹ For larger solutes, hydrophobic effect is dominated by the enthalpic loss of hydrogen bonds of water in the vicinity, and the hydration free energy scales proportional to the exposed surface area of the solute.^{8,12} Near large hydrophobic solutes, the low-density solvent fluctuations are enhanced relative to Gaussian statistics.^{13,14} Thus, water near large hydrophobic solutes sits at the edge of a dewetting transition.^{15,16} As a result, liquid water, when confined between large non-polar solutes, becomes metastable with respect to its vapor below a critical confinement gap.^{17–20} This phenomenon is understood to dictate the hydrophobic self-assembly of large solutes.

The Gibbs free energy of solvation is given by, $\Delta G_{hyd} = \Delta H_{hyd} - T\Delta S_{hyd}$, where ΔH_{hyd} is the change in the enthalpy when the solute enters the aqueous phase, and ΔS_{hyd} is the associated change in the entropy. ΔH_{hyd} comprises of solute-solvent direct interactions ΔE_{UV} and changes in the solvent-solvent interactions, ΔH_{VV} ($= \Delta E_{VV} + P\Delta V$). The ΔH_{VV} exactly cancels out the solvent’s entropic contribution, $T\Delta S_{VV}$.²¹ Therefore, the ΔH_{hyd} is determined entirely by the solute-solvent contribution, that is, $\Delta G_{hyd} = \Delta E_{UV} - T\Delta S_{UV}$.²¹ Previous works have shown that the positive (unfavorable) ΔG_{hyd} of alkanes arise from a near perfect cancellation of the attractive (favorable) solute-solvent interactions, ΔE_{UV} and the unfavorable solute-solvent entropic term, $T\Delta S_{UV}$.²¹ The ΔG_{hyd} can also be broken down

into the free energy of creating a solute-sized cavity, ΔG_{cavity} , and the energetic contribution from the attractive solute-solvent interactions, ΔH_{att} .²²

Several experiments have reported the solubility of linear alkanes in water, but reliable estimates are available only up to decane because of the extremely low solubilities of longer alkanes.^{23–31} Cabani et al.³² developed a group contribution method based on the experimentally known solubilities of small alkanes to predict the solubilities of linear- and cyclo-alkanes. This group contribution method was updated for aliphatic and mono-aromatic hydrocarbons, monohydric alcohols, and aliphatic, non-cyclic ketones.^{33,34} In a group contribution method, the thermodynamic property of interest is correlated with the number and types of molecular fragments that make up a molecule, allowing estimation of average contribution of each molecular fragment towards that thermodynamic property.

Aqueous solubility of alkanes has been a subject of several molecular simulation studies. Ferguson et al.³⁵ employed the Transferable Potentials for Phase Equilibria (TraPPE)-United Atom (UA) force field³⁶ for alkanes and Simple Point Charge Enhanced (SPC/E) water model.³⁷ Using the incremental Widom insertion technique³⁸ and a potential cutoff of 9.875 Å for both Lennard-Jones and electrostatic interactions, they determined the aqueous solubility of n-alkanes up to docosane (C_{22}). While Ferguson et al.’s³⁵ calculations matched experimental values, other studies that employed the same molecular potentials reported deviations from the experiments.^{39,40}

Ashbaugh and coworkers⁴⁰ compared ten different water models for their ability to reproduce experimental temperature-dependence of liquid water density and methane hydration and concluded that the TIP4P/2005 water model performs the best. Ashbaugh et al.⁴¹ calculated the hydration free energy of linear and branched alkanes using the TraPPE-UA + TIP4P/2005 potentials for alkanes and water, respectively, via thermodynamic integration. They concluded that the hydration free energies are overestimated compared to the experimental values when the standard Lorentz-Berthelot mixing rules are used. They adjusted the Lennard-Jones well depth parameter between the alkane united atoms and water

oxygen to match the experimental data. The new model, called HH-Alkane, reduced the deviation of hydration free energy from experiments to 0.25 kJ/mol on average. However, their simulations were performed for alkanes of size up to butane and neopentane.

Chen and Siepmann⁴² studied hydration of small alkanes via Gibbs ensemble Monte Carlo simulations using the Optimized Potentials for Liquid Simulations (OPLS) force field⁴³ for alkanes and the TIP4P model of water. They reported that the hydration free energy of alkanes from the simulations was consistently higher than the experimental values. Similar conclusions were drawn in another study by Siepmann and coworkers³⁹ where they employed the TraPPE force field for n-alkanes along with different water models: TIP4P, TIP4P/2005, and SPC/E. Interestingly though, they found that the hydration free energies are closer to the experimental values for the SPC/E water model compared to the TIP4P/2005 water model. Singh and Sharma⁴⁴ reported large deviations in the hydration free energies of n-alkanes from the experimental values. They employed the General Amber Force Field (GAFF)⁴⁵ for alkanes and SPC/E water with a spherical cutoff of 10 Å and the potentials shifted by their value at the cutoff distance.

In this work, we calculate the hydration free energies of linear alkanes up to eicosane ($C_{20}H_{42}$) using the TraPPE-UA force field for alkanes combined with various three- and four-point water models. All tested water models systematically overestimate the hydration free energies. The "Optimal 3-Charge, 4-Point rigid" (OPC) water model⁴⁶ and its 3-site counterpart OPC3,⁴⁷ designed by optimizing charge distributions to capture bulk electrostatics, yield hydration free energies similar to those from TIP4P/2005 and SPC/E, respectively. This indicates that OPC and OPC3 do not improve predictions for non-polar solutes. By utilizing the free energy of cavity formation, we adjust the alkane-water Lennard-Jones well depth parameter (ϵ) for each model to match experimental values. Remarkably, in all cases, the well-depth parameter needs to be increased by about 5% relative to the Lorentz-Berthelot mixing rule. We further show that the HH-alkane model with TIP4P/2005 water reproduces experimental hydration free energies up to eicosane. Similarly, the General Am-

ber force Field (GAFF) combined with TIP4P/2005 water model provides good agreement with experiments.

Finally, we demonstrate that shifting the Lennard-Jones potential by its value at the spherical cutoff further increases deviations from the experiment. More broadly, these results highlight that molecular force fields parameterized on pure-component thermodynamics often perform poorly for mixtures when heuristic mixing rules like Lorentz-Berthelot are used. For non-polar species like alkanes, accurate hydration free energies can be obtained by directly calibrating the interaction parameters using cavity-formation free energies.

