

Forecasting the Observable Rates of Gravitationally Lensed Supernovae for the PASSAGES Dusty Starbursts

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ABSTRACT

More than 60 years have passed since the first formal suggestion to use strongly-lensed supernovae to measure the expansion rate of the Universe through time-delay cosmography. Yet, fewer than 10 such objects have ever been discovered. We consider the merits of a targeted strategy focused on lensed hyperluminous infrared galaxies—among the most rapidly star-forming galaxies known in the Universe. With star formation rates (SFRs) $\sim 200 - 6000 \text{ M}_{\odot} \text{ yr}^{-1}$, the ~ 30 objects in the Planck All-Sky Survey to Analyze Gravitationally-lensed Extreme Starbursts (PASSAGES) are excellent candidates for a case study, in particular, and have already led to the discovery of the multiply-imaged SN H0pe. Considering their lens model-corrected SFRs, we estimate their intrinsic supernova rates to be an extraordinary $1.8 - 65 \text{ yr}^{-1}$ (core-collapse) and $0.2 - 6.4 \text{ yr}^{-1}$ (Type Ia). Moreover, these massive starbursts typically have star-forming companions which are unaccounted for in this tally. We demonstrate a strong correlation between Einstein radius and typical time delays, with cluster lenses often exceeding several months (and therefore most favorable for high-precision H_0 inferences). A multi-visit monitoring campaign with a sensitive infrared telescope (namely, JWST) is necessary to mitigate dust attenuation. Still, a porous interstellar medium and clumpy star formation in these extreme galaxies might produce favorable conditions for detecting supernovae as transient point sources. Targeted campaigns of known lensed galaxies to discover new lensed supernovae can greatly complement wide-area cadenced surveys. Increasing the sample size helps to realize the potential of supernova time-delay cosmography to elucidate the Hubble tension through a single-step measurement, independent of other H_0 techniques.

Keywords: Hubble constant (758) — Starburst galaxies (1570) — Strong gravitational lensing (1643)
— Supernovae (1668)

1. INTRODUCTION

Gravitationally lensed supernovae (glSNe) are invaluable cosmological tools that are finally now being discovered and leveraged to make unique, one-step measurements of the Hubble constant, H_0 , describing the expansion rate of the Universe (S. H. Suyu et al. 2024). For multiply-imaged lensed objects, the arrival of the different images is staggered in time due to *i*) the difference in path lengths along the different null geodesics; and *ii*) the Shapiro effect (I. I. Shapiro 1964), by which the light rays experience disparate amounts of time dilation from the differing gravitational potential along their paths. The magnitude of this effect for galaxies at cosmological distances—typically of order hours to decades—is usually far too small to be detectable, given the timescales of Myr for galaxy-scale variations. However, with rapidly varying or transient signals, like from quasars or supernovae, it is possible to capture and measure these lensing-induced time delays through light curve monitoring. Through a technique now known as time-delay (TD) cosmography first introduced by S. Refsdal 1964 (see also reviews by R. D. Blandford & R. Narayan 1992; T. Treu & P. J. Marshall 2016; T. Treu et al. 2022; S. Birrer et al. 2024), these delays may be inverted to infer distances within the Hubble flow, and therefore H_0 . This owes to the dependence of the time delays on a ratio of 3 angular-diameter distances (from the observer to the lens, from the observer to the source, and from the lens to the source; P. Schneider 1985), which in turn is proportional to H_0^{-1} (with minimal dependence on other cosmological parameters).

The “Hubble tension” between calculations of the Hubble constant H_0 still endures, despite an extraordinary number of measurements that have been put forth in the last two decades (see recent review by L. Verde et al. 2024). The primary conflict arises from the smaller value of $H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Planck Collaboration et al. 2020) inferred from the cosmic microwave background (CMB) within the standard Λ CDM model (also S. Aiola et al. 2020; T. Louis et al. 2025), relative to the larger values found from the local Universe (e.g., $H_0 = 73.0 \pm 1.0 \text{ km s}^{-1} \text{ Mpc}^{-1}$ from SH0ES; A. G. Riess et al. 2022). The latter measurements are predominantly determined through calibration of a distance ladder on cosmological scales, making use of indicators such as Type Ia supernovae in combination with, e.g., *i*) Cepheid variable stars (e.g., A. G. Riess et al. 2022),

ii) the tip of the red giant branch (TRGB; e.g., W. L. Freedman et al. 2019; G. S. Anand et al. 2024), or *iii*) the J-Region Asymptotic Giant Branch (JAGB; e.g., A. J. Lee et al. 2021; W. L. Freedman et al. 2025). Given the manifold challenges in this calibration (E. Mörtzell et al. 2022a,b), there is a drastic need for independent and orthogonal measurements of H_0 that do not suffer from the same systematics.

One such example is the Megamaser Cosmology Project (M. J. Reid et al. 2009, 2013; D. W. Pesce et al. 2020), which enables a “single-rung” geometric distance inference through high-precision mapping of circumnuclear H_2O masers originating from accretion disks around active galactic nuclei (AGN) in low- z galaxies. Another, of course, is TD cosmography, which is capable of yielding a single-rung measurement well into the Hubble flow without hinging on the possible pitfalls from the usual distance ladder methods¹⁴.

TD cosmography has perhaps matured more quickly for lensed quasars, which are variable but offer the benefit of persistence that supernovae lack (K. C. Wong et al. 2020; S. Birrer et al. 2020, 2024). Over 300 lensed quasars have been identified, most with image separations of only a few arcseconds and with time delays typically less than one year, although some (e.g., J. Fohlmeister et al. 2007, 2008; H. Dahle et al. 2015; J. A. Muñoz et al. 2022; K. Napier et al. 2023) have measured time delays using wide-separation cluster-lensed quasars (which have some advantages over galaxy-scale lenses and their systematic uncertainties; C. S. Kochanek 2020). However, inferring time delays from quasars requires long-term monitoring (of order 10 years) for accurate measurements (F. Courbin et al. 2005; V. Bonvin et al. 2017), and can be plagued by microlensing (M. J. Irwin et al. 1989; H. J. Witt et al. 1995; P. L. Schechter et al. 2003; G. Varnardos et al. 2024), degeneracies and systematics in lens models (C. R. Keeton et al. 2000; L. V. E. Koopmans et al. 2003), and the well-known mass-sheet and mass-slope degeneracies (E. E. Falco et al. 1985; M. V. Gorenstein et al. 1988; J. Wambsganss & B. Paczynski 1994; C. S.

¹⁴ To be clear, this technique does not rely on the nature of SNe Ia as “standardizable candles” like other late-Universe efforts (although this property may assist in more objectively assessing the accuracy of various lens models; M. Pascale et al. 2025). Supernovae are simply a useful transient source by which time delays may be measured, revealing the underlying cosmology.

Kochanek 2002; P. Schneider & D. Sluse 2013). While some of these challenges also affect TD cosmography with supernovae, this approach has some distinct advantages. Their rapid and more predictable variation in brightness means that time delays can be measured with much shorter monitoring campaigns—even as little as a few hours of spectroscopy (W. Chen et al. 2024)—and with a level of precision and accuracy that is actually more affected by photometric uncertainties than by microlensing (e.g. J. D. R. Pierel & S. Rodney 2019; S. Huber et al. 2022; J. D. R. Pierel et al. 2024a).

Perhaps the most important systematic plaguing the time-delay cosmography approach for supernovae at present is scarcity. Supernovae are inherently rare events— $\lesssim 1\%$ of all stars will end their lifetimes in core-collapse supernovas (CCSNe). As their duration above a survey’s sensitivity limits is short-lived, especially at $z > 1$, their discovery essentially requires a not insignificant amount of luck. Strong gravitational lensing in the regime of producing multiple images is similarly quite rare (T. Treu 2010). While the lensing optical depth (probability of being lensed above a certain magnification threshold or lensed into more than one image) increases monotonically with source-plane redshift, this largely asymptotes above $z \gtrsim 2$ (e.g., S. Hilbert et al. 2007, 2008; A. Robertson et al. 2020). As a result, barely more than a handful of other multiply-imaged lensed SNe have been discovered in the last decade since SN Refsdal was first identified behind the MACS J1149.6+2223 galaxy cluster (P. L. Kelly et al. 2015, 2016; C. Grillo et al. 2018; H_0 measurements in P. L. Kelly et al. 2023a; C. Grillo et al. 2024). Since then, three other gLSNe suitable for TD cosmography have been discovered: SN H0pe behind the PLCK G165.7+67.0 cluster (B. L. Frye et al. 2023, 2024), and the pair of SN Requiem (S. A. Rodney et al. 2021) and SN Encore (J. D. R. Pierel et al. 2024b), both within the same massive host galaxy lensed by MACS J0138.0-2155 and separated by 2.5 years in the galaxy’s rest frame. The analysis of SN H0pe, the first confirmed gLSN Ia used for TD cosmography, recently produced a new H_0 measurement at $\sim 10\%$ precision (M. Pascale et al. 2025). This work also introduced a new weighting scheme for the seven independently-constructed lens models according to their ability to accurately predict observables like magnifications, made possible by H0pe’s nature as a standardizable candle. The first H_0 result from SN Encore is imminent (S. Ertl et al. 2025; S. Suyu et al., in prep.; J. D. R. Pierel et al., in prep.), and now there is also hope for a precise measurement from SN Requiem’s return a decade later in 2026-2027 (HST program GO-18069).

Upcoming wide-area surveys like the Vera C. Rubin Observatory’s Legacy Survey of Space and Time (LSST; LSST Science Collaboration et al. 2009) promise to reveal $\sim 50 - 100$ gLSNe yr^{-1} (N. Arendse et al. 2024; S. Bag et al. 2024; A. Melo et al. 2025; A. Sainz de Murieta et al. 2024), but not all of these will be discovered sufficiently early to follow up with light curve monitoring for the purposes of TD cosmography. Also, many of the gLSNe behind galaxy-scale deflectors will have time delays too short to yield meaningful precision on H_0 , as in the case of iPTF16geu ($z = 0.409$; A. Goobar et al. 2017). Moreover, in the pessimistic scenario, currently active facilities like the Zwicky Transient Facility (ZTF; E. Bellm 2014) were expected to yield at least one gLSN per year, but only one was identified in four years (SN Zwicky at $z = 0.354$; A. Goobar et al. 2023; J. D. R. Pierel et al. 2023), with few other compelling candidates (M. R. Magee et al. 2023; A. Sagués Carracedo et al. 2024; see also P. Craig et al. 2024). Still, the next decade is likely to see TD cosmography with gLSNe mature more fully and reach a competitive precision on H_0 , closer to 1% than 10% (T. Treu et al. 2022).

What, then, is the best strategy at present for discovering “live” gLSNe¹⁵? One answer might come from remarking that some of the recent discoveries have been identified behind well-studied lensing clusters. These include two of the famous Hubble Frontier Fields: SN Refsdal behind MACS J1149.6+2223 (P. L. Kelly et al. 2015) and a $z \approx 3$ CCSN behind Abell 370 (W. Chen et al. 2022). There is undoubtedly an observational bias here, given the attention these fields receive, resulting in a more well-sampled cadence, and the presence of numerous lens models to identify multiple imaging (M. Bronikowski et al. 2025). Yet, these massive lensing clusters also provide sizable magnification for a large number of background sources (e.g., A. Gal-Yam et al. 2002; V. Stanishev et al. 2009; T. Petrushevska et al. 2016, 2018a,b; T. Petrushevska 2020). However, SN H0pe, SN Requiem, and SN Encore were all identified within high-mass host galaxies lensed by less massive, previously lesser-known clusters. These discoveries were facilitated not necessarily by the extraordinary nature of the foreground, but more so of the background lensed host galaxies.

A targeted search for gLSNe in known lensed galaxies that are very massive or have a high SFR (or both) is

¹⁵ Here, “live” gLSNe draws a distinction from those discovered after the supernova has faded in all images, only apparent through its disappearance in a second epoch of observation, and therefore not suitable for monitoring to infer H_0 .

not an entirely novel idea. Y. Shu et al. (2018) estimated that monitoring a sample of > 100 galaxy-scale lensed star-forming galaxies would yield rates of ~ 3 combined CCSN and SN Ia events per year (Y. Shu et al. 2021), reaching a greater efficiency than a blind search. A targeted strategy also provides greater confidence that any discovered SNe are in fact lensed (see also B. W. Holwerda et al. 2021). Here, we modify the approach to encompass a much smaller sample, but with commensurately larger rates of star formation. There is some difficulty in identifying sufficient numbers of starburst galaxies (with high intrinsic rates of supernovae) that are lensed into multiple images. One possible approach is to monitor samples of known lensed dusty star-forming galaxies (DSFGs), also referred to as submillimeter galaxies (SMGs) which now number in the hundreds (M. Giuliotti et al. 2024), as these objects are inferred to form stars at prodigious rates of $300 - 1000 M_{\odot} \text{ yr}^{-1}$ (or even greater). The prevailing selection method for this population is unique, relying essentially on submillimeter flux alone (A. W. Blain 1996; F. Perrotta et al. 2002; M. Negrello et al. 2010, 2017), as opposed to methods that identify distorted lensing morphologies or peaks in foreground mass density or Sunyaev-Zel’dovich effect signal.

As an application of this tactic, we examine in particular the set of lensed DSFGs identified from *Planck*, which is perhaps most well suited for this experiment due to its all-sky coverage. For now, we consider the ~ 30 members of the *Planck* All-Sky Survey to Analyze Gravitationally-lensed Extreme Starbursts (PASSAGES; K. C. Harrington et al. 2016; D. A. Berman et al. 2022; P. S. Kamienieski et al. 2024a), some of which were also identified independently through *Herschel* follow-up (R. Cañameras et al. 2015; Planck Collaboration et al. 2015). Of these, 21 objects (summarized in Table 1) have the information necessary to compute expected gLSN rates (§2.4 and 3.1). P. S. Kamienieski et al. (2024a) determined that the median de-lensed (i.e. intrinsic) infrared luminosity for PASSAGES exceeded $10^{13} L_{\odot}$, qualifying them as hyperluminous infrared galaxies (HyLIRGs). Nonetheless, the dust geometry of such extreme HyLIRGs remains quite uncertain at high- z . Any supernovae are likely to be attenuated by dust in even the best-case scenario, so near-IR sensitivity is paramount.