2 Simulation System and Methods

A widely used force field for alkanes is the Transferable Potentials for Phase Equilibria (TraPPE)- United Atom (UA) model.³⁶ In this model, each alkyl group is represented as a single united atom bead, with distinct sites defined for CH_4 , $-CH_3$, and $-CH_2$. Beyond alkanes, TraPPE-UA has also been parameterized for alcohols, thiols, ethers, sulfides, aldehydes, ketones, nitriles, cycloalkanes, and aromatics. We evaluate the performance of TraPPE-UA with the General Amber Force field (GAFF)⁴⁵ and the HH-alkane model.⁴¹ For water, we employ four commonly used models: SPC/E, OPC3, TIP4P/2005, and OPC. SPC/E and OPC3 are three-site models, while TIP4P/2005 and OPC are four-site models, in which the negative charge is shifted off the oxygen atom onto the $H - O - H$ angle bisector.⁴⁶⁻⁴⁸

Hydration free energies of alkanes are calculated using the free energy perturbation (FEP) method.^{3,49} Alkane-water interactions are described by a soft-core Lennard-Jones potential (equation 1),⁵⁰ with $\alpha = 0.5$ and $n = 2$. The coupling parameter λ is varied from 0 to 1 in 40 windows with $\Delta\lambda = 0.025$. Each window is simulated for 6 ns, and ensemble averages are computed from the last 4.5 ns. Accuracy is validated by also tracing the reverse path ($\lambda = 1$ to 0) with the same protocol. Reported uncertainties are standard deviation over three

independent simulations.

$$V(\lambda, r) = \lambda^n 4\epsilon \left[\left(\alpha(1 - \lambda)^2 + \left(\frac{r}{\sigma} \right)^6 \right)^{-2} - \left(\alpha(1 - \lambda)^2 + \left(\frac{r}{\sigma} \right)^6 \right)^{-1} \right] \quad (1)$$

Hydration free energy is calculated in the isothermal-isobaric ensemble using equation 2.^{51,52}

$$\Delta G = -k_B T \sum_{i=0}^{n-1} \ln \left(\frac{\langle V \exp \left(-\frac{U(\lambda_{i+1}) - U(\lambda_i)}{k_B T} \right) \rangle_{\lambda_i}}{\langle V \rangle_{\lambda_i}} \right) \quad (2)$$

The simulation system comprises one alkane molecule in bulk water. Nominal size of the cubic simulation system is selected to ensure that the periodic images of the alkane do not interact with each other (Table S1, Supporting Information). Periodic boundary conditions are applied in all directions. Coulombic interactions between water molecules are calculated using Particle-Particle Particle Mesh Ewald summation with an accuracy of 10^{-4} . Lennard-Jones and real-space part of the Coulombic interactions between water molecules are truncated at a spherical cutoff of 10 Å. The Lennard-Jones interactions between water-oxygen and alkane atoms have a spherical cutoff of 14 Å as recommended in the TraPPE-UA force field.⁵³ Unless noted otherwise, the potential functions are not shifted by their value at the spherical cut-off, and long-range/tail corrections to the potential and pressure are applied for Lennard-Jones interactions. The simulations are performed in the isothermal-isobaric ensemble at the temperature $T = 300$ K and the pressure $P = 1$ bar. Temperature and pressure in the system are maintained using the Nose-Hoover thermostat and barostat respectively. All simulations are conducted using the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS).⁵⁴ Initial configurations are generated using the PACKMOL package.⁵⁵

3 Results and Discussion

Figure 1(a) presents the hydration free energies, ΔG_{hyd} of alkanes from methane to eicosane, calculated using the TraPPE-UA alkane potential with four different water models (SPC/E, OPC3, TIP4P/2005, and OPC). The results are compared with experimental ΔG_{hyd} values up to octane and with estimates from the group contribution method³² for longer alkanes. For all water models, the TraPPE-UA force field overpredicts ΔG_{hyd} . The deviations are larger for the 3-point water models (SPC/E and OPC3) than for the 4-point water models (TIP4P/2005, OPC), and the deviations increase with alkane length. The two 3-point water models yield similar results, as do the two 4-point water models. Our results are consistent with the observation by Kanduč et al.³ and others^{4,5} who report that the currently available atomistic force fields systematically yield stronger adsorption affinities for oil-water interfaces and under-predict the critical micelle concentration. Our ΔG_{hyd} values match well with the estimates in previous studies as shown in the Table S2 (Supporting Information).

To reconcile the hydration free energies obtained from the TraPPE-UA force field with different water models, we re-parameterize the alkane-water Lennard-Jones well-depth parameter, ϵ . The hydration free energy can be expressed as $\Delta G_{hyd} = \Delta G_{cavity} + \Delta H_{att}$, where $\Delta H_{att} \approx \Delta U_{att}$ corresponds to the alkane-water Lennard Jones interaction energy. Values of ΔG_{cavity} are taken from previous studies.^{44,56} The experimental (or group contribution) estimate of the ΔH_{att} can then be obtained as $\Delta H_{att}^{exp} = \Delta G_{hyd}^{exp} - \Delta G_{cavity}$. Analogously, ΔH_{att} can be computed for each alkane + water model combination. For small perturbations to ϵ , the local solvent structure around the alkane is assumed unchanged. Therefore, the updated ϵ is found as $\epsilon^{updated} = \frac{\Delta H_{att}^{exp}}{\Delta H_{att}} \times \epsilon$. This procedure is demonstrated for the SPC/E water model in Table 1. Interestingly, for all the models, ϵ needs to be increased by approximately 5% relative to its Lorentz-Berthelot value. Applying it to all the water models yields the updated ϵ values summarized in Table 2. Figure 1(b) shows that the ΔG_{hyd} obtained using the updated ϵ for all the water models have an excellent match with the experiments/group

contribution values, except for OPC3, which shows some deviation for large alkanes.

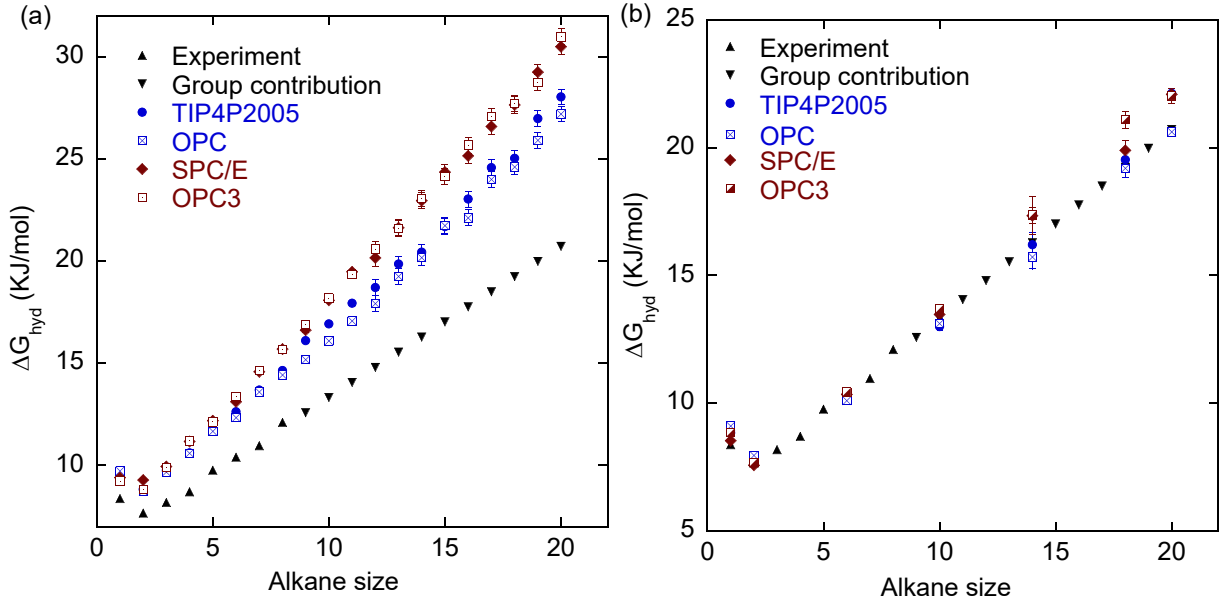


Figure 1: (a) Hydration free energies, ΔG_{hyd} of alkanes using the TraPPE-UA model and different water models. All models show positive deviation from the experiments/group contribution. The 3-point water models show larger deviation from the experimental/group contribution values compared to the 4-point water models. (b) ΔG_{hyd} of alkanes using the TraPPE-UA model but with the alkane-water well depth parameter updated via the method discussed in the text. An excellent match with the experimental/group-contribution values is found, except for some deviations observed with the OPC3 model for large alkanes.

Table 1: Comparison of experimental hydration data with TraPPE-UA + SPC/E and updated SPC/E models. The units are in [kJ/mol]. $\Delta G_{hyd}^{SPC/E,pred}$ are the predicted ΔG_{hyd} values after updating the ϵ . $\Delta G_{hyd}^{SPC/E,sim}$ are the values obtained in the simulations.

Alkane	ΔG_{hyd}^{exp}	$\Delta G_{hyd}^{SPC/E}$	ΔG_{cavity}	ΔH_{att}^{exp}	$\Delta H_{att}^{SPC/E}$	$\Delta H_{att}^{SPC/E,updated}$	$\Delta G_{hyd}^{SPC/E,pred}$	$\Delta G_{hyd}^{SPC/E,sim}$
1	8.37	9.39	24.52	-16.15	-15.12	-15.96	8.56	8.53
2	7.66	9.28	34.87	-27.21	-25.59	-27.01	7.86	7.57
3	8.18	9.94	43.85	-35.67	-33.91	-35.78	8.07	
4	8.70	11.16	52.55	-43.85	-41.39	-43.68	8.87	
5	9.76	12.19	61.86	-52.10	-49.67	-52.42	9.44	
6	10.4	13.11	70.34	-59.94	-57.23	-60.40	9.94	10.34
8	12.1	15.69	87.72	-75.62	-72.03	-76.01	11.71	
10	13.32	18.08	105.75	-92.43	-87.68	-92.53	13.23	13.47
12	14.80	20.15	123.36	-108.56	-103.21	-108.92	14.44	
14	16.28	22.95	140.80	-124.52	-117.85	-124.37	16.43	17.34
16	17.76	25.15	157.81	-140.05	-132.66	-140.00	17.81	
18	19.24	27.64	174.72	-155.48	-147.08	-155.21	19.51	19.90

Ashbaugh et al.⁴¹ reported that the TraPPE-UA force field combined with TIP4P/2005

Table 2: Original and updated Lennard-Jones well-depth parameter (ϵ) for CH₄-O, CH₃-O, and CH₂-O for different water models in [kJ/mol]. The sigma (σ) parameter was not modified.

	CH ₄ -O		CH ₃ -O		CH ₂ -O	
	ϵ	$\epsilon^{updated}$	ϵ	$\epsilon^{updated}$	ϵ	$\epsilon^{updated}$
SPC/E	0.8942	0.9436	0.7276	0.7679	0.4985	0.5261
OPC3	0.9172	0.9668	0.7464	0.7867	0.5114	0.5390
OPC	1.0467	1.0841	0.8517	0.8822	0.5835	0.6044
TIP4P2005	0.9765	1.0169	0.7946	0.8274	0.5444	0.5669

water overestimates the hydration free energies of small alkanes. To address this, they proposed the HH-alkane model, in which the alkane-water interaction parameters were re-parameterized. Their study validated the HH-alkane model against experimental data for alkanes up to butane and neopentane.⁴¹ Here, we extend their analysis by calculating the hydration free energies of linear alkanes up to eicosane using the HH-alkane + TIP4P/2005 water model. As shown in Figure 2, the resulting ΔG_{hyd} values are in excellent agreement with both the experimental/group-contribution data and our re-parameterized TraPPE + TIP4P/2005 force field combination.

We also calculated the ΔG_{hyd} using the General Amber Force Field (GAFF) with both the SPC/E and TIP4P/2005 water models. Figure 3 compares the ΔG_{hyd} obtained from GAFF with those from TraPPE-UA. The alkane-water interactions are determined using the Lorentz-Berthelot mixing rules in both cases. GAFF yields smaller deviations from the experimental and group contribution values compared to TraPPE-UA. Specifically, GAFF + SPC/E combination systematically overestimates the ΔG_{hyd} by roughly 1 to 1.6 kJ/mol. GAFF+TIP4P/2005 tends to overestimate ΔG_{hyd} for small alkanes but underestimates it for larger alkanes. Our results align with those of Luz et al.,⁴ who report that GAFF + SPC/E show too strong affinity of polyethoxylated alkyl ethers (C_8EO_m) to a heptane-water interface.

Lastly, we study the impact of potential shift on the ΔG_{hyd} calculations. Often, molecular interaction potentials are shifted by their value at the spherical cutoff so that the potential

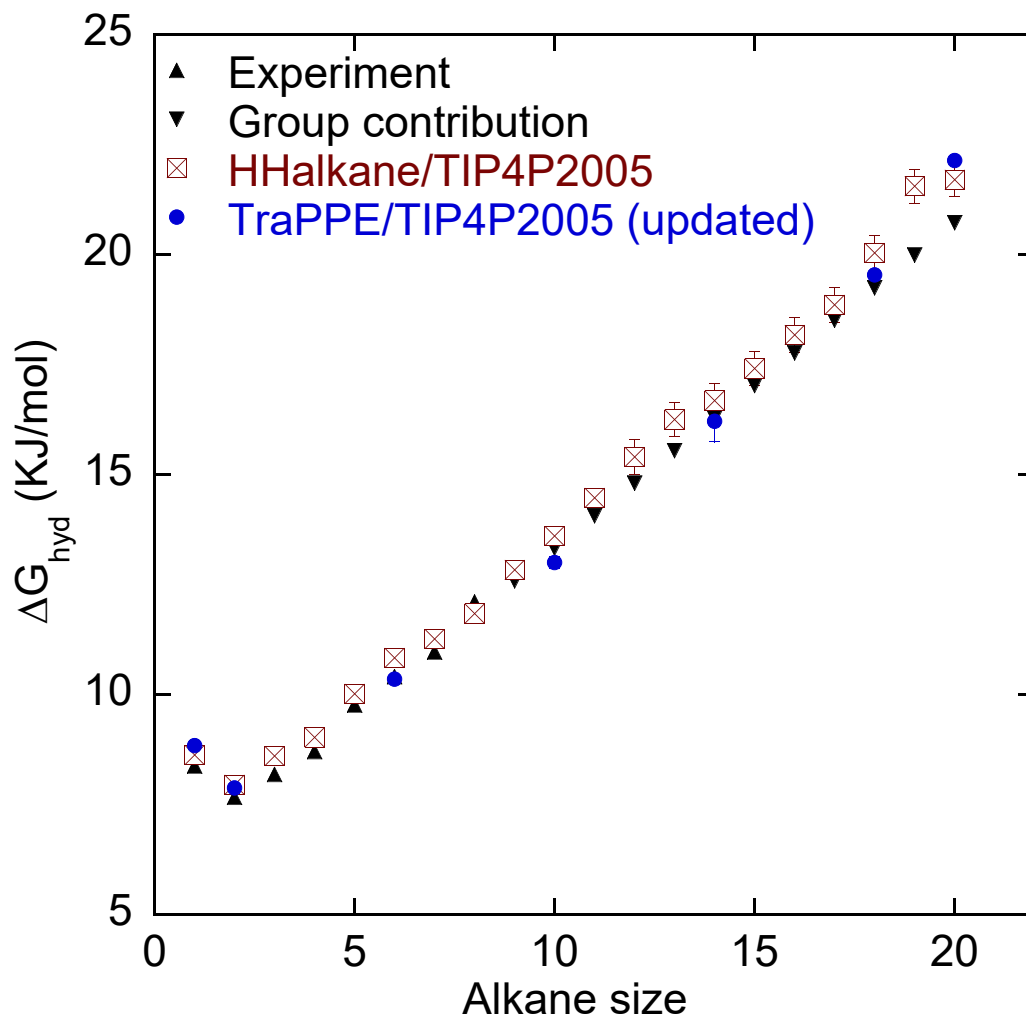


Figure 2: Hydration free energy of alkanes calculated using the HH-alkane model is compared with the TraPPE-UA force field and the experimental/group-contribution values. TIP4P/2005 water model is employed. The HH-alkane model matches the experimental/group contribution values well up to C_{20} .