HyLIRGs such as these are often signposts of significant over-dense regions (e.g., N. Foo et al. 2025). While we consider primarily the contribution to the supernova rate from the primary starburst galaxies, there is a high likelihood of other star-forming objects at the same red-

shift that might also fall into the strongly lensed portion of the source plane, further boosting the chances of identifying lensed transients in these fields. This is also borne out in part with the discovery of SN H0pe behind the lensing cluster G165.7+67.0, which was itself identified through its amplification of one of the PASSAGES DSFGs. Initial JWST/NIRCam imaging of the field through the Prime Extragalactic Areas for Reionization and Lensing Science program (R. A. Windhorst et al. 2023) revealed the Type Ia supernova not within the giant arc of lensed DSFGs, but in a highly-magnified arc nearby in projection. Both this host galaxy and the DSFGs were found to be members of respective photometric-redshift overdensities at $z = 1.78$ and $z = 2.24$ (B. L. Frye et al. 2024).

This work is organized as follows: in Section 2, we detail our novel approach to deriving forecasts for the intrinsic and observer-frame rates of supernovae in HyLIRGs, using the PASSAGES fields as an example. In Section 3, we discuss our inference of star formation rates (both obscured and unobscured modes), lensing multiplicities, and the core-collapse and degenerate white dwarf supernova rates that result from these inferences. We also examine the expected typical time delays and draw a connection to the angular separation between images. In Section 4, we summarize our findings and reflect on the feasibility of our proposed approach in making a meaningful contribution to the rather saturated industry of deriving H_0 constraints. Throughout, we adopt a fiducial Λ CDM concordance cosmology of $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. OBSERVATIONS & METHODS

2.1. Case study sample selection: PASSAGES

In this work, we aim to forecast the expected rates of supernovae from strongly-lensed DSFGs at $z > 1$. Lensed DSFGs are efficiently selected through their submillimeter flux owing to a steep drop-off in number counts (A. W. Blain 1996), such that an extragalactic source brighter than 100 mJy at $500 \mu\text{m}$ is $\gtrsim 30$ times more likely to be lensed than unlensed (M. Negrello et al. 2017). However, they are still rare objects, with a modeled all-sky number density of $0.09 \pm 0.05 \text{ deg}^{-2}$ for $S_{500\mu\text{m}} > 80 \text{ mJy}$, while observations suggest up to $\sim 0.3 \text{ deg}^{-2}$ (C. Sedgwick et al. 2025, and references therein including M. Negrello et al. 2010; R. S. Bussmann et al. 2013; J. L. Wardlow et al. 2013; M. Negrello et al. 2014, 2017; T. J. L. C. Bakx et al. 2018; S. A. Urquhart et al. 2022; E. Borsato et al. 2024). This model predicts 3600 ± 1800 such sources to exist in the entire sky (increasing by a factor of ~ 40 if the threshold is

lowered by a factor of 10; T. J. L. C. Bakx et al. 2024a; C. Sedgwick et al. 2025), but so far only a few hundred such objects have been uncovered (e.g. M. Giuliotti et al. 2024). *Euclid*’s Wide Survey (Euclid Collaboration et al. 2022) is expected to be sensitive to several thousand.

For now, while *Planck*’s surveys reach shallower depths than *Herschel*, its wide-area coverage has been an asset for identifying the very brightest lensed DSFGs in the sky (T. Trombetti et al. 2021). As discussed by P. S. Kamieneski et al. (2024a), there is a complex balance between their intrinsic luminosities and their magnifications: HyLIRGs tend to have larger sizes to match their higher luminosities (in line with the Eddington limit; P. S. Kamieneski 2024), while size bias leads to more strongly-magnified objects correlating with more compact sizes (Y. D. Hezaveh et al. 2012). Together, this means that candidates with apparent luminosities $\mu_{\text{IR LIR}} \gtrsim 10^{14} L_{\odot}$ tend to still have intrinsic $L_{\text{IR}} \gtrsim 10^{12.5} L_{\odot}$. For this reason, the greater submillimeter fluxes of *Planck*-identified lensed DSFGs are not simply the result of higher magnifications alone. They are thus among the best candidates for high rates of gISNe given their high SFRs. Moreover, their lower median redshift than lensed DSFGs identified in the millimeter regime (e.g., with the South Pole Telescope; A. Weiss et al. 2013) lends well to greater ease in detecting gISNe in the observed-frame near-IR.

2.2. Determining the expected value of image multiplicity

A galaxy that crosses the caustic network will have different parts of the source plane lensed into varying numbers of multiple images. In the canonical lensing example of a singular isothermal ellipsoid, an astroid tangential caustic encloses a region with an image multiplicity of 4 (excluding demagnified images), whereas the region between the tangential caustic and the elliptical radial caustic is lensed into 2 images, and structures exterior to the radial caustic are weakly lensed into only a single image. For cluster-scale lenses, which have larger source-plane areas inside the caustics, it is more likely for most of a galaxy’s light to be contained within a region with constant image multiplicity. On the other hand, galaxy-scale lenses have much tighter caustic loci, so galaxies can easily cross caustics and have two (or even more) different image multiplicities of the source.

The lensing multiplicity of a galaxy has a direct bearing on the average rate of SNe that can be observed on Earth. To account for this, we introduce the concept of *effective multiplicity*, $\mathcal{N}_{\text{eff}}$, which is the average mul-

tiplicity weighted by the distribution of star formation. We define it as

$$\mathcal{N}_{\text{eff}} \equiv \sum_n \left[n \cdot \frac{\text{SFR}_n}{\text{SFR}} \right] \quad (1)$$

for the different multiplicities n , where SFR_n is the total star formation rate within the region of multiplicity n . This calculation is illustrated for a singular isothermal ellipsoid lens (with a large axis ratio) in a cartoon in Fig. 1. $\mathcal{N}_{\text{eff}}$ can also be functionally expressed as a pixel-based summation:

$$\mathcal{N}_{\text{eff}} \equiv \frac{\sum_{i,j} N_{i,j} \text{SFR}_{i,j}}{\sum_{i,j} \text{SFR}_{i,j}} \quad (2)$$

where $\text{SFR}_{i,j}$ and $N_{i,j}$ are the star formation rate and multiplicity, respectively, at pixel (i, j) .

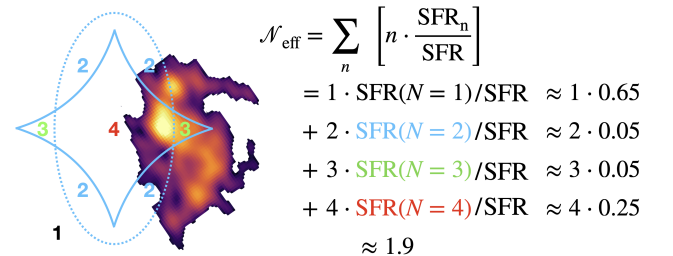


Figure 1. Cartoon schematic demonstrating the calculation of effective multiplicity $\mathcal{N}_{\text{eff}}$ per Equation 1, using an ALMA 870 μm image of the unlensed DSFG ALESS 112.1 as an example (J. A. Hodge et al. 2019). Mock caustic curves from an imaginary lensing galaxy are overlaid (radial=dashed, tangential=solid). Put simply, $\mathcal{N}_{\text{eff}}$ is the weighted average of multiplicities ($n = 1, 2, 3, \dots$), where the weights are the respective portions of the total SFR.

2.3. ALMA 1mm continuum and VLA 6 GHz

To infer a map of SFR to compute $\mathcal{N}_{\text{eff}}$ with the information available for the majority of PASSAGES, we rely on the 1mm dust continuum observed with the Atacama Large Millimeter/submillimeter Array (ALMA), by which we apportion the total IR SED-derived SFR (primarily from K. C. Harrington et al. 2016; D. A. Berman et al. 2022). For northern-declination sources not covered in these observations, we instead use 6 GHz (5 cm) continuum imaging from the Karl G. Jansky Very Large Array in A-configuration, with angular resolutions relatively close to the ALMA images. The 6 GHz images are largely correlated with the dust continuum through the radio-FIR correlation (e.g., J. J. Condon 1992). These observations are described in detail in Sections 2.4 and 2.5 of P. S. Kamieneski et al. (2024a), with images shown in their Figure 2.

We use these observations to map the source-plane spatial distribution of SFR_{IR} (as inferred from unresolved far-IR photometry, the source of which is specified for each target in Table 1). Since the star formation is likely dominated by the obscured mode probed by SFR_{IR} , the distribution $\Sigma_{\text{SFR}_{\text{IR}}}$ is our best estimate of the 2d probability density function of core-collapse supernovae (e.g., M. Miluzio et al. 2013). While slightly less direct, this is also likely to closely match the spatial distribution of Type Ia supernovae, as well (especially if one assumes that Σ_{SFR} correlates with the distribution of stellar mass, Σ_* ; e.g., W. M. Baker et al. 2022). Of course, the *observed* distribution of supernovae is more complex, and depends on dust geometry, but for the purpose of computing $\mathcal{N}_{\text{eff}}$, $\Sigma_{\text{SFR}_{\text{IR}}}$ should suffice. Nonetheless, given the highly stochastic nature of supernovae, even for galaxies with very high SFRs, and imperfections in the lens models, we adopt a conservative fractional uncertainty¹⁶ of 20% on $\mathcal{N}_{\text{eff}}$. The achieved resolutions for the ALMA and VLA observations ranged from $\theta \approx 0.4 - 0.8''$ and $\theta \approx 0.3 - 0.7''$, respectively. While higher-resolution observations (e.g., spatially-resolved SED fitting with JWST) would improve the fidelity of $\mathcal{N}_{\text{eff}}$, the location of the caustic network from lens models and systematics of SED-fitting dominate the uncertainty at present.

There is some concern that heavily dust-obscured active galactic nuclei (AGN) might contribute in the radio (J. L. Donley et al. 2005; A. Del Moro et al. 2013; I. Delvecchio et al. 2017), thus biasing the calculation of $\mathcal{N}_{\text{eff}}$. However, P. S. Kamieneski et al. (2024a) found that the PASSAGES DSFGs did not have obvious evidence of radio-loud AGN manifesting as an excess in spatially-integrated radio continuum relative to FIR, suggesting that this bias is not likely to have a sizable effect.

2.4. Estimating the obscured & unobscured SFR

2.4.1. The situation at low- z vs. $z > 2$

CCSNe have been discovered successfully in low- z luminous infrared galaxies (LIRGs) in the near-IR within

projected radii < 1 kpc (F. Mannucci et al. 2003; S. Mattila et al. 2007; E. Kankare et al. 2008, 2012; M. Miluzio et al. 2013; E. C. Kool et al. 2018; J. E. Jencson et al. 2019; O. D. Fox et al. 2021; E. Kankare et al. 2021; M. Pérez-Torres et al. 2021). These include some radio supernovae and supernova remnants found through very long baseline interferometry (e.g., I. Martí-Vidal et al. 2007; M. A. Pérez-Torres et al. 2009; M. Bondi et al. 2012; E. Varenus et al. 2019). On the other hand, some campaigns have yielded zero, or at least drastically fewer than expected, detected events for starbursts and ultra-luminous infrared galaxies (ULIRGs), including G. Cresci et al. (2007) with *HST*/NICMOS, or P. Väisänen et al. (2008) with adaptive optics-assisted VLT imaging. I. Mäntynen et al. (2025) recently found that $\approx 90\%$ of CCSNe in local LIRGs might be missed if attenuations only up to $A_V < 3$ mag are detectable. Even if hypothetically sensitive to extremely high values of $A_V \gtrsim 40$, the authors obtain an undetectable fraction $\gtrsim 50\%$ owing to the concentrated distribution of dust and star formation in local LIRGs. O. D. Fox et al. (2021) emphasized the importance of a stable, symmetric, high-resolution PSF in the near-IR (as achieved with space-based facilities) in order to combat this high concentration.

This might paint a dire picture for executing successful campaigns at high- z , although clever workarounds are possible. For example, H. Yan et al. (2018) demonstrated that the presence of SNe may be revealed through variability in the integrated near-IR light of a galaxy (at the time with *Spitzer*). However, there also appear to be key distinctions between the typical structures of high- z HyLIRGs and the LIRGs/ULIRGs in the low- z Universe. The typical star-dust geometry of DSFGs and starburst galaxies remains a matter of ongoing research, which of course has implications for the detectability of supernovae. In particular, the presence of unobscured UV-bright sightlines in DSFGs may be responsible for bluer UV slopes β_{UV} , resulting in the observed deviation from the IRX- β relation (G. R. Meurer et al. 1999) where $\text{IRX} \equiv L_{\text{IR}}/L_{\text{UV}}$ is the IR excess (e.g., L. Cortese et al. 2006; M. Boquien et al. 2009; C. M. Casey et al. 2014b; A. L. Faisst et al. 2017; M. Safarzadeh et al. 2017; D. Narayanan et al. 2018; L. Liang et al. 2021). In essence, the exceptional rate of supernovae occurring per year in each of the PASSAGES galaxies (Table 1) is likely to result in a very porous ISM, especially considering the groundwork laid by pre-supernova feedback (W. E. Lucas et al. 2020; M. Chevance et al. 2022; E. J. Watkins et al. 2023). Supernovae are likely to occur within an inhomogeneous medium, and further contribute to this through compression of swept-up shells and rarefied bubbles (e.g., C.

¹⁶ This uncertainty can be very roughly approximated as the fraction of a galaxy’s star-forming area that is within the 1σ uncertainty on the caustic’s location, multiplied by the relative change in multiplicity on either side of the caustic. In a canonical case of a galaxy straddling a caustic curve separating regions of double- vs. quad-imaging, this would be $\Delta N = 2$ from the $N = 2$ to $N = 4$ region, with average $N \sim 3$. For a source-plane positional uncertainty of $\sim 0.1''$ and a typical source-plane size of $\sim 0.4''$ for PASSAGES (P. S. Kamieneski et al. 2024a), the typical uncertainty thus becomes $\sigma_{\mathcal{N}_{\text{eff}}}/\mathcal{N}_{\text{eff}} \sim (0.1/0.4) \cdot (4 - 2)/3 \sim 20\%$.