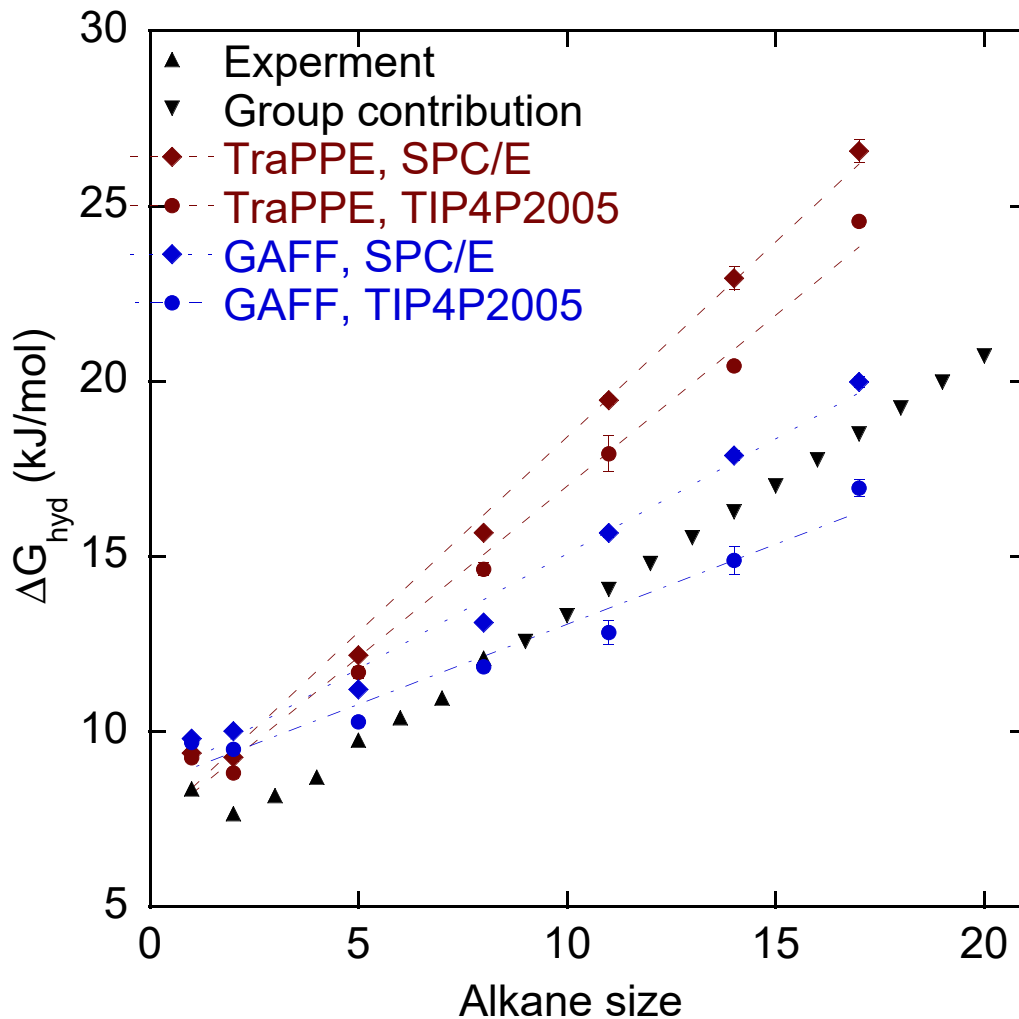


Figure 3: Hydration free energies of alkanes calculated using the General Amber Force Field (GAFF) all-atom model of alkanes and two different water models: SPC/E and TIP4P/2005. The results are compared with the TraPPE-UA model and experimental/group contribution values. Overall, results using GAFF are closer to the experimental/group contribution values compared to TraPPE. GAFF, SPC/E overestimates the ΔG_{hyd} values. GAFF, TIP4P/2005 overestimates the ΔG_{hyd} for small alkanes ($\leq C_5$) but underestimates the ΔG_{hyd} for large alkanes. Lines are guide to the eyes.

becomes zero at the cutoff, r_c . Shifted potential functions are given by,

$$u_{shift}(r_{ij}) = \begin{cases} u(r_{ij}) - u(r_c), & r_{ij} \leq r_c \\ 0, & r_{ij} > r_c \end{cases} \quad (3)$$

For the "unshifted" potentials, the contribution of the potential (which remains non-zero) beyond the r_c , called long-range or tail correction, is included for energy and pressure calculations. It should be noted that in molecular dynamics only the forces matter. So whether a potential function is shifted or not and whether a tail correction is applied or not does not influence the dynamics and final trajectories, except through pressure calculations, which could affect the NPT ensemble.

For molecules belonging to different species (for example, an alkane molecule in water), the expression for ensemble averaged interaction energy is given by,

$$\langle E \rangle = N_{alkane} \rho_{water} \int_0^\infty 2\pi r^2 g(r) u(r) dr \quad (4)$$

Where, N_{alkane} is the number of united atoms in the alkane molecule, ρ_{water} is the number density of water, and $g(r)$ is the alkane-water radial distribution function. Change in the energy due to the shifting of the potential by $u(r_c)$ is given by:

$$\langle \Delta E \rangle = N_{alkane} \rho_{water} u(r_c) \int_0^{r_c} 2\pi r^2 g(r) dr \quad (5)$$

Equation 5 can be approximated as,

$$\langle \Delta E \rangle = N_{alkane} \rho_{water} u(r_c) \left[\frac{2}{3} \pi \left((r_c - \sigma)^3 - (\tilde{N}_{alkane} - 1) \sigma^3 \right) \right] \quad (6)$$

In equation 6, the first term in the brackets assumes $g(r) = 1$ for $r > \sigma$ and 0 for $r < \sigma$. The second term accounts for the excluded volumes of other alkane united atoms. $\tilde{N}_{alkane}$ refers to the number of alkane united atoms that are within the r_c distance of one united atom.

For small alkanes, $\tilde{N}_{alkane} = N_{alkane}$. For the spherical cutoff, $r_c = 1.4$ nm, $\tilde{N}_{alkane} = 11$.

The tail contribution to the energy in the case of "unshifted" potential is also calculated through equation 4 with the assumption of $g(r) = 1$ for $r > r_c$. The tail contribution of the Lennard Jones interactions between alkane and water is given by,

$$\langle E_{LR} \rangle = N_{alkane} \rho_{water} 8\pi \epsilon \sigma^3 \left[\frac{\sigma^9}{9r_c^9} - \frac{\sigma^3}{3r_c^3} \right] \quad (7)$$

Figure 4 compares the ΔG_{hyd} obtained for the unshifted HH-alkane potential (labeled as HHalkane), the shifted HH-alkane (labeled as HHalkane (shifted)), the shifted HH-alkane with the effect of potential shift corrected using the equation 6 and the tail corrections added (labeled as HHalkane (shift adj., tail), and the shifted HH-alkane with only the tail corrections added (labeled as shifted, only tail). The main observation is that the shifted potential exacerbates the deviation from the experimental/group contribution values. The correction for the shifted potential + the tail correction results in a negative deviation from the ΔG_{hyd} obtained from the unshifted potential, with the largest deviation of 3.1 kJ/mol observed for C_{19} . Adding only the tail correction to the shifted potential matches the results of the unshifted potential, but this is just fortuitous.