Clarke & M. S. Oey 2002; C.-G. Kim & E. C. Ostriker 2015. This ISM structure, in turn, favors the ability to observe supernovae, even in dusty environments.

Local ULIRGs often host extremely concentrated starburst regions (although as K. B. W. McQuinn et al. 2012 point out, this may be partially a selection bias). This high concentration reaches an extreme with compact obscured nuclei, or CONs (which have sizes of 10 – 100 pc and very high attenuations of $A_V \gtrsim 10$; K. Sakamoto et al. 2013; S. Aalto et al. 2015; N. Falstad et al. 2021). At Cosmic Noon ($z \sim 1 - 3$), their more luminous counterparts sustain high rates of star formation over the scale of several kpc (W. Rujopakarn et al. 2011; J. A. Hodge et al. 2016, 2019; K. C. Harrington et al. 2021; P. S. Kamienieski et al. 2024a,b; I. Mitsuhashi et al. 2024; M. Polletta et al. 2024), often in clumps resulting from gravitational instabilities in gas-rich disks (A. Immeli et al. 2004; K. Tadaki et al. 2018; A. L. Faisst et al. 2025; S. Fujimoto et al. 2024; D. Liu et al. 2024; B. S. Kalita et al. 2025) that are continually replenished through accretion (F. Bournaud et al. 2007; A. Dekel et al. 2009).

Also, the high rates of star formation likely lend well to an increased rate of star cluster formation, and thus a better sampling of the high-mass end of the cluster mass function. For example, super star clusters (SSCs) are preferentially found in intense starburst regions, as exemplified by M82 and the Antennae Galaxies (e.g., L. J. Smith & J. S. Gallagher 2001; S. Mengel et al. 2002; R. de Grijs et al. 2003; B. C. Whitmore et al. 2010; S. T. Linden et al. 2017; K. L. Emig et al. 2020; R. C. Levy et al. 2024). If much of the star formation of DSFGs is concentrated in SSCs, which are progenitors of massive globular clusters, then their strong stellar feedback may contribute to clearing sightlines that both allows for Lyman continuum (LyC) leakage (e.g., A. Bik et al. 2018; M. Pascale et al. 2023; Z. Ji et al. 2025) and the escape of less-attenuated optical light from SNe (e.g., E. Leitet et al. 2013; N. Roy et al. 2024).

2.4.2. Adopting a fraction of unobscured SFR

$H\alpha$ SFRs are typically significantly less than those derived from the infrared. This discrepancy is primarily resolved after applying a Balmer decrement extinction correction to the $H\alpha$ -derived value (L. J. Kewley et al. 2002; T. Takata et al. 2006; H. Domínguez Sánchez et al. 2012; N. Timmons et al. 2015; A. Puglisi et al. 2016; D. Liu et al. 2024), although not in all cases (C.-C. Chen et al. 2020). For the D. Calzetti et al. (2000) attenuation law, $SFR_{H\alpha}$ is corrected as

$$SFR_{H\alpha, \text{corr}} = SFR_{H\alpha} \cdot 10^{0.4 \cdot E(B-V)_{\text{neb}} \cdot k'(\text{H}\alpha)} \quad (3)$$

where $k'(0.656\mu\text{m}) \approx 3.325$ and $E(B-V)_{\text{neb}}$ is the color excess inferred from emission lines,

$$E(B-V)_{\text{neb}} \approx 1.97 \cdot \log_{10} \left[\frac{L_{H\alpha}/L_{H\beta}}{2.86} \right] \quad (4)$$

for case B recombination (D. E. Osterbrock & G. J. Ferland 2006). Inherently, the strong attenuation of DSFGs has made it difficult to recover multiple Balmer lines. In a composite spectrum of 31 DSFGs in the COSMOS field, C. M. Casey et al. (2017) found a median Balmer decrement of 21.0 ± 2.4 , yielding $E(B-V) = 1.7 \pm 0.1$ or $A_V = 6.9 \pm 1.4$ (using $R_V = 4.05 \pm 0.80$). This is higher than observed even for local ULIRGs on global scales (e.g., V. Wild et al. 2011). More recently, in a sample of typical DSFGs at $z \sim 2 - 3$, O. R. Cooper et al. (2025) found consistency with the shape of the D. Calzetti et al. (2000) attenuation curve, and $A_V \sim 3 - 4$, through combination of Balmer and Paschen lines obtained with JWST/NIRSpec.

As some star formation is likely to be hosted in regions with dust obscuration strong enough such that no $H\alpha$ emission would be detectable, these Balmer decrements are biased low (A. Puglisi et al. 2017). The extinction-corrected $SFR_{H\alpha}$ estimates are likely to give a more realistic assessment of the observable rates of supernovae, however. Therefore, in our analysis, we introduce an unobscured fraction $f_{\text{unobsc}} \equiv SFR_{\text{unobsc}}/SFR_{\text{IR}} (\sim SFR_{H\alpha, \text{corr}}/SFR_{\text{IR}})$. For example, V. Olivares et al. (2016) found this fraction to be $< 30\%$ in $z \sim 2$ SMGs (an upper limit since their $H\alpha$ SFRs are not corrected for extinction). In other words, the discrepancy between the extinction-corrected $SFR_{H\alpha, \text{corr}}$ and SFR_{IR} is a quantification of how much star formation is hosted in regions of extreme attenuation (from which neither $H\beta$ nor $H\alpha$ may be detected).

For the PASSAGES sample itself, two members already have measurements of the Balmer decrement. For the pair of DSFGs PJ1127+42 at $z = 2.24$ (comprising Arcs 1abc, 3abc, 4abc, and 6abc lensed by the G165.7+67.0 cluster), B. L. Frye et al. (2024) found a value of $E(B-V) = 0.85 \pm 0.25$ through NIRSpec observations (corresponding to a Balmer decrement of 7.7 ± 2.3 and $A_V = 3.4 \pm 1.2$). This yields a correction of $\log_{10}(SFR_{H\alpha}/SFR_{H\alpha, \text{corr}}) = -1.1 \pm 0.3$, such that the demagnified $SFR_{H\alpha, \text{corr}} \approx 100^{+200}_{-70} M_{\odot} \text{ yr}^{-1}$ for Arc 1 only. Given that $SFR_{\text{IR}} = 320 \pm 70 M_{\odot} \text{ yr}^{-1}$ for the same object (P. S. Kamienieski et al. 2024b), this gives $f_{\text{unobsc}} \approx 31\%$. We adopt this fraction for the entire arc complex (Arcs 1, 3, 4, and 6, per notation from B. L. Frye et al. 2019), which all lies at $z \approx 2.24$ (R. Cañameras et al. 2018; P. S. Kamienieski

et al. 2024b). Similarly, for PJ0116-24 ($z = 2.13$), D. Liu et al. (2024) derived a color excess through Balmer decrement of $E(B-V) = 0.95 \pm 0.13$ with VLT/ERIS observations (Balmer decrement 8.7 ± 1.3 ; $A_V = 3.9 \pm 0.9$), suggesting $\log_{10}(\text{SFR}_{\text{H}\alpha}/\text{SFR}_{\text{H}\alpha,\text{corr}}) = -1.3 \pm 0.2$ and $\text{SFR}_{\text{H}\alpha,\text{corr}} = 470 \pm 60 M_{\odot} \text{ yr}^{-1}$ and $f_{\text{unobsc}} \approx 32\%$. In this work, for objects without these Balmer decrement measurements at present, we adopt a range of $f_{\text{unobsc}} = 20 \pm 10\%$ in Table 1 (see also, e.g., A. M. Swinbank et al. 2004; C.-C. Chen et al. 2020; C. Cheng et al. 2020).

This might at first seem to run counter to the results of K. E. Whitaker et al. (2017) that $f_{\text{obsc}} \equiv \text{SFR}_{\text{IR}}/\text{SFR}_{\text{UV+IR}}$ increases continually for higher SFRs and stellar masses (exceeding 90% for massive galaxies $\log(M/M_{\odot}) > 10.5$)¹⁷. Higher dust obscuration may be due to elevated surface densities of both star formation and gas (which are themselves correlated; M. Schmidt 1959; J. Kennicutt 1998). However, Σ_{SFR} does not seem to increase strongly with L_{FIR} . The size-luminosity relation found by S. Fujimoto et al. (2017) for $11 \lesssim \log(L_{\text{FIR}}/L_{\odot}) \lesssim 13$, $R_e \propto L_{\text{FIR}}^{0.28}$, implies a weak dependence of $\Sigma_{\text{SFR}} \propto \Sigma_{\text{FIR}} \propto L_{\text{FIR}}^{0.44}$. Empirically, HyLIRGs appear to remain at or below $\Sigma_{\text{SFR}} \approx 100 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$, with a similar distribution as ULIRGs with luminosities a decade lower (e.g., J. A. Hodge et al. 2019; T. J. L. C. Bakx et al. 2024b; P. S. Kamieneski et al. 2024a), suggesting that Σ_{SFR} may even saturate. If this property plays an important role in the K. E. Whitaker et al. (2017) relation, then the obscured fraction may saturate, as well.

Drawing again a parallel to the escape of Lyman continuum, this fraction of 20% has some precedent. For star-forming galaxies (SFGs) in UVCANDELS ($2.5 < z < 3.0$), X. Wang et al. (2025) reported an upper limit in the absolute Lyman continuum escape fraction of $f_{\text{esc}} \lesssim 26\%$. B. M. Smith et al. (2018) found that the average absolute f_{esc} for massive SFGs and weak AGN at $z \sim 2.4$ was $\sim 22^{+44}_{-22}\%$ (see also B. M. Smith et al. 2020 and B. M. Smith et al. 2024, which found $f_{\text{esc}} \sim 18\%$ for weak AGN in UVCANDELS). If stellar and AGN feedback in galaxies at similar redshifts with comparable (or even much lower) SFRs can clear the way for this level of escape of Lyman continuum—which is much more affected by dust than the light from SNe—then it is likely

not unreasonable to expect an unobscured fraction of $\sim 20\%$.

While clearly only a fraction of the star formation is visible in the unobscured mode for these objects, we emphasize that their total SFRs are large enough that the absolute unobscured star formation can still be quite substantial. Moreover, these large color excesses $E(B-V)$ primarily quantify the dust attenuation within the more obscured star-forming regions (e.g., V. Wild et al. 2011; S. H. Price et al. 2014; C.-C. Chen et al. 2020), which D. Calzetti (1997) found differed as $E(B-V)_{\text{stellar}} = 0.44 E(B-V)_{\text{nebular}}$. Deviation from this towards greater color excess for the nebular component appears to correlate with specific SFR ($\text{sSFR} \equiv \text{SFR}/M_{\star}$), as a greater share of star formation occurs in the obscured mode (N. A. Reddy et al. 2015), but it also is likely to vary spatially within individual galaxies (e.g., C. Robertson et al. 2024). It is probably not reasonable to expect that DSFGs will have uniformly large dust attenuation of $A_V \sim 4 - 7$, but this remains to be tested more rigorously in larger samples. It is also worth noting that multi-band JWST (or even HST) imaging enables robust spatially-resolved SED fitting for a wide range of redshifts (e.g., Abdurro'uf et al. 2023; C. Giménez-Arteaga et al. 2023; P. S. Kamieneski et al. 2024b; Z. Liu et al. 2024; M. Polletta et al. 2024; H. B. Akins et al. 2025; T. Harvey et al. 2025), such that the distribution of star formation and dust attenuation can be characterized at sub-kpc scales. This exercise is crucial to gain an understanding of where supernovae might be attenuated beyond detection limits, and even to better model the light curve of any SNe that are detected. This can also help account for any contribution to L_{IR} from dust-obscured AGN in PASSAGES galaxies; K. C. Harrington et al. (2016) and D. A. Berman et al. (2022) use mid- and far-IR photometry to show that they are star-formation-dominated, but not incontrovertibly.

3. RESULTS

3.1. Computing expected intrinsic and observer-frame rates of CCSNe

As the progenitors of core-collapse supernovae are massive stars, the core-collapse rate is linearly related to the rate of star formation,

$$R_{\text{CC}} = k_{\text{CC}} \cdot \text{SFR} \quad (5)$$

(e.g., P. Madau et al. 1998). The factor k_{CC} is determined from the initial mass function (IMF), $\phi(M)$, integrated over the mass range of progenitors, typically $8 M_{\odot}$ (S. J. Smartt 2009) to $50 M_{\odot}$ (T. Tsujimoto et al.

¹⁷ Note the different definition from K. E. Whitaker et al. (2017) for f_{obsc} , which also differs in their computation of SFR_{IR} using a calibration from UV and $24\mu\text{m}$ photometry (K. E. Whitaker et al. 2014).

1997):

$$k_{\text{CC}} = \frac{\int_{8 M_{\odot}}^{50 M_{\odot}} \phi(M) dM}{\int_{0.1 M_{\odot}}^{125 M_{\odot}} M \cdot \phi(M) dM}, \quad (6)$$

where the denominator is limited to the total mass range of 0.1 to 125 $M_{\odot}$. As the SFR estimates used in this work are based on a P. Kroupa (2001) IMF, we adopt a value of $k_{\text{CC}} = 0.0104 M_{\odot}^{-1}$. This is consistent with the optically-thick regime ($\epsilon \approx 1$) of equation 5 of S. Mattila & W. P. S. Meikle (2001), $R_{\text{CC}}/\text{yr}^{-1} = 1.1 \times 10^{-12} \cdot \epsilon^{-1} \cdot L_{\text{FIR}}/L_{\odot}$, where ϵ is the fraction of optical/UV energy absorbed and re-radiated in the FIR. In comparison, for a E. E. Salpeter (1955) IMF¹⁸, this yields $k_{\text{CC}} = 0.0070 M_{\odot}^{-1}$ (e.g., D. R. Young et al. 2008; J. Melinder et al. 2012).