Figure 5 shows the carbon-oxygen radial distribution functions, $g(r)$ for four different alkane-water systems. The $g(r)$ of C_{10} , C_{14} , and C_{20} are shifted vertically by 0.1 for ease of visualization. Beyond a weak first peak and a trough, the $g(r)$ is close to 1. Thus, the assumption in equation 6 of $g(r) = 1$ for $r > \sigma$ is justified. Table 3 compares the contribution of the potential shift on the ΔG_{hyd} calculated using the equations 6 and 5 for the case of HH-alkane with TIP4P/2005 water with a spherical cutoff of 1.4 nm. The table shows that the two estimates are close, justifying the approximation in equation 6.

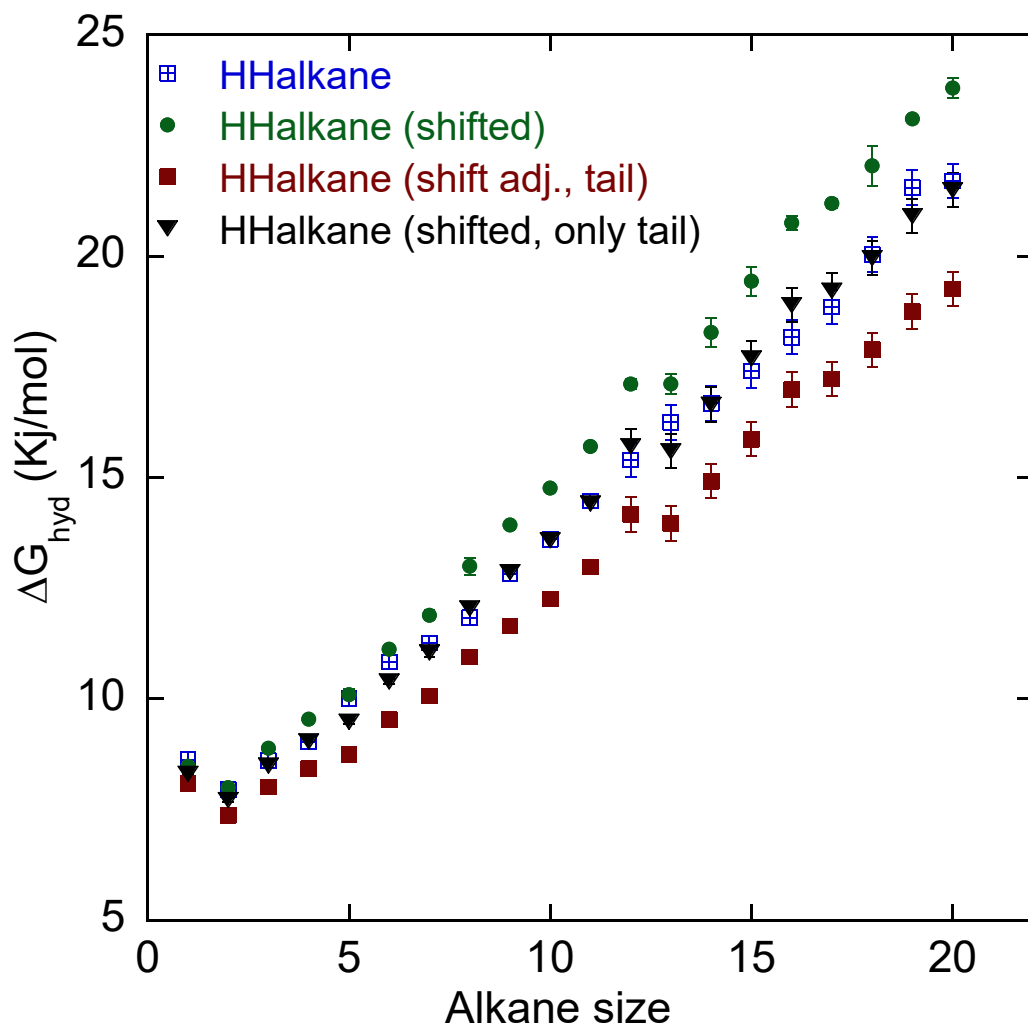


Figure 4: Hydration free energies, ΔG_{hyd} of alkanes for the unshifted HH-alkane (HHalkane) compared to those obtained for the shifted HH-alkane (HHalkane (shifted)); shifted HH-alkane with the potential shift corrected using equation 6 and tail corrections added (equation 7) (HHalkane (shift adj., tail)); and shifted potential with only tail corrections added (HHalkane (shifted, only tail)).

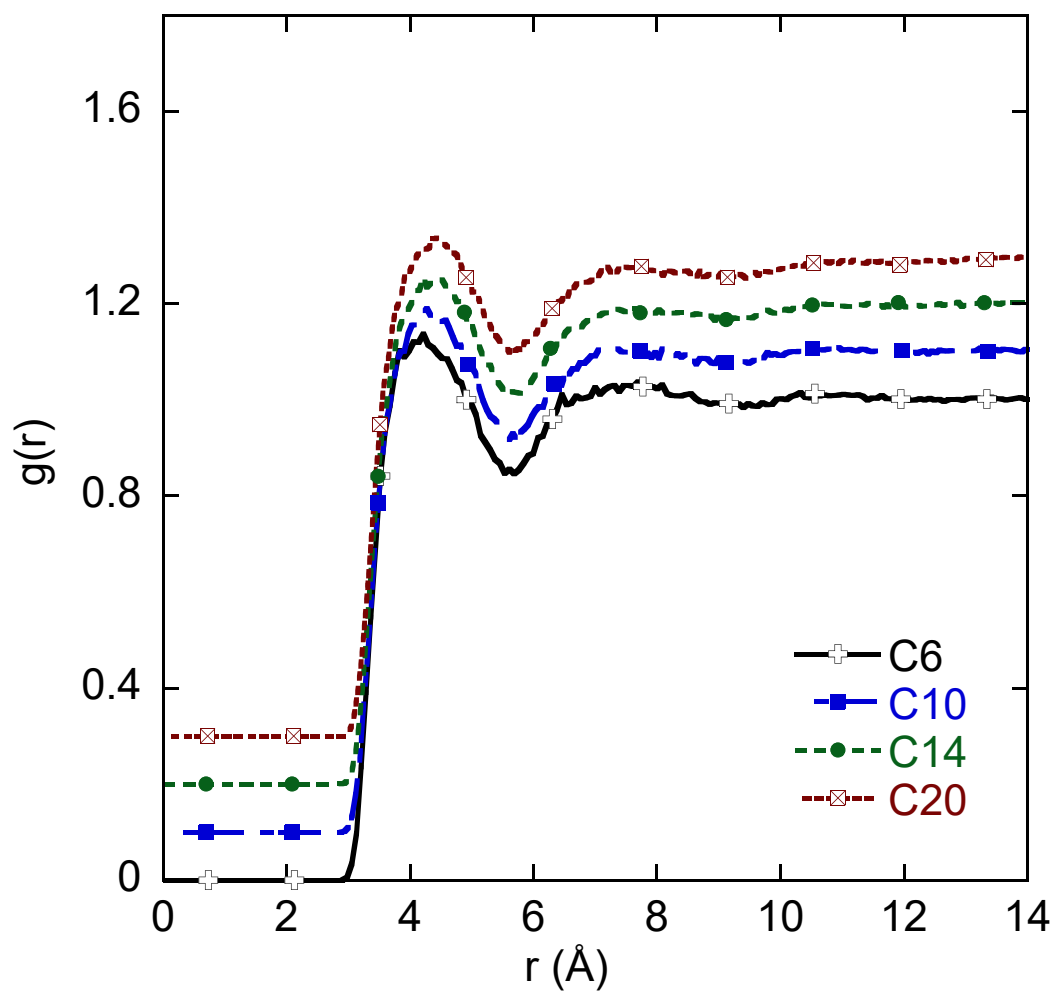


Figure 5: Carbon-oxygen radial distribution function for four different alkanes. The radial distribution functions of C_{10} , C_{14} , and C_{20} are shifted vertically by 0.1 from the previous graph for ease of visualization.