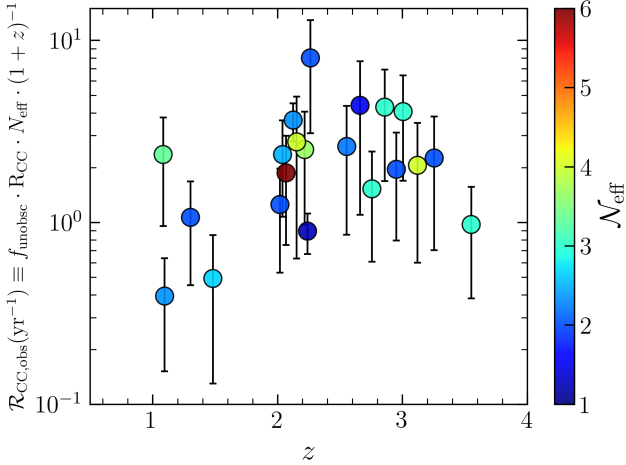


Figure 2. Observable rate of core-collapse supernovae $\mathcal{R}_{\text{CC,obs}}$ vs. redshift for the 21 PASSAGES galaxies considered, using $\mathcal{R}_{\text{CC,obs}}$ as defined in Equation 7. The unobscured fractions adopted are provided in Table 1. Colors show the effective multiplicity, $\mathcal{N}_{\text{eff}}$, described in Equations 1 and 2. The increase with redshift is predominantly due to a general increase in SFR with z , which is also responsible for the trend observed in Fig. 4 (see §3.3).

In Fig. 2, we show the observable rate of CCSN images¹⁹

$$\mathcal{R}_{\text{CC,obs}} \equiv f_{\text{unobsc}} \cdot R_{\text{CC}} \cdot \mathcal{N}_{\text{eff}} \cdot (1+z)^{-1} \quad (7)$$

¹⁸ For completeness, a G. Chabrier (2003) IMF integrated over the same progenitor mass ranges gives $k_{\text{CC}} = 0.0110 M_{\odot}^{-1}$, closer to that for the Kroupa IMF. However, since converting from a Salpeter to Chabrier IMF also lowers the SFR by a factor of 0.63 (P. Madau & M. Dickinson 2014), the resulting $R_{\text{CC}} = 0.0069 \cdot \text{SFR}_{\text{Salpeter}}$, thus certainly consistent within uncertainties.

¹⁹ To minimize confusion, we use $\mathcal{R}$ when referring to what we define as the observable rate, and simply R when referring to an intrinsic, rest-frame rate.

against redshift, with intrinsic rate R_{CC} determined from the intrinsic (i.e., magnification-corrected) SFR_{IR} . The apparent rates, μSFR , and magnifications μ are retrieved from the references given in Table 1. Given the dusty nature of these sources, we include f_{unobsc} in the equation *ab initio*, for a more realistic quantification of expected rates. This does not quantify the fraction of supernovae that could be detectable in any observational campaign, but is more akin to a *maximum* recoverable fraction for what is reasonable with current telescope facilities. For comparison, I. Mäntynen et al. (2025) recently found that the undetectable fraction of CCSNe in low- z LIRGs for a survey sensitive to $A_V < 16$ mag is $66^{+8.6}_{-14.6}\%$. Using our formulation, this would suggest $f_{\text{unobsc}} = 34^{+14.6}_{-8.6}\%$. For a much shallower survey down to $A_V < 3$ mag, they found instead an undetectable fraction of $89.7^{+2.6}_{-4.4}\%$.

The large uncertainties in $\mathcal{R}_{\text{CC,obs}}$ are the direct result of a combination of *i*) the broad range chosen for f_{unobsc} ; *ii*) inherently large uncertainty in SFR_{IR} ; *iii*) large uncertainty in magnification μ for the current lens models; and *iv*) the conservative fractional uncertainties used for the effective multiplicity $\mathcal{N}_{\text{eff}}$. However, despite this uncertainty, the median $\mathcal{R}_{\text{CC,obs}}$ is very high at $\sim 2 \text{ yr}^{-1}$, especially considering the average volumetric rates of $\sim 10^{-4} - 10^{-3} \text{ yr}^{-1} \text{ Mpc}^{-3}$ at Cosmic Noon (T. Dahlen et al. 2012; L.-G. Strolger et al. 2015). As discussed in §2.4, the IR-inferred SFRs are likely the closest to the true SFRs for these dust-obscured galaxies, but they are not necessarily representative of the rates of SNe that one could expect to observe. We adopt a typical value of $f_{\text{unobsc}} = 0.2 \pm 0.1$, following the findings of Balmer decrements for two members of the sample and for other DSFGs in the literature (§2.4)²⁰.

In §3.3, we compare the predicted rates R_{CC} (and the rate of SNe Ia) for PASSAGES with those from other works that also examine candidate samples for SN monitoring, alongside the expected rates for host galaxies of some of the already-discovered gISNe. In Fig. 2, we observe an increase in $\mathcal{R}_{\text{CC,obs}}$ with redshift, which is likely to be driven primarily by the generally higher SFRs in the sample above $z \gtrsim 2$ (whereas $\mathcal{N}_{\text{eff}}$ is essentially constant with redshift). In §3.3, we discuss how this compares with the redshift evolution of the cosmic star formation rate density.

²⁰ As noted in Table 1, for two exceptions we use the direct measurements of f_{unobsc} that are available for PJ0116-24 (D. Liu et al. 2024) and PJ1127+42 (B. L. Frye et al. 2024).

3.2. Estimating the rate of Type Ia SNe

As the progenitors of Type Ia supernovae are best understood to be binary systems that include a white dwarf star, the rate of SNe Ia inherently depends in part on the number of evolved lower-mass stars (A. J. Ruiter & I. R. Seitenzahl 2025). In turn, since these make up the bulk of the stellar mass of a typical galaxy, it is reasonable to expect that the rate of Type Ia supernovae R_{Ia} would increase with M_* (either linearly or with some positive power law). The donor star from which the progenitor white dwarf accretes may itself be another white dwarf or a main sequence or giant star, which implies that R_{Ia} should also have some dependence on the SFR, as with R_{CC} .

F. Mannucci et al. (2005) and E. Scannapieco & L. Bildsten (2005) found that the observed rate of SNe Ia could be described as a two-component linear combination of SFR and M_* (see also M. Sullivan et al. 2006). M. Smith et al. (2012) included a power law for both terms in their bivariate parameterization, favoring

$$\begin{aligned} R_{\text{Ia}} &= (1.05 \pm 0.16) \times 10^{-10} M_*^{0.68 \pm 0.01} \\ &\quad + (1.01 \pm 0.09) \times 10^{-3} \text{SFR}^{1.00 \pm 0.05} \\ &\approx (6.6 \pm 1.0) \times 10^{-4} \left(\frac{M_*}{10^{10} M_\odot} \right)^{0.68 \pm 0.01} \\ &\quad + (1.0 \pm 0.1) \times 10^{-1} \left(\frac{\text{SFR}}{100 M_\odot \text{ yr}^{-1}} \right)^{1.00 \pm 0.05} \end{aligned} \quad (8)$$

with a “prompt” term and a “delayed” term (although this is for a sample at $z < 0.25$). M. Sullivan et al. (2006) found that the rate of SNe Ia per unit mass increases with increasing sSFR, which may partly explain the sub-linear dependence on M_* . A more rigorous treatment would use the star formation history (SFH) convolved with the delay time distribution (DTD; P. Madau et al. 1998; F. Mannucci et al. 2006). Instead, the “A+B” parameterization with M_* and SFR essentially samples the continuous SFH and DTD at two times (D. Maoz et al. 2014). However, as cautioned by P. Andersen & J. Hjorth (2018), this calibration is unconstrained for starburst galaxies with $\log(\text{sSFR}) > -9$. While this dependency may in principle also evolve with redshift, several combinations of cosmic star formation histories and delay time distributions tested by P. A. Palicio et al. (2024) were able to adequately fit the observed rates of Type Ia supernovae (which are themselves still quite uncertain above $z > 2$). For our purposes, we consider it justifiable to use the M. Smith et al. (2012) results—derived from a wide range of $8 < \log(M_*/M_\odot) < 11$ —to make predictions for our sample.

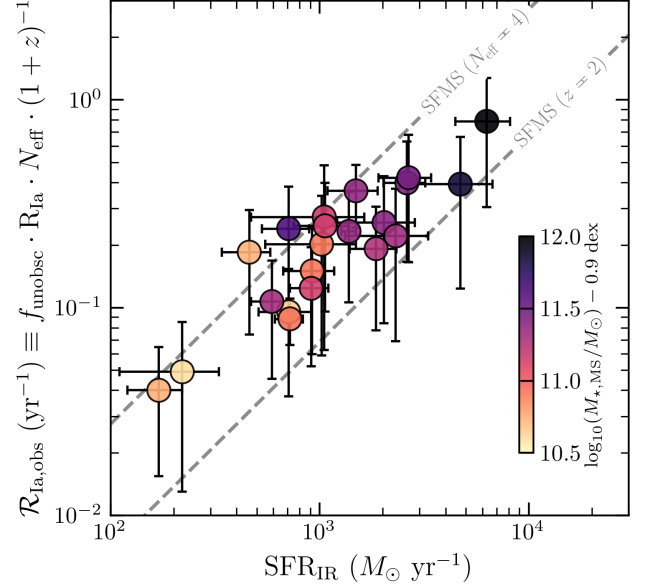


Figure 3. For the same galaxies as in Fig. 2: predicted observer-frame rates $\mathcal{R}_{\text{Ia,obs}}$ of Type Ia supernovae (the intrinsic rate R_{Ia} multiplied by the unobscured fraction f_{unobsc} , the effective number of multiple images $\mathcal{N}_{\text{eff}}$ and the time dilation factor, $(1+z)^{-1}$). In this regime of active star formation, R_{Ia} is primarily a function of SFR and weakly dependent on M_* . Stellar masses are bounded by assuming that the sSFRs lie between 0.3 dex below and 0.9 dex above the star-forming main sequence. Colors of data points show this effective lower limit on M_* for 0.9 dex above the SFMS. A dashed gray line shows the expected rate for a galaxy exactly on the SFMS at $z = 2$ according to the J. S. Speagle et al. (2014) treatment, and a second dashed line shows the observable rate for the same galaxy with an effective multiplicity of $\mathcal{N}_{\text{eff}} = 4$.

Unfortunately, the stellar masses for the majority of the PASSAGES DSFGs remain unconstrained, but they are at least very likely to be on the massive end of the stellar mass function ($\log(M_*/M_\odot) > 10.5$) given their extreme luminosities and molecular gas masses (K. C. Harrington et al. 2021). While most are actually detected in H -band imaging with HST (P. S. Kamienieski et al. 2024a), insufficient observed-frame near-IR data have been collected so far to enable robust SED fitting for most of the background lensed sources²¹, apart from two exceptions. For the pair of interacting DSFGs behind the G165 cluster,

²¹ In principle, lensing-corrected rest-frame K -band luminosity may correlate with stellar mass (e.g., T. H. Jarrett et al. 2013) and could be determined for $z \sim 2$ with WISE at $4.6\mu\text{m}$, for example. However, there is likely significant differential magnification between the stellar continuum and dust continuum, and measuring the magnification factors for the rest-frame near-IR is beyond the scope of this work.

JWST NIRCcam and NIRSpec observations yield stellar masses of $\log_{10} M_{\star} \approx 10.2$ and 10.3 (B. L. Frye et al. 2024; P. S. Kamieneski et al. 2024b). With their IR-inferred SFRs, their sSFRs are both 0.9 dex above the MS, but the likely tidal interaction between the two

galaxies might be driving an elevated starburst phase above the rest of the sample. Also, D. Liu et al. (2024) found a large stellar mass of $\log(M_{\star}/M_{\odot}) \approx 11.2 \pm 0.4$ for PJ0116-24 with $\text{SFR}_{\text{IR}} \approx 1480 M_{\odot} \text{yr}^{-1}$, which is 0.8 dex above the star-forming main sequence (SFMS).