Table 3: Contribution of the potential shift to the hydration free energies, ΔG_{hyd} of different alkanes when the HH-alkane force field with TIP4P/2005 water is used with a spherical cutoff of 1.4 nm. The second column is the approximation based on the equation 6. Values in the third column are calculated from the radial distribution functions using the equation 5. The two estimates differ by only 0.33 kJ/mol at most.

Alkane	ΔE (eq. 6) (kJ/mol)	ΔE (eq. 5) (kJ/mol)
6	-0.87	-0.73
10	-1.34	-1.17
14	-1.82	-1.60
20	-2.58	-2.24

4 Conclusions

We show that the hydration free energies of linear alkanes from methane to eicosane ($C_{20}H_{42}$) computed using the TraPPE-UA alkane model and four water models (TIP4P/2005, OPC, SPC/E, OPC3) are systematically overestimated relative to experimental/group contribution values when Lorentz-Berthelot mixing rules are applied. Using the cavity free energies of alkanes, we adjust the alkane-water Lennard Jones well-depth parameter (ϵ) to match the hydration free energies to the experimental/group-contribution values. Interestingly, for each water model, the optimal ϵ is approximately 5% greater than its Lorentz-Berthelot value. The General Amber Force Field (GAFF) all-atom alkane model exhibits smaller deviations from experimental/group contribution values. Finally, we show that applying shifted potential functions increases the deviation of the hydration free energies from the experimental/group contribution values.

Author Contributions

S.S. conceptualized the project. Y.R. and S.S. designed the methodology. Experiments were performed and analyzed by Y.R. Y.R. and S.S. wrote the original manuscript draft, and performed editing and review. S.S. supervised the project and obtained resources.

Acknowledgement

This work is supported by the National Science Foundation (NSF) CAREER grant 2046095. Computational resources for this work were provided by the NSF ACCESS grant DMR190005 and NSF MRI grant 2320493. The authors acknowledge detailed discussions with Drs. Amish Patel, Matej Kanduč, Dor Ben-Amortz, Hank Ashbaugh, Michael R. Shirts, Andrew Ferguson, Ilja Siepmann, and Himanshu Singh.

5 Conflicts of Interest

The authors have no conflict of interest to declare.

6 Data availability

The data that support the findings of this study are openly available in Zenodo at <https://doi.org/10.5281/zenodo.15875249>.⁵⁷

7 Supporting Information

Supporting information is available. Table S1 lists details of the alkane-water simulation systems. Table S2 compares our hydration free energy estimates with those reported in previous studies. Table S3 lists ΔG_{hyd} from experiments, group-contribution, and all the four water models with alkane-water interaction parameters estimated using the Lorentz-Berthelot mixing rules. Table S4 lists the ΔG_{hyd} obtained for the four water models with the updated alkane-water well-depth parameter (ϵ). Table S5 lists the ΔG_{hyd} from GAFF with TIP4P/2005 and SPC/E.

References

- (1) Tanford, C. The hydrophobic effect and the organization of living matter. *Science* **1978**, *200*, 1012–1018.
- (2) Southall, N. T.; Dill, K. A.; Haymet, A. A view of the hydrophobic effect. *The Journal of Physical Chemistry B* **2002**, *106*, 521–533.
- (3) Kanduc, M.; Stubenrauch, C.; Miller, R.; Schneck, E. Interface adsorption versus bulk micellization of surfactants: insights from molecular simulations. *Journal of Chemical Theory and Computation* **2023**, *20*, 1568–1578.
- (4) Luz, A. M.; Dos Santos, T. J.; Barbosa, G. D.; Camargo, C. L.; Tavares, F. W. A molecular study on the behavior of polyethoxylated alkyl ethers surfactants in a water/n-alkane interface. *Colloids and Surfaces A: Physicochemical and Engineering Aspects* **2022**, *651*, 129627.
- (5) Jusufi, A.; Panagiotopoulos, A. Z. Explicit-and implicit-solvent simulations of micellization in surfactant solutions. *Langmuir* **2015**, *31*, 3283–3292.
- (6) Whitmore, L. M.; Ramezani, Y.; Sharma, S.; Shirts, M. R. Force switching and potential shifting lead to significant cutoff dependence in alchemical free energies. *Journal of Chemical Theory and Computation* **2024**,
- (7) Lum, K.; Chandler, D.; Weeks, J. D. Hydrophobicity at small and large length scales. *The Journal of Physical Chemistry B* **1999**, *103*, 4570–4577.
- (8) Rajamani, S.; Ghosh, T.; Garde, S. Size dependent ion hydration, its asymmetry, and convergence to macroscopic behavior. *The Journal of chemical physics* **2004**, *120*, 4457–4466.
- (9) Ashbaugh, H. S.; Pratt, L. R. Colloquium: Scaled particle theory and the length scales of hydrophobicity. *Reviews of Modern Physics* **2006**, *78*, 159–178.

- (10) Chandler, D. Interfaces and the driving force of hydrophobic assembly. *Nature* **2005**, *437*, 640–647.
- (11) Hummer, G.; Garde, S.; Garcia, A. E.; Pohorille, A.; Pratt, L. R. An information theory model of hydrophobic interactions. *Proceedings of the National Academy of Sciences* **1996**, *93*, 8951–8955.
- (12) Wallqvist, A.; Berne, B. Computer simulation of hydrophobic hydration forces on stacked plates at short range. *The Journal of Physical Chemistry* **1995**, *99*, 2893–2899.
- (13) Jamadagni, S. N.; Godawat, R.; Garde, S. Hydrophobicity of proteins and interfaces: Insights from density fluctuations. *Annual review of chemical and biomolecular engineering* **2011**, *2*, 147–171.
- (14) Patel, A. J.; Varilly, P.; Chandler, D. Fluctuations of water near extended hydrophobic and hydrophilic surfaces. *The journal of physical chemistry B* **2010**, *114*, 1632–1637.
- (15) Patel, A. J.; Varilly, P.; Jamadagni, S. N.; Hagan, M. F.; Chandler, D.; Garde, S. Sitting at the edge: How biomolecules use hydrophobicity to tune their interactions and function. *The Journal of Physical Chemistry B* **2012**, *116*, 2498–2503.
- (16) Zhou, R.; Huang, X.; Margulis, C. J.; Berne, B. J. Hydrophobic collapse in multidomain protein folding. *Science* **2004**, *305*, 1605–1609.
- (17) Sharma, S.; Debenedetti, P. G. Evaporation rate of water in hydrophobic confinement. *Proceedings of the National Academy of Sciences* **2012**, *109*, 4365–4370.
- (18) Sharma, S.; Debenedetti, P. G. Free energy barriers to evaporation of water in hydrophobic confinement. *The Journal of Physical Chemistry B* **2012**, *116*, 13282–13289.
- (19) Luzar, A. Activation barrier scaling for the spontaneous evaporation of confined water. *The Journal of Physical Chemistry B* **2004**, *108*, 19859–19866.

- (20) Kanduč, M.; Schlaich, A.; Schneck, E.; Netz, R. R. Water-mediated interactions between hydrophilic and hydrophobic surfaces. *Langmuir* **2016**, *32*, 8767–8782.
- (21) Ben-Amotz, D. Water-mediated hydrophobic interactions. *Annual review of physical chemistry* **2016**, *67*, 617–638.
- (22) Rensing, R. C.; Patel, A. J. Water density fluctuations relevant to hydrophobic hydration are unaltered by attractions. *The Journal of Chemical Physics* **2015**, *142*.
- (23) Khadikar, P. V.; Mandloi, D.; Bajaj, A. V.; Joshi, S. QSAR study on solubility of alkanes in water and their partition coefficients in different solvent systems using PI index. *Bioorganic & medicinal chemistry letters* **2003**, *13*, 419–422.
- (24) Sander, R. Henry’s law constants in NIST Chemistry WebBook. *NIST standard reference database* **2017**,
- (25) Mackay, D.; Shiu, W. Y. A critical review of Henry’s law constants for chemicals of environmental interest. *Journal of physical and chemical reference data* **1981**, *10*, 1175–1199.
- (26) Tsonopoulos, C. Thermodynamic analysis of the mutual solubilities of normal alkanes and water. *Fluid Phase Equilibria* **1999**, *156*, 21–33.
- (27) Sutton, C.; Calder, J. A. Solubility of higher-molecular-weight normal-paraffins in distilled water and sea water. *Environmental science & technology* **1974**, *8*, 654–657.
- (28) Franks, F. Solute–water interactions and the solubility behaviour of long-chain paraffin hydrocarbons. *Nature* **1966**, *210*, 87–88.
- (29) Tolls, J.; van Dijk, J.; Verbruggen, E. J.; Hermens, J. L.; Loeprecht, B.; Schüürmann, G. Aqueous solubility- molecular size relationships: A mechanistic case study using C10-to C19-alkanes. *The Journal of Physical Chemistry A* **2002**, *106*, 2760–2765.

- (30) McAuliffe, C. Solubility in water of normal c9 and c10, alkane hydrocarbons. *Science* **1969**, *163*, 478–479.
- (31) McAuliffe, C. Solubility in water of paraffin, cycloparaffin, olefin, acetylene, cycloolefin, and aromatic hydrocarbons¹. *The Journal of Physical Chemistry* **1966**, *70*, 1267–1275.
- (32) Cabani, S.; Gianni, P.; Mollica, V.; Lepori, L. Group contributions to the thermodynamic properties of non-ionic organic solutes in dilute aqueous solution. *Journal of Solution Chemistry* **1981**, *10*, 563–595.
- (33) Plyasunov, A. V.; Shock, E. L. Thermodynamic functions of hydration of hydrocarbons at 298.15 K and 0.1 MPa. *Geochimica et Cosmochimica Acta* **2000**, *64*, 439–468.
- (34) Plyasunov, A. V.; Shock, E. L. Group contribution values of the infinite dilution thermodynamic functions of hydration for aliphatic noncyclic hydrocarbons, alcohols, and ketones at 298.15 K and 0.1 MPa. *Journal of Chemical & Engineering Data* **2001**, *46*, 1016–1019.
- (35) Ferguson, A. L.; Debenedetti, P. G.; Panagiotopoulos, A. Z. Solubility and molecular conformations of n-alkane chains in water. *The Journal of Physical Chemistry B* **2009**, *113*, 6405–6414.
- (36) Maerzke, K. A.; Schultz, N. E.; Ross, R. B.; Siepmann, J. I. TraPPE-UA force field for acrylates and Monte Carlo simulations for their mixtures with alkanes and alcohols. *The Journal of Physical Chemistry B* **2009**, *113*, 6415–6425.
- (37) Berendsen, H. J.; Grigera, J.-R.; Straatsma, T. P. The missing term in effective pair potentials. *Journal of Physical Chemistry* **1987**, *91*, 6269–6271.
- (38) Kumar, S. K.; Szleifer, I.; Panagiotopoulos, A. Z. Determination of the chemical potentials of polymeric systems from Monte Carlo simulations. *Physical review letters* **1991**, *66*, 2935.

- (39) Xue, B.; Harwood, D. B.; Chen, J. L.; Siepmann, J. I. Monte Carlo Simulations of Fluid Phase Equilibria and Interfacial Properties for Water/Alkane Mixtures: An Assessment of Nonpolarizable Water Models and of Departures from the Lorentz–Berthelot Combining Rules. *The Journal of Physical Chemistry B* **2018**, *122*, 7617–7627.
- (40) Ashbaugh, H. S.; Collett, N. J.; Hatch, H. W.; Staton, J. A. Assessing the thermodynamic signatures of hydrophobic hydration for several common water models. *The Journal of chemical physics* **2010**, *132*.
- (41) Ashbaugh, H. S.; Liu, L.; Surampudi, L. N. Optimization of linear and branched alkane interactions with water to simulate hydrophobic hydration. *The Journal of chemical physics* **2011**, *135*.
- (42) Chen, B.; Siepmann, J. I. A novel Monte Carlo algorithm for simulating strongly associating fluids: Applications to water, hydrogen fluoride, and acetic acid. *The Journal of Physical Chemistry B* **2000**, *104*, 8725–8734.
- (43) Jorgensen, W. L.; Maxwell, D. S.; Tirado-Rives, J. Development and testing of the OPLS all-atom force field on conformational energetics and properties of organic liquids. *Journal of the American Chemical Society* **1996**, *118*, 11225–11236.
- (44) Singh, H.; Sharma, S. Hydration of linear alkanes is governed by the small length-scale hydrophobic effect. *Journal of Chemical Theory and Computation* **2022**, *18*, 3805–3813.
- (45) Wang, J.; Wolf, R. M.; Caldwell, J. W.; Kollman, P. A.; Case, D. A. Development and testing of a general amber force field. *Journal of Computational Chemistry* **2004**, *25*, 1157–1174.
- (46) Izadi, S.; Anandakrishnan, R.; Onufriev, A. V. Building water models: A different approach. *The Journal of Physical Chemistry Letters* **2014**, *5*, 3863–3871.

- (47) Izadi, S.; Onufriev, A. V. Accuracy limit of rigid 3-point water models. *The Journal of Chemical Physics* **2016**, *145*, 074501.
- (48) Chaplin, M. Water Models. https://water.lsbu.ac.uk/water/water_models.html, Accessed: April 11, 2025.
- (49) Alchemistry.org Community Alchemistry Wiki. https://alchemistry.org/wiki/Main_Page, 2025; Accessed: April 11, 2025.
- (50) Beutler, T. C.; Mark, A. E.; van Schaik, R. C.; Gerber, P. R.; van Gunsteren, W. F. Avoiding singularities and numerical instabilities in free energy calculations based on molecular simulations. *Chemical Physics Letters* **1994**, *222*, 529–539.
- (51) Zwanzig, R. W. High-temperature equation of state by a perturbation method. *The Journal of Chemical Physics* **1954**, *22*, 1420–1426.
- (52) Shirts, M. R.; Pande, V. S. Comparison of efficiency and bias of free energies computed by exponential averaging, the Bennett acceptance ratio, and thermodynamic integration. *The Journal of Chemical Physics* **2005**, *122*, 144107.
- (53) Siepmann, J. I. Transferable Potentials for Phase Equilibria (TraPPE) Force Field. <https://trappe.chem.umn.edu>, Accessed: April 11, 2025.
- (54) LAMMPS Developers LAMMPS - Large-scale Atomic/Molecular Massively Parallel Simulator. <https://www.lammps.org>, 2024; Accessed: January 2024, Version: 10 Mar 2021.
- (55) Martínez, L.; Andrade, R.; Birgin, E. G.; Martínez, J. M. PACKMOL: A package for building initial configurations for molecular dynamics simulations. *Journal of Computational Chemistry* **2009**, *30*, 2157–2164.
- (56) Gallicchio, E.; Kubo, M.; Levy, R. M. Enthalpy- entropy and cavity decomposition

of alkane hydration free energies: numerical results and implications for theories of hydrophobic solvation. *The Journal of Physical Chemistry B* **2000**, *104*, 6271–6285.