Table 1. Estimated intrinsic and observable rates of SNe in a subset of PASSAGES

ID	z_s	μ	$\text{SFR}_{\text{IR},\text{intr.}}$	$f_{\text{unobsc}}^{\dagger}$	$R_{\text{CC}}(\text{SFR}_{\text{IR}})$	R_{Ia}	$\mathcal{N}_{\text{eff}}$	$\mathcal{R}_{\text{CC},\text{obs}}$	$\mathcal{R}_{\text{Ia},\text{obs}}$	Refs.
			($M_{\odot} \text{yr}^{-1}$)	(%)	(yr^{-1})	(yr^{-1})		(yr^{-1})	(yr^{-1})	
PJ0116-24	2.125	≈ 17	1490 ± 400	$\approx 32\%^{\ddagger}$	15.5 ± 4.2	1.5 ± 0.4	2.3 ± 0.5	3.6 ± 0.9	1.1 ± 0.4	(1)
PJ0143-01	1.096	7.1 ± 2.2	170 ± 50	$20 \pm 10\%$	1.8 ± 0.5	0.2 ± 0.1	2.3 ± 0.5	0.4 ± 0.2	0.2 ± 0.1	(2) μ (3) SFR
PJ0209+00	2.554	10.5 ± 3.7	2030 ± 820	$20 \pm 10\%$	21.1 ± 8.5	2.1 ± 0.8	2.2 ± 0.4	2.6 ± 1.8	1.3 ± 0.6	(2) μ (4) SFR
PJ0226+23	3.120	28.2 ± 11.3	1020 ± 470	$20 \pm 10\%$	10.6 ± 4.9	1.0 ± 0.5	4.0 ± 0.8	2.1 ± 1.5	1.0 ± 0.5	(2) μ (3) SFR
PJ0305-30	2.263	2.2 ± 0.6	6290 ± 1850	$20 \pm 10\%$	65 ± 19	6.4 ± 1.9	2.0 ± 0.4	8.0 ± 4.9	3.9 ± 1.4	(2) μ (3) SFR
PJ0748+59	2.755	≈ 15	920 ± 250	$20 \pm 10\%$	9.6 ± 2.6	0.9 ± 0.3	3.0 ± 0.6	1.5 ± 0.9	0.8 ± 0.3	(5) μ (3) SFR
PJ0846+15	2.664	7.7 ± 1.5	5200 ± 2600	$20 \pm 10\%$	54 ± 27	5.3 ± 2.6	1.5 ± 0.3	4.4 ± 3.3	2.2 ± 1.2	(6) μ (3) SFR
PJ1053+60	3.549	≈ 24	710 ± 200	$20 \pm 10\%$	7.4 ± 2.1	0.7 ± 0.2	3.0 ± 0.6	1.0 ± 0.6	0.5 ± 0.2	(7) μ (3) SFR
PJ1053+05	3.005	7.6 ± 0.7	2610 ± 590	$20 \pm 10\%$	27.1 ± 6.1	2.7 ± 0.6	3.0 ± 0.6	4.1 ± 2.4	2.0 ± 0.6	(2) μ (4) SFR
PJ1127+46	1.303	4.5 ± 0.6	590 ± 120	$20 \pm 10\%$	6.1 ± 1.2	0.6 ± 0.1	2.0 ± 0.4	1.1 ± 0.6	0.5 ± 0.2	(2) μ (3) SFR
PJ1127+42	2.236	16.4 ± 3.0	720 ± 110	$\approx 31\%$	7.5 ± 1.1	0.7 ± 0.1	1.3 ± 0.3	0.9 ± 0.2	0.3 ± 0.1	(8) μ (4) SFR
PJ1138+32	2.019	2.8 ± 0.4	910 ± 190	$20 \pm 10\%$	9.5 ± 2.0	0.9 ± 0.2	2.0 ± 0.4	1.3 ± 0.7	0.6 ± 0.2	(2) μ (3) SFR
PJ1139+20	2.858	4.8 ± 1.1	2660 ± 750	$20 \pm 10\%$	27.7 ± 7.8	2.7 ± 0.8	3.0 ± 0.6	4.3 ± 2.6	2.1 ± 0.7	(2) μ (3) SFR
PJ1322+09	2.068	≈ 20	460 ± 120	$20 \pm 10\%$	4.8 ± 1.2	0.5 ± 0.1	6.0 ± 1.2	1.9 ± 1.1	0.9 ± 0.3	(5) μ (3) SFR
PJ1326+33	2.951	4.3 ± 0.6	1860 ± 470	$20 \pm 10\%$	19.3 ± 4.9	1.9 ± 0.5	2.0 ± 0.4	2.0 ± 1.2	1.0 ± 0.3	(2) μ (3) SFR
PJ1329+22	2.040	11 ± 2	1380 ± 110	$20 \pm 10\%$	14.4 ± 1.1	1.4 ± 0.1	2.5 ± 0.5	2.4 ± 1.3	1.2 ± 0.3	(6) μ (3) SFR
PJ1336+49	3.254	8.3 ± 3.1	2310 ± 990	$20 \pm 10\%$	24 ± 10	2.4 ± 1.0	2.0 ± 0.4	2.3 ± 1.6	1.1 ± 0.5	(2) μ (3) SFR
PJ1446+17	1.084	3.9 ± 0.7	710 ± 180	$20 \pm 10\%$	7.4 ± 1.9	0.7 ± 0.2	3.3 ± 0.7	2.4 ± 1.4	1.2 ± 0.4	(2) μ (3) SFR
PJ1449+22	2.153	10.1 ± 5.2	1050 ± 580	$20 \pm 10\%$	10.9 ± 6.0	1.1 ± 0.6	4.0 ± 0.8	2.8 ± 2.1	1.4 ± 0.8	(2) μ (3) SFR
PJ1607+73	1.482	6.8 ± 1.7	220 ± 110	$20 \pm 10\%$	2.3 ± 1.1	0.2 ± 0.1	2.7 ± 0.5	0.5 ± 0.4	0.2 ± 0.1	(2) μ (4) SFR
PJ2313+01	2.217	6.1 ± 1.2	1060 ± 310	$20 \pm 10\%$	11.0 ± 3.2	1.1 ± 0.3	3.7 ± 0.7	2.5 ± 1.5	1.2 ± 0.4	(2) μ (3) SFR

[†] Unobscured SFR estimated using the adopted f_{unobsc} , except for PJ0116-24 (D. Liu et al. 2024) and G165, which are estimated directly from H α (B. L. Frye et al. 2024) following correction from the measured Balmer decrement. For G165, we assume that the f_{unobsc} for Arc 1 ($\approx 31\%$) applies also for its counterpart, Arc 3.

[‡] Derived using $\text{SFR}_{\text{H}\alpha,\text{corr}} = 470 \pm 60 M_{\odot} \text{yr}^{-1}$ (D. Liu et al. 2024).

NOTE— **References** for SFR and μ estimates: (1) D. Liu et al. 2024; (2) P. S. Kamieneski et al. 2024a (3) D. A. Berman et al. 2022; (4) K. C. Harrington et al. 2016; (5) P. Kamieneski et al., in prep.; (6) N. Foo et al. 2025; (7) Q. D. Wang et al. 2024; (8) P. S. Kamieneski et al. 2024b; (9) A. Díaz-Sánchez et al. 2017.

In Appendix A, we use the expected offset of DSFGs from the SFMS to gain an imprecise estimate of reasonable stellar masses. However, ultimately the dependence of Equation 8 on $M_{\star}$ is highly subdominant to the contribution from SFR in the star-forming regime ($\text{SFR} \gtrsim 10 M_{\odot} \text{yr}^{-1}$). Fortunately, this allows us to still predict R_{Ia} for the sample within reason, which we include in Table 1. In Fig. 3, we show the predicted observable rates of Type Ia supernovae for PASSAGES, $\mathcal{R}_{\text{Ia},\text{obs}} \equiv f_{\text{unobsc}} \cdot R_{\text{Ia}} \cdot \mathcal{N}_{\text{eff}} \cdot (1+z)^{-1}$, as a function of their SFR_{IR} . In this regime of star formation, the SN Ia

rates are dominated by the contribution from SFR, but the data points' colors correspond to the lower limits in stellar masses that we adopt, at 0.9 dex above the star-forming main sequence. In Fig. 4, we show the observable rates $\mathcal{R}_{\text{Ia},\text{obs}} \cdot (f_{\text{unobsc}})^{-1}$ vs. redshift²², with transparent points indicating the intrinsic rates R_{Ia} . This

²² Dividing $\mathcal{R}_{\text{Ia},\text{obs}}$ by the obscured fraction in this version reduces the relative uncertainties and thus makes it easier to interpret. Given that R_{Ia} is dominated by the SFR, we expect the SNe Ia to be subject to roughly the same average attenuation as the CCSNe, but few works have yet examined this at these redshifts.

particularly emphasizes our finding that the decrement in observable rate due to redshift time dilation is approximately counteracted by the boost provided by multiple imaging.

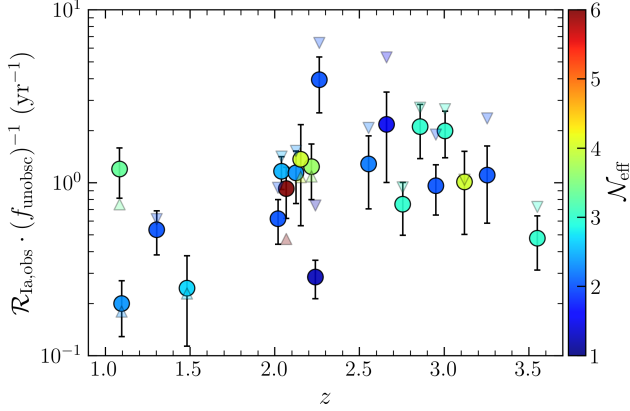


Figure 4. Redshift distribution of the observable rate of SNe Ia from PASSAGES estimated in Fig. 3, $\mathcal{R}_{\text{Ia}}$, but now removing the factor of f_{unobs} (thus reducing uncertainties and improving legibility). Colors indicate the effective multiplicity $\mathcal{N}_{\text{eff}}$. Transparent, smaller triangles indicate the intrinsic rates (R_{Ia}) for each target (i.e., without factoring in the boost from multiple-imaging or the $1+z$ decrement from cosmological time dilation). The triangles for intrinsic rates are oriented to point towards their corresponding observable rates. This illustrates that since $\mathcal{N}_{\text{eff}} \cdot (1+z)^{-1}$ is typically of order unity, these effects roughly cancel out.

3.3. Predicting the rate of independent supernova events

Up to this point, we have considered the rate of observable supernovae from Earth’s perspective, taking into account both cosmological time dilation by $(1+z)^{-1}$ and amplification by multiple imaging $\mathcal{N}_{\text{eff}}$. This rate is useful if one’s goal is to catch any image of a gLSN, but if the goal is to perform TD cosmography, then the rate of *independent* supernovae events is of greater interest²³. We show these rates for PASSAGES in Fig. 5, along with the predicted rates from similar works forecasting gLSN rates in targeted monitoring searches, including the Frontier Fields (T. Petrushevska et al. 2018b,a) and 128 galaxy-scale lenses from Y. Shu et al. (2018, 2021). We also indicate rates from the host galaxies of a number of the already-discovered gLSNe—e.g., the core-collapse SN Refsdal (P. L. Kelly et al. 2015) in a galaxy lensed by MACS J1149, and the set of Type Ia supernovae that

²³ Here, this rate still accounts for R_{CC} and R_{Ia} being modulated by $(1+z)^{-1}$ time dilation, but not by f_{unobs} , to allow for a more direct comparison with literature values.

includes SN Requiem/SN Encore (S. A. Rodney et al. 2021; J. D. R. Pierel et al. 2024b) in MRG-M0138 (A. B. Newman et al. 2018) and SN H0pe in G165 Arc 2abc (B. L. Frye et al. 2024).

While R_{CC} and R_{Ia} might appear at first to be equivalent to within a constant factor, this is not quite the case. By equations 5 and 8, the ratio $R_{\text{Ia}}/R_{\text{CC}} \sim \text{sSFR}^{-1} \cdot M_{\star}^{-0.32}$ (plus a constant term). By the star-forming main sequence, many of the star-forming galaxies included in Fig. 5 will have comparable values of sSFR, while the ratio is more weakly dependent on $M_{\star}$. For a $10^{10} M_{\odot}$ galaxy on the main sequence at $z \sim 2$, for example, $R_{\text{Ia}}/R_{\text{CC}} \approx 0.1$ (adopting a Kroupa IMF).

Every PASSAGES object included in this work exceeds the rate of all other targets considered in Fig. 5, demonstrating the dramatic potential of this sample. Most are even > 2 dex above typical arcs in the Frontier Fields; while these clusters are remarkable for their lensing power, the background objects are largely unremarkable in terms of their SFR. Perhaps more surprising is the observation that our predictions for R_{CC} are all $\gtrsim 1.5$ dex above the host galaxy of SN Refsdal, and even our predicted R_{Ia} are $\gtrsim 1$ dex above MRG-M0138, the host of two recent SNe Ia, Requiem and Encore. We also observe that the redshift-dilated R_{CC} and R_{Ia} rates for PASSAGES roughly increase with redshift (likely owing to their identification by flux; see Fig. 2 of Q. D. Wang et al. 2024). This trend is contrary to the slow decline of the (dilated) cosmic star formation rate density, $\psi(z) \cdot (1+z)^{-1}$ (P. Madau & M. Dickinson 2014), shown as a gray curve in Fig. 5.

In absolute terms, the median (Earth-frame) occurrence rate of individual CCSNe is 3.5 yr^{-1} and $\sim 0.3 \text{ yr}^{-1}$ for SNe Ia. This does not imply, we caution, that any 1-year monitoring program would yield multiple gLSNe per field, as the actual yield is the occurrence rate multiplied by the *control time* (F. Zwicky 1938). This is effectively the cumulative duration for which a given supernovae would fall above the detection threshold, which itself depends on a combination of observing sensitivity, dust attenuation, lensing magnification, and the precise supernova type. We do not simulate a mock observing campaign in this work, but simply remark that this sample has $\gtrsim 18$ members with core-collapse occurrence rates $R_{\text{CC}} \cdot (1+z)^{-1}$ in excess of 1 yr^{-1} (with a median closer to 4 per year). As a conservative example, an observer-frame control time of 1 month per epoch, with 3 epochs over the course of a year, would result in a yield of $N_{\text{CC}} \sim 0.5$ detections for each field. If these 18 fields were all monitored at this rate, one could expect to detect ~ 9 CCSNe with this campaign alone (not

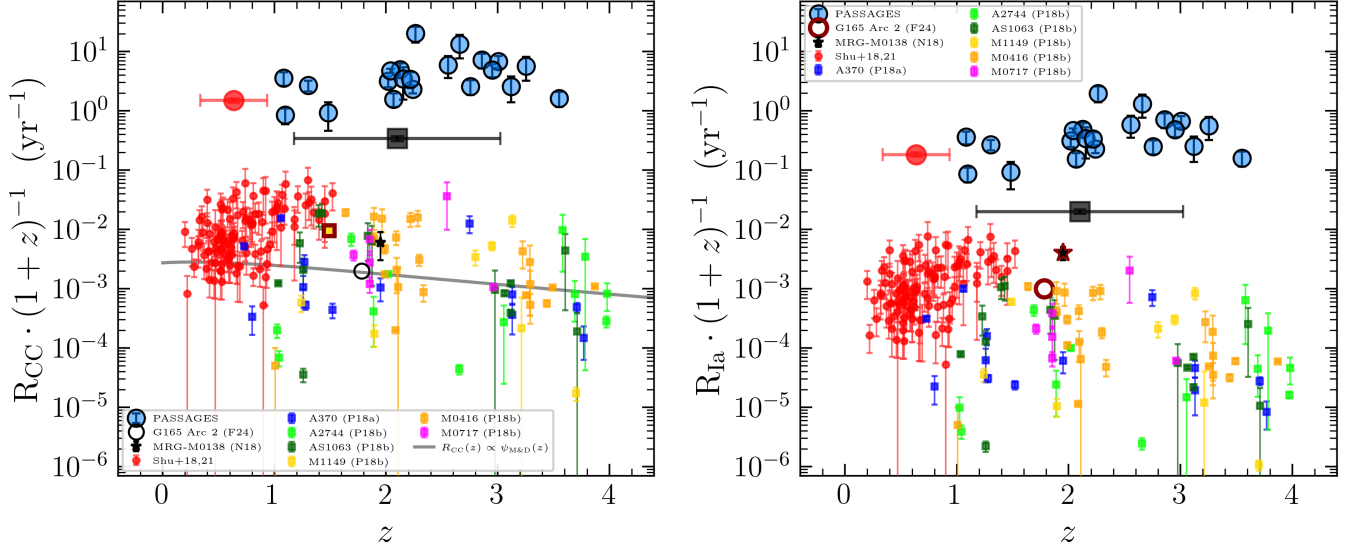


Figure 5. Intrinsic supernova rates (core-collapse on *left*, Type Ia on *right*), still rescaled by time dilation but excluding multiple imaging (and $f_{\text{unobs.}}$ correction), vs. redshift. Whereas $\mathcal{R}_{\text{CC,obs}}$ and $\mathcal{R}_{\text{Ia,obs}}$ represented the average rate at which supernova images appear, $R_{\text{CC}} \cdot (1+z)^{-1}$ and $R_{\text{Ia}} \cdot (1+z)^{-1}$ are the actual rate of individual supernova events, as if the galaxies were not lensed. We compare with the predictions made for a large sample of galaxy-galaxy lenses by Y. Shu et al. (2018), incorporating the corrections from Y. Shu et al. (2021), and the Frontier Fields considered by T. Petrushevska et al. (2018a,b). The sums of the Y. Shu et al. and T. Petrushevska et al. samples are shown as large red circles and large black squares, respectively. Predicted rates for G165 Arc 2, the host galaxy of the Type Ia SN H0pe, are shown with open circles (based on SFR/ M_* from B. L. Frye et al. 2024). Similarly, the predicted rates for MRG-M0138 (based on A. B. Newman et al. 2018) are indicated as black stars (with a dark red border on the right panel, highlighting SN Requiem/Encore). In the left panel, the MACS J1149 point with a dark red border is the host galaxy of the discovered core-collapse glSN Refsdal. The PASSAGES objects considered in this work have CCSN rates about 100 times greater than the Y. Shu et al. sample (and similarly for SNe Ia). In the left panel, the gray curve shows the expectation of $R_{\text{CC}}(z) \propto \psi(z)$ for the P. Madau & M. Dickinson (2014) parameterization of the cosmic star formation rate density $\psi(z)$, which has units of $M_{\odot} \text{ yr}^{-1} \text{ Mpc}^{-3}$, rescaled arbitrarily to approximately match the Frontier Fields data points.

to mention any SNe Ia that are uncovered). With the depths of 28 – 29 mag routinely reachable by JWST at $\sim 1.5 \mu\text{m}$ in $\sim 1 \text{ hr}$, it is highly feasible to extend the per-epoch control time well beyond 1 month (e.g., Fig. 12 of T. Petrushevska et al. 2016), even for only modestly magnified arcs, such that even a subsample would be expected to result in at least one detection.

As another example, we consider SNe Ia, which of course are more uniform in their light curve behavior, and which are themselves predicted to be quite frequent in HyLIRGs. With SN H0pe as a recent example of a $z \sim 2$ glSN Ia in a relatively dusty environment, we note that its de-magnified peak was observed at ~ 24 mag in F150W (rest-frame V -band), but it also remained above 25 mag for a duration of ≈ 90 days in the observed frame (J. D. R. Pierel et al. 2024a). The light curve model suggested $A_V = 1.21 \pm 0.11$ (also W. Chen et al. 2024); if the supernova were subjected to substantially higher attenuation as might be expected for HyLIRGs, such as $A_V = 5$, then the peak would be ~ 4 mag fainter (i.e. ~ 28 mag) and the SN would remain above 29

mag for an observer for ~ 3 months. With only modest magnification $\mu = 5$ (or 1.7 mag), a 5σ point-source limiting depth of 27.3 mag would be required for a detection, achieved in less than 10 minutes of integration with JWST/NIRCam²⁴ or < 2 orbits with HST WFC3/IR in F160W.

As a caveat, however, the occurrence rates we estimate do not account for the possibility that some detected SN events might be caught only when the last image is still visible. In this hypothetical scenario, there is not likely to be any hope for performing TD cosmography, since no delays can actually be measured through light curves. It is rather non-trivial to quantify the likelihood of this actually occurring, as it depends on both the time delays between images and the control time (such that the penultimate image to arrive has faded below the detection limit, but not the final image).

²⁴ Sensitivity is estimated with the JWST Exposure Time Calculator (K. M. Pontoppidan et al. 2016).

To place these forecasts in context, we compare with the yields that are currently expected from other search strategies. A. Sainz de Murieta et al. (2024) predicted that LSST will uncover ~ 7 Type Ia gLSNe per year within known galaxy-lensed objects that are suitable for TD cosmography. In this case, the authors note that an H_0 measurement is not feasible if the host galaxy is not itself lensed as well (thereby enabling precise lens modeling). Similarly, N. Arendse et al. (2024) predict a “gold sample” of ~ 10 gLSNe Ia yr^{-1} uncovered with LSST that are sufficiently bright and with time delays that are long enough to enable follow-up observations (which are likely essential; S. Huber et al. 2019). Complementary to this will be an approach of monitoring a “watchlist” of lensing galaxy clusters (D. Rychanowski et al. 2023), which are beneficial for reasons discussed in §3.4. M. Bronikowski et al. (2025) predict 1 – 2 such SNe will be discovered by LSST per year from a sample of 46 well-studied lensing clusters. The SNe Ia cosmology program of the upcoming *Nancy Grace Roman Space Telescope* (R. Hounsell et al. 2018) will also reveal some fraction that are gravitationally lensed (M. Oguri & P. J. Marshall 2010), which may number as high as ~ 11 gLSNe Ia and ~ 20 cumulative lensed CCSNe (J. D. R. Pierel et al. 2021).

3.4. Identifying candidates with the longest median time delay

Cluster-scale lenses are typically the best candidates for high rates of lensed SNe in the observed frame due to their large lensing cross sections $\sigma(z_s)$ in the source plane at z_s (E. L. Turner et al. 1984). This cross-section is closely linked to the Einstein radius

$$\theta_E = \left[\frac{4GM(<\theta_E)}{c^2} \cdot \frac{D_{LS}}{D_L D_S} \right]^{1/2} \quad (9)$$

(e.g., R. Narayan & M. Bartelmann 1996) for enclosed mass $M(<\theta_E)$ and angular-diameter distances to the lens (D_L), to the source plane (D_S), and between these two (D_{LS}). To first order, the area that produces 4 lensed images from a singular isothermal ellipsoid (again excluding demagnified images) is $\sigma_4 = \pi \epsilon^2 \theta_E^2 / 6$ (C. Kochanek et al. 2006), where $\epsilon \equiv 1 - b/a$ is the ellipticity (from major and minor axes, a and b). The cross section then scales linearly with mass, $\sigma_4 \propto M(<\theta_E)$, such that a cluster can have orders of magnitude larger areas. As discussed in §2.2, this larger area of magnification means that a galaxy is more likely to be lensed uniformly into a constant multiplicity of images, but it also means that objects nearby in projected distance will also be multiply-imaged (§3.6). This further amplifies the expected rate of observable SNe.

Cluster lenses with large Einstein radii are also beneficial for following up lensed SNe for the purpose of TD cosmography (e.g., M. Bronikowski et al. 2025). It is true that time delays between any pair of cluster-lensed images can still be very short (e.g. a few days)—especially in the case where the deflection is dominated by a galaxy- or group-scale halo embedded within the cluster. For example, this was the case with the first four images of SN Refsdal, which formed an Einstein cross configuration ($\theta_{\text{Ein}} \approx 1.3$; delays $\approx 10 - 20$ days; P. L. Kelly et al. 2023a) around an elliptical galaxy in the cluster at $z = 0.54$ (P. L. Kelly et al. 2015). However, one should expect that a larger Einstein radius (or angular separation between images) would correlate with a larger median delay, by virtue of the longer path lengths followed by the highly-deflected light rays.

In practice, varying approaches are used to quantify the Einstein radius of a system (see for example §3.5 of P. S. Kamienieski et al. 2024a). For the PASSAGES objects in this work, the values of θ_{Ein} shown in Table 2 are derived according to the *equivalent* Einstein radius definition, which is the radius of the smallest circle centered on the peak of lensing convergence κ that contains an average $\langle \kappa \rangle < 1$ (P. Schneider et al. 1992). For lensed systems with multi-modal mass distributions, different Einstein radii may be measured for the different mass components. This notably includes G165, the field containing both SN H0pe and the PJ1127+42 DSFG. With the model from P. S. Kamienieski et al. (2024b), we measure $\theta_{\text{Ein}} = 10''.7 \pm 1''.1$ for the $z = 2.24$ DSFG arc on the southwest side of the cluster, and $21''.1 \pm 0''.5$ for the $z = 1.78$ arc hosting SN H0pe on the northeast side. B. L. Frye et al. (2019) measured a lens size of $13''$, but with a different definition (based on the total area inside the critical curve for the full cluster). M. Pascale et al. (2022) measured $15''.3$ for $z = 9$ using the same approach, or $\approx 14''.4$ rescaled to $z_s = 2.24$, although this and the B. L. Frye et al. measurement were made before new constraints from NIRCcam were available (B. L. Frye et al. 2024).

For other previously discovered gLSNe summarized at the bottom of Table 2, the Einstein radii are estimated using the publicly-available Frontier Fields lens models (J. M. Lotz et al. 2017). For these, we also employ a model-independent approach to determine the radius of a circle that best captures the distribution of features/clumps within the lensed arcs (e.g., J. D. Remolina González et al. 2020; S. D. Mork et al. 2025).

Fig. 6 shows the median lens model-predicted time delay ($\bar{t}_d$) vs. Einstein radius for the PASSAGES sample, along with the observed/predicted values for the set of

known gISNe. While there is a decent amount of scatter—especially at the high- θ_E , high- t_d end—there is a clear strong correlation between t_d and θ_E (Spearman’s rank correlation coefficient $\rho = 0.89$, with high significance $p \ll 0.01$), such that θ_E may be used to select likely long-delay lenses as a rule-of-thumb. As we discuss in Appendix B, this correlation has some theoretical underpinning, since time delays can be related to the image separations of arcs relative to the lens centroid.

3.5. Optimizing the success of a random monitoring program

Ideally, for a monitoring program to be successful, time delays between images should be relatively comparable to the average duration between supernovae in the observer-frame—i.e., $\tau_{\text{SN}} \equiv (R_{\text{CC}} + R_{\text{Ia}})^{-1} \cdot (1 + z)$. If the median time delay is much less than this characteristic time between SNe, $\tilde{t}_d \ll \tau_{\text{SN}}$, then multiple imaging does not contribute very favorably to boosting the rate of observable SNe. In this scenario, there would still

be long durations where no SN images would be visible, presenting challenges for monitoring campaigns. The PASSAGES targets and the hosts of some of the confirmed gISNe in the literature are shown in Fig. 7. There are also unique challenges for fields with very short τ_{SN} timescales (e.g. less than 1 month observed-frame), as it can then become difficult to confirm that transient events seen in multiple images of a galaxy are in fact images of the same supernova. This risk of confusion can certainly be mitigated: information on parity and relative location of the transient within the arc can be helpful in ruling out unrelated events. Very few targets are likely to lie in this regime, and a well-refined lens model can assist in assessing the reliability of gISN candidates. For PASSAGES, for example, PJ0846+15 nominally has a very short τ_{SN} , but in reality, the very high SN rates arise from a very high SFR from multiple galaxies in a candidate protocluster core (N. Foo et al. 2025), in which case it is much easier to rule out unrelated transient events.

Table 2. Einstein radii and lens model-estimated median time delays for PASSAGES targets and for gISNe drawn from the literature.

ID	z_l	z_s	θ_{Ein} ($''$)	$\tilde{t}_d^{\dagger}$ (days)	$\max t_d^{\dagger}$ (days)	Refs. [‡]
PJ0116–24	0.555	2.125	2.37 ± 0.04	72	201	(1)
PJ0143–01	0.594	1.096	0.53 ± 0.08	3.4	10	(1)
PJ0209+00	0.202	2.554	2.6 ± 0.2	56	60	(1)
PJ0226+23	0.41	3.120	3.6 ± 0.3	110	190	(1)
PJ0305–30	0.5	2.263	0.6 ± 0.1	11	11	(1)
PJ0748+59	0.402	2.755	16.2 ± 1.3	3600	5400	(2,3)
PJ0846+15	0.766	2.664	$5.5 \pm 1.6^{\dagger\dagger}$	$560^{\dagger\dagger}$	$780^{\dagger\dagger}$	(4)
PJ1053+60	0.837	3.549	5.9	—	—	(5)
PJ1053+05	1.525	3.005	0.71 ± 0.04	23	62	(1)
PJ1127+46	0.42	1.303	0.58 ± 0.06	14	14	(1)
PJ1127+42	0.348	2.236	10.7 ± 1.1	470	580	(6,7)
PJ1138+32	0.52	2.019	0.40 ± 0.05	14	16	(1)
PJ1139+20	0.57	2.858	0.7 ± 0.4	46	59	(1)
PJ1322+09	0.6	2.068	6.1 ± 1.0	420	560	(3)
PJ1326+33	0.786	2.951	1.8 ± 0.2	510	580	(1)
PJ1329+22	0.44	2.040	11.0 ± 0.4	—	—	(8)
PJ1336+49	0.26	3.254	1.2 ± 0.1	36	39	(1)
PJ1446+17	0.493	1.084	0.82 ± 0.05	12	14	(1)
PJ1449+22	0.4	2.153	6.5 ± 1.2	300	460	(1)
PJ1607+73	0.65	1.482	1.0 ± 0.1	35	36	(1)
PJ2313+01	0.560	2.217	2.1 ± 0.2	58	94	(1)
Literature						
PS1-10afx	1.117	1.388	0.12	1.3	—	(9,10)
SN Refsdal(S1-S4)	0.54	1.49	$1.37 \pm 0.08^{\dagger\dagger}$	4	—	(11,12)
SN Refsdal(SX)	—	—	$4.5^{\dagger\dagger}$	380	—	(11,13)
iPTF16geu	0.216	0.409	0.3	1.4	—	(14,15,16)

Table 2 *continued*

Table 2 (*continued*)

ID	z_l	z_s	θ_{Ein} ($''$)	$\tilde{t}_d$ [†] (days)	max t_d [†] (days)	Refs. [‡]
SN Requiem/Encore	0.338	1.95	18.8 ± 1.1	7800	—	(17,18,19)
SN Zwicky	0.226	0.354	0.168	0.42	—	(20,21)
SN A370-C22	0.375	2.93	$1.0 \pm 0.5^{\dagger\dagger}$	31	—	(22)
SN H0pe	0.348	1.78	$21.1 \pm 0.5^{\dagger\dagger}$	83	—	(6,23)

[†] Median (and maximum) time delays for PASSAGES objects derived in this work (unless otherwise noted), using lens models from the supplied references. The representative values are simply determined by taking the median/maximum of the delays from the first image in each lensed system to arrive. Estimates are not currently available for PJ1053+60 and PJ1329+22.