- (57) Ramezani, Y. LAMMPS Input Files for Hydration Free Energy Simulations. 2025; <http://doi.org/10.5281/zenodo.1234567>, Accessed: [insert date you accessed it, e.g., July 13, 2025].

Supporting Information: Hydration Free Energies of Linear Alkanes: Evaluating and Correcting Classical Force Field Predictions with Different Water Models

Yalda Ramezani and Sumit Sharma^{1*}

*Department of Chemical and Biomolecular Engineering, Ohio University, Athens, OH -
45701*

E-mail: sharmas@ohio.edu

Table 1: Details of the Alkane-Water Simulation System. Three system sizes are used depending on the alkane length. The simulation system volume fluctuates so as to maintain a constant pressure.

Alkane	box length [Å]	Number of Water Molecules
C_1-C_8	36	1500
C_9-C_{14}	46	3390
$C_{15}-C_{20}$	56	6440

Table 2 compares the ΔG_{hyd} estimated in this work using the TraPPE force field and the TIP4P/2005 and SPC/E water models with the previous estimates by Chen (2000),¹ Xue (2018),² and Ashbaugh (2011).³ Our estimates for TraPPE + TIP4P/2005 match well with those of Ashbaugh (2011) and Xue (2018) with the maximum deviation of 1.65 kJ/mol observed for C_9 with Xue (2018). The results from the OPLS + TIP4P are also within 0.7 kJ/mol of our estimates for TraPPE + TIP4P/2005. Our results using the SPC/E water

¹Corresponding author: Sumit Sharma

model show the largest deviation of 1.5 kJ/mol for C_8 when compared to Xue (2018). Overall, this shows that our estimates are in good agreement with the previous studies.

Table 2: Comparison of hydration free energy obtained in this work with previous studies. The estimated error in our calculation, determined from three independent simulations, is 0.05 kJ/mol up to C_6 , 0.1 kJ/mol up to C_{11} , and 0.4 kJ/mol for longer alkanes.

Alkane	This work		Chen (2000) ¹	Xue (2018) ²		Ashbaugh (2011) ³
	TraPPE+TIP4P/2005	TraPPE+SPC/E	OPLS+TIP4P	TraPPE+TIP4P/2005	TraPPE+SPC/E	TraPPE+TIP4P/2005
1	9.26	9.39	9.40			9.33
2	8.82	9.28	8.20			8.66
3	9.75	9.94	9.70			9.67
4	10.61	11.16	10.70			10.33
5	11.69	12.19		11.79	11.05	
6	12.62	13.11		12.99	12.12	
7	13.68	14.58		14.38	13.13	
8	14.64	15.69		15.91	14.19	
9	16.10	16.62		17.75	15.30	

Table 3: Hydration free energies (kJ/mol) of linear alkanes from methane (C_1) to eicosane (C_{20}) using different water models with alkane-water interaction parameters calculated using Lorentz-Berthelot mixing rules. The estimated error in our calculation, determined from three independent simulations, is 0.05 kJ/mol up to C_6 , 0.1 kJ/mol up to C_{11} , and 0.4 kJ/mol for longer alkanes.

Alkane	Experiments	Group Contribution	TIP4P/2005	OPC	SPC/E	OPC3	HH-alkane	Shifted HH-alkane
1	8.37		9.26	9.7249	9.3933	9.2343	8.6256	8.4752
2	7.66		8.82	8.7348	9.2782	8.8111	7.9453	7.9936
3	8.18		9.75	9.6725	9.9414	9.9027	8.6006	8.8800
4	8.70		10.61	10.589	11.162	11.192	9.0241	9.5404
5	9.76		11.69	11.671	12.188	12.129	10.011	10.095
6	10.40		12.62	12.329	13.105	13.387	10.833	11.118
7	10.96		13.68	13.589	14.578	14.642	11.258	11.886
8	12.10		14.64	14.422	15.691	15.681	11.837	12.996
9		12.58	16.10	15.170	16.617	16.889	12.831	13.926
10		13.32	16.92	16.089	18.078	18.186	13.598	14.759
11		14.06	17.94	17.068	19.472	19.351	14.465	15.701
12		14.80	18.70	17.916	20.151	20.580	15.395	17.107
13		15.54	19.85	19.245	21.628	21.608	16.245	17.112
14		16.28	20.44	20.164	22.948	23.066	16.673	18.275
15		17.02	21.69	21.732	24.350	24.134	17.405	19.433
16		17.76	23.03	22.113	25.149	25.677	18.171	20.750
17		18.50	24.57	24.001	26.585	27.081	18.852	21.188
18		19.24	25.03	24.606	27.642	27.725	20.033	22.039
19		19.98	26.97	25.912	29.246	28.745	21.548	23.097
20		20.72	28.03	27.201	30.486	30.973	21.693	23.796

Table 4: Hydration free energies (kJ/mol) of alkanes with different water models with updated alkane-water well-depth parameter (ϵ).

Alkane	TIP4P/2005	OPC	SPC/E	OPC3
1	8.8378	9.106	8.5273	8.8462
2	7.8727	7.9507	7.5677	7.6850
6	10.346	10.099	10.340	10.432
10	12.996	13.117	13.474	13.689
14	16.204	15.726	17.338	17.361
18	19.531	19.198	19.895	21.102
20	22.132	20.623	22.092	22.035

Table 5: Hydration free energies (kJ/mol) of alkanes computed using the General Amber Force Field and TIP4P/2005 and SPC/E water models.

Alkane	TIP4P/2005	SPC/E
1	9.696	9.802
2	9.5008	10.015
5	10.282	11.212
8	11.850	13.113
11	12.832	15.675
14	14.890	17.883
17	16.956	19.986

References

- (1) Chen, B.; Siepmann, J. I. A novel Monte Carlo algorithm for simulating strongly associating fluids: Applications to water, hydrogen fluoride, and acetic acid. *The Journal of Physical Chemistry B* **2000**, *104*, 8725–8734.
- (2) Xue, B.; Harwood, D. B.; Chen, J. L.; Siepmann, J. I. Monte Carlo Simulations of Fluid Phase Equilibria and Interfacial Properties for Water/Alkane Mixtures: An Assessment of Nonpolarizable Water Models and of Departures from the Lorentz–Berthelot Combining Rules. *The Journal of Physical Chemistry B* **2018**, *122*, 7617–7627.
- (3) Ashbaugh, H. S.; Liu, L.; Surampudi, L. N. Optimization of linear and branched alkane interactions with water to simulate hydrophobic hydration. *The Journal of chemical physics* **2011**, *135*.