[‡] References for table values, roughly in order of columns (e.g., SN discovery if applicable, followed by redshifts, then θ_{Ein} , and finally time delays). For SN Requiem/Encore, θ_{Ein} is determined by rescaling $\theta_{\text{Ein}}(z \rightarrow \infty)$ from S. Ertl et al. (2025) to $z_s = 1.95$.

^{††} Estimated in this work. The Einstein radii for the SNe in Abell 370 and MACS J1149 (Refsdal) are taken as the median θ_{Ein} derived from the publicly available convergence maps from the Frontier Fields (J. M. Lotz et al. 2017) lens models at <https://archive.stsci.edu/prepds/frontier/lensmodels>—in particular, the CATS, GLAFIC, and Sharon models (given their similarity to the LENSTOOL models used for the PASSAGES objects). The range of values are combined with our own empirical measurements according to the method from S. D. Mork et al. (2025). For PJ0846+15, θ_{Ein} and $\tilde{t}_d$ are estimated for the Einstein cross system, 12abcd (N. Foo et al. 2025).

NOTE—References: (1) P. S. Kamieneski et al. 2024a; (2) S. Amodeo et al. 2018; (3) P. Kamieneski et al., in prep.; (4) N. Foo et al. 2025; (5) Q. D. Wang et al. 2024; (6) B. L. Frye et al. 2024; (7) P. S. Kamieneski et al. 2024b; (8) A. Díaz-Sánchez et al. 2017; (9) R. Chornock et al. 2013; (10) R. M. Quimby et al. 2014; (11) P. L. Kelly et al. 2015; (12) S. A. Rodney et al. 2016; (13) P. L. Kelly et al. 2023b; (14) A. Goobar et al. 2017; (15) J. M. Diego et al. 2022; (16) S. Dhawan et al. 2020; (17) S. A. Rodney et al. 2021; (18) J. D. R. Pierel et al. 2024b; (19) S. Ertl et al. 2025; (20) A. A. Goobar et al. 2022; (21) J. D. R. Pierel et al. 2023; (22) W. Chen et al. 2022; (23) J. D. R. Pierel et al. 2024a.

The sample members with the longest predicted median time delays > 100 days include (in descending order) PJ0748+59, PJ0846+15, PJ1326+33, PJ1127+42, PJ1322+09, PJ1449+22, and PJ0226+23. These are also among the widest-separation targets, as expected. Except for PJ0226+23, these all also have $\tilde{t}_d > \tau_{\text{SN}}$ and $\mathcal{R}_{\text{CC,obs}} + \mathcal{R}_{\text{Ia,obs}} > 1$. This upper echelon only considers the $\mathcal{R}$ rates and expected time delays—i.e., not magnification, dust attenuation, or other factors that influence the control time.

Lastly, we note that the vast majority (90%) of objects in the full sample have an expected value of multiplicity, $\mathcal{N}_{\text{eff}} > 2$. This suggests that supernovae hosted by the primary DSFGs in these fields are likely to be multiply-imaged (and not just weakly lensed into a single image), and therefore hypothetically suitable for time-delay analyses—although $\mathcal{N}_{\text{eff}} < 2$ certainly does not mean gISNe are not possible. In the next section, we discuss contribution from other galaxies in the fields nearby to the DSFGs that might also be lensed into multiple images, but this generally requires a large lensing

cross section that can only be attributed to galaxy cluster lenses.

3.6. Contribution from galaxy-overdense regions

Thus far, our estimated SN rates have been limited to the lensed dusty star-forming galaxies that were responsible for the submillimeter flux by which the PASSAGES sample was selected. However, this does not account for the contributions from other galaxies that might also be gravitationally lensed, especially in the case of cluster-scale lenses with wide caustic networks. Numerous recent works have revealed that DSFGs, like other very massive galaxies (T. R. Greve et al. 2005), might be effective signposts of proto-clusters (or at least overdense regions; G. Kauffmann et al. 1999; Y.-K. Chiang et al. 2013; reviews by R. A. Overzier 2016; S. Alberts & A. Noble 2022). This complements the established association of proto-clusters with over-densities of H α and Lyman- α emitters, High- z Radio Galaxies, and Lyman Break Galaxies (e.g., C. De Breuck et al. 2004; B. P. Venemans et al. 2007; G. Miley & C. De Breuck 2008; E. Daddi et al. 2009; P. L. Capak et al. 2011; A. B. Drake et al. 2020). The rich set of literature with evi-

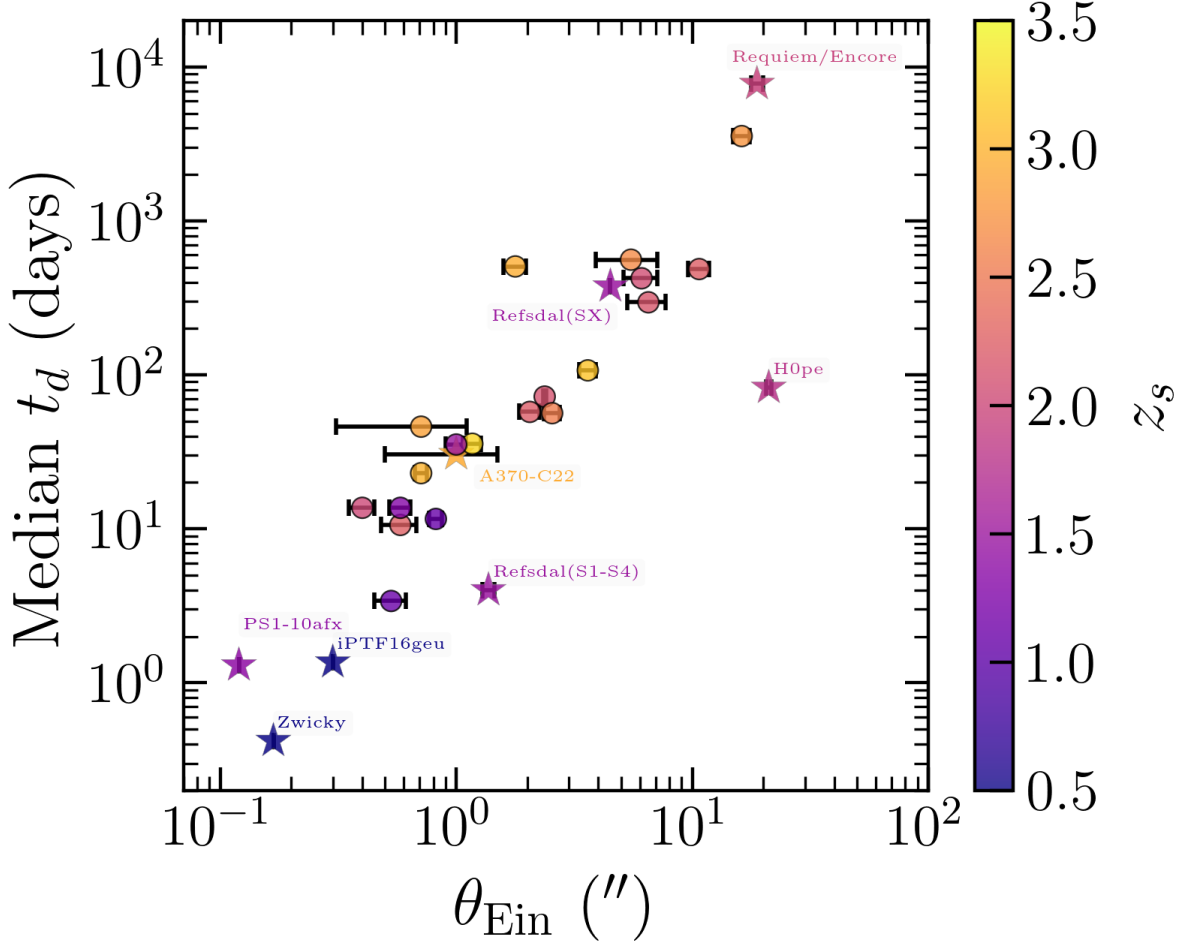


Figure 6. Median time delays t_d (between the first image to arrive and the other multiple images) in days vs. the Einstein radius θ_E in arcsec; see Table 2. Lensed SNe from the literature (and their time delay/Einstein radius measurements) shown as stars include PSF1-10afx (R. Chornock et al. 2013; R. M. Quimby et al. 2013, 2014), SN Refsdal (for both the Einstein Cross images S1-S4 and the last image SX; P. L. Kelly et al. 2015, 2016, 2023b; S. A. Rodney et al. 2016), iPTF16geu (A. Goobar et al. 2017; J. M. Diego et al. 2022), SN Requiem (S. A. Rodney et al. 2021), SN Zwicky (A. A. Goobar et al. 2022; A. Goobar et al. 2023; J. D. R. Pierel et al. 2023), the $z = 2.9$ SN discovered by W. Chen et al. (2022), and SN H0pe (B. L. Frye et al. 2024; J. D. R. Pierel et al. 2024a); see review by S. H. Suyu et al. (2024). For SN H0pe and the SX image of SN Refsdal, the time delays are the photometric light curve-derived values; in all other cases, delays are lens model-predicted. Despite the scatter, there is a statistically significant correlation between t_d and θ_E , validating the assumption that larger image separations generally yield longer time delays (see Appendix B).

dence for DSFGs (or over-densities of DSFGs) as proto-cluster signposts includes D. A. Riechers et al. (2010); H. Dannerbauer et al. (2014); C. M. Casey et al. (2015); H. Umehata et al. (2015); C. M. Casey (2016); D. L. Clements et al. (2016); C.-L. Hung et al. (2016); V. Smolčić et al. (2017); A. J. R. Lewis et al. (2018); T. B. Miller et al. (2018); R. Pavesi et al. (2018); R. Calvi et al. (2023). Two members of the PASSAGES sample have themselves been highlighted as protocluster candidates (B. L. Frye et al. 2024; N. Foo et al. 2025). On the other hand, DSFGs may not be efficient tracers of over-densities at all redshifts. T. B. Miller et al. (2015)

suggest that since $z \lesssim 2.5$, the high-mass end of galaxies within the most massive dark matter halos have already quenched their star formation and ceased to be submillimeter-bright.

Semi-analytic modeling by P. Araya-Araya et al. (2024) revealed an excess of SMGs in $z \gtrsim 2$ protocluster cores (relative to protocluster outskirts or field environments). The authors concluded that this was driven primarily by oversampling the high-mass end of the halo mass function. Fortunately, overdensities of starbursts in proto-cluster cores (I. Oteo et al. 2018; A. S. Long et al. 2020; J. B. Champagne et al. 2021; S. Arribas et al. 2024)

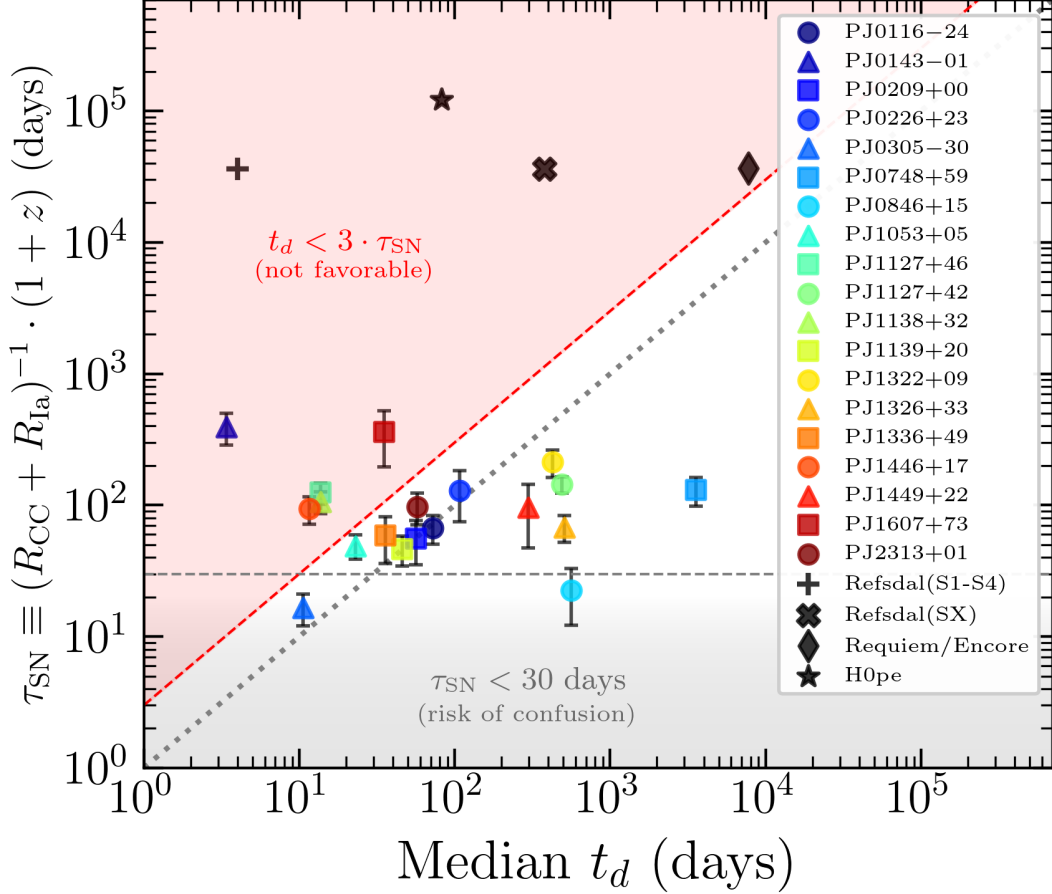


Figure 7. Characteristic timescale between supernovae in the observer-frame, $\tau_{\text{SN}} \equiv (R_{\text{CC}} + R_{\text{Ia}})^{-1} \cdot (1+z)$, vs. the median time delays t_d for PASSAGES and for gISN host galaxies in the literature. A dotted line indicates $\tilde{t}_d = \tau_{\text{SN}}$, while the red shaded region marks $\tilde{t}_d < 3 \cdot \tau_{\text{SN}}$. We consider this regime not particularly favorable for a sparse monitoring cadence, as these target fields are likely to have long stretches with no images of gISNe arriving. On the other hand, targets with a very short τ_{SN} (e.g. < 30 days) carry a risk of confusion in ensuring that SN candidates identified in different arcs are in fact multiple images of the same SN.

suggest that they may be confined within regions of $\sim 100\text{--}500$ kpc in diameter ($\sim 0.2\text{--}1.0'$ at $z = 3$). They thus can overlap more substantially with the multiply-imaged source-plane regions behind lensing clusters. For example, [B. L. Frye et al. \(2024\)](#) estimated an integrated SFR of $100\text{--}500 M_{\odot} \text{ yr}^{-1}$ in two overdensities ($z \approx 1.8$ and $z \approx 2.2$) behind the G165 cluster, accounting for $\sim 1\text{--}3$ CCSNe yr^{-1} . Perhaps as a proof of concept, the triply-imaged SN H0pe was discovered in a massive host galaxy within the $z \sim 1.8$ overdensity behind G165 ([B. L. Frye et al. 2023](#); [M. Polletta et al. 2023](#); [B. L. Frye et al. 2024](#)), through JWST/NIRCam imaging that was primarily targeting the PASSAGES DSFG that is nearby in projection.

4. SUMMARY

So far, discoveries of gravitationally lensed supernovae that can be observed in multiple images have been very

limited—unsurprisingly, as both lensing and supernovae are rare phenomena. They are, however, exceptionally useful for the purpose of time-delay cosmography, which depends upon the delays in arrival time between pairs of multiple images (induced by the difference both in path lengths of their respective geodesics and in the gravitational potential that they experience). Considering the yet-unresolved Hubble tension in different measurements of the Universe’s expansion rate, novel and independent methods to constrain H_0 are likely to be highly informative. Yet, fewer than 10 multiply-imaged supernovae have ever been discovered, and only 2 of which have so far been employed successfully for TD cosmography (SN Refsdal and SN H0pe; [P. L. Kelly et al. 2023a](#); [M. Pascale et al. 2025](#)). There are several advantages to using supernovae for this measurement over, for example, lensed quasars (e.g., reviews by [T. Treu et al. 2022](#); [S. Birrer et al. 2024](#)); chief among them is that the

light curve of a supernova is transient, not just variable like quasars, and is capable of being modeled. For now, though, lensed quasars have a key advantage through being simply more numerous. A joint inference of H_0 , combining information from several lensed supernovae, can be quite competitive with the level of precision achieved for other methods that have so far received much more attention. To get to this point in the next decade, however, requires many more discoveries, and it will likely not be sufficient to rely on luck alone.

To this end, we consider the feasibility of a targeted approach focused on galaxies that are expected to be uniquely fruitful for gravitationally lensed supernovae. In this work, we have attempted to forecast the rates of gLSNe that might be reasonably observed for a set of 21 dusty star-forming galaxies from the PASSAGES sample, spanning $z \approx 1.1 - 3.5$. Using their magnification-corrected intrinsic star formation rates, derived in previous works, we tabulate their rates of core-collapse and Type Ia supernovae, R_{CC} and R_{Ia} . Given the expectation that only a fraction of this star formation is occurring in regions with low enough dust obscuration to ever be detectable, even with the likes of JWST, we apply an assumed unobscured fraction ($\sim 20\%$) to our supernova rates. The exact sensitivity and control time will depend on observing setup, but I. Mäntynen et al. (2025) found a detectable fraction of $\approx 34\%$ for local LIRGs in an experiment sensitive to $A_V < 16$. We also include the reduction in observable rates due to the fact that time in these galaxies is slowed by a factor of $1 + z$ from the perspective of Earth. On the other hand, the observable rates are boosted by some factor $\mathcal{N}_{\text{eff}}$ (capturing the expected value of multiple images that a SN will appear in), based on existing gravitational lens models and the probabilistic distribution of star formation captured by dust and/or radio continuum.

As a result, we estimate a range of intrinsic rates $R_{CC} \approx 1.8 - 65 \text{ yr}^{-1}$ (core-collapse; median 11 yr^{-1}) and $R_{Ia} \approx 0.2 - 6.4 \text{ yr}^{-1}$ (Type Ia; median 1.1 yr^{-1}), with observable rates $\mathcal{R}_{CC} \approx 0.4 - 8.0 \text{ yr}^{-1}$ (median 2.3 yr^{-1}) and $\mathcal{R}_{Ia} \approx 0.2 - 3.9 \text{ yr}^{-1}$ (median 1.1 yr^{-1}). As for the time-delayed rates of individual SNe, $R \cdot (1 + z)^{-1}$, we find ranges of $0.8 - 20 \text{ yr}^{-1}$ (median 3.5 yr^{-1}) and $0.1 - 2.0 \text{ yr}^{-1}$ (median 0.3 yr^{-1}) for CCSNe and SNe Ia, respectively. The number of supernovae that a monitoring campaign would yield is dependent on the control time of the observations, or the duration for which a given supernova would be above survey limits. In this regard, the biggest challenge for this particular sample would be ensuring adequate near-IR sensitivity to withstand dust attenuation, effectively necessi-

tating JWST/NIRCam. While we have discussed some evidence that the attenuation might be inhomogeneous enough to allow some relatively unobscured sightlines, this is a source of large uncertainty at the moment.

Despite this challenge, the population of lensed starbursts is a veritable wealth of supernovae, in the extremely rarefied stratum of galaxies with more than one supernova occurring per (rest-frame) year. Notwithstanding sheer luck, for almost any other targeted strategy to discover gLSNe, it would be necessary to monitor either a small sample for several years, or else a very large sample over a shorter timespan. Whereas only 2 gLSNe have yet delivered time-delay cosmographical measurements (SN Refsdal and SN H0pe, at time of writing), every new discovery has enormous potential to significantly improve the level of uncertainty on H_0 inferences and other cosmological parameters (e.g., C. Grillo et al. 2024). The ultimate goal of the next decade is to reach $\sim 1\%$ precision through joint inference (D. Coe & L. A. Moustakas 2009; T. Treu & P. J. Marshall 2016; T. Treu et al. 2022).

Fortunately, the PASSAGES objects typically have wider separations between lensed images; their Einstein radii satisfy $\theta_{\text{Ein}} \gtrsim 0.5''$ in the vast majority of cases, with some even exceeding $10''$. We find that a strong correlation between θ_{Ein} and their median lens model-predicted time delays, which may even have some analytical basis connecting the maximum time delay that can be expected for an axisymmetric isothermal lens and its Einstein radius (Appendix B). Finally, we compare the expected median time delays to the characteristic observed-frame timescale between supernova events (including both core-collapse and Type Ia). We find that PASSAGES occupies an ideal regime where the lensing time delays are not significantly shorter than the time between individual supernovae, such that multiple imaging from lensing helps improve the odds of catching one in a random monitoring program.

While this work forecasts the potential of the ~ 30 PASSAGES lensed DSFGs, in part because they account for a non-negligible fraction of the known HyLIRGs, there are several hundred other candidate lensed DSFGs known currently, and perhaps many thousand more yet to be discovered at slightly lower intrinsic luminosities (C. Sedgwick et al. 2025). We contend that an optimal approach would involve targeted searches in tandem with (ongoing and planned) wide-area and blind surveys with *Euclid*, Rubin LSST, the *China Space Station Telescope*, and the *Roman Space Telescope* (e.g., D. A. Goldstein & P. E. Nugent 2017; D. A. Goldstein et al. 2019; R. Wojtak et al. 2019; J. D. R. Pierel et al.

2021; D. Ryczanowski et al. 2023; A. Sainz de Murieta et al. 2023; N. Arendse et al. 2024; J. Dong et al. 2024; A. Sainz de Murieta et al. 2024; M. Bronikowski et al. 2025).

The level of precision in H_0 measurements from cluster-lensed supernovae has been of order 6 – 7% for SN Refsdal (C. Grillo et al. 2018; P. L. Kelly et al. 2023a) and 7 – 13% for SN H0pe (M. Pascale et al. 2025). While it will not be possible to replicate the fully-blinded process used in obtaining these results, there is a distinct possibility in refining these uncertainties. For example, the lens models for SN H0pe were constructed with only 5 spectroscopically-confirmed image system redshifts (out of 21), which can have a sizeable influence on model accuracy (e.g., T. L. Johnson & K. Sharon 2016). Similarly, the SN H0pe inference was subject to unique photometric uncertainties at the time of publication due to the lack of a “template” image (where the supernova was not visible) of the host galaxy in most filters (J. D. R. Pierel et al. 2024a). The images of SN Encore with the shortest time delays are similarly expected to yield a measurement of order $\approx 10\%$ precision, whereas the longest delays (> 3000 days) could reduce this to 2 – 3% (J. D. R. Pierel et al. 2024b; S. Suyu et al., in prep.; J. D. R. Pierel et al., in prep.).

Within PASSAGES, 5 cluster fields have estimated median time delays exceeding 100 days and $\theta_{\text{Ein}} > 5''$ (PJ0748+59, PJ0846+15, PJ1127+42, PJ1322+09, and PJ1449+22) and should in principle offer the greatest likelihood of a similar level of precision if gLSNe were discovered in each. A joint population inference for ~ 20 lensed supernovae has the potential to reach $\sim 1\%$ level precision on H_0 (S. H. Suyu et al. 2020), but even a sample of only 6 lensed quasars has been able to reach $\sim 2\%$ relative uncertainty (K. C. Wong et al. 2020). The discovery of 5 lensed supernovae suitable for cosmography from a sample like PASSAGES would result in a competitive H_0 measurement, shedding much-needed light on the Hubble tension.

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Facilities: ALMA, VLA

Software: APLPY (T. Robitaille & E. Bressert 2012; T. Robitaille 2019), ASTROPY (Astropy Collaboration et al. 2013, 2018, 2022), BLOBCAT (C. A. Hales et al. 2012), CASA (J. P. McMullin et al. 2007), LENSTOOL (J. P. Kneib et al. 1993; J.-P. Kneib et al. 1996; E. Jullo et al. 2007; E. Jullo & J.-P. Kneib 2009), matplotlib (J. D. Hunter 2007), pandas (W. McKinney 2010; The pandas Development Team 2024), Ned Wright’s Cosmology Calculator (E. L. Wright 2006)

APPENDIX

A. ESTIMATING TYPE IA SUPERNOVA RATES ROBUSTLY WITHOUT STELLAR MASS MEASUREMENTS

For a subset of the PASSAGES sample, P. S. Kamieneski et al. (2024a) made predictions for the sSFRs relative to the star-forming main sequence of galaxies between SFR and M_* (e.g., J. Brinchmann et al. 2004; E. Daddi et al. 2007; K. E. Whitaker et al. 2012; J. S. Speagle et al. 2014). P. S. Kamieneski et al. (2024a) used the objects’ gas depletion times ($\sim 150 - 350$ Myr; K. C. Harrington et al. 2016, 2021; D. A. Berman et al. 2022) to estimate that they occupied the regime of $\Delta\text{MS} \equiv \log_{10}(\text{SFR}/\text{SFR}_{\text{MS}}) \approx 0.0 - 0.9$, following the prescription of T.-M. Wang et al. 2022 (see also R. Genzel et al. 2015; L. J. Tacconi et al. 2018; D. Liu et al. 2019). In an independent approach, P. S. Kamieneski et al. (2024a) used star formation rate surface densities Σ_{SFR} to estimate ΔMS , as per E. F. Jiménez-Andrade et al. (2019), resulting in a range of $\Delta\text{MS} \approx -0.1 - 0.5$.

With this information in mind, a sensible upper limit for their sSFRs would be $\Delta\text{MS} < 0.9$ dex, which happens to be ≈ 3 times the 1σ scatter of the main sequence, and also 0.3 dex above the typical threshold for starburst galaxies (G. Rodighiero et al. 2011). To further motivate this, we consider some recent measurements of stellar masses in large samples of DSFGs. O. Miettinen et al. (2017) found that 57% of a sample of 124 mm-selected DSFGs in COSMOS were within a factor of 3 (≈ 0.5 dex) of the main sequence, and 89% were below $\Delta\text{MS} < 0.9$ dex. Similarly, for 185 submm-selected DSFGs in the North Ecliptic Pole (NEP) field, L. Barrufet et al. (2020) found 57% within 0.5 dex of the main sequence. More recently, in a large sample of ≈ 450 $z > 1$ sources in the NEP selected at $850 \mu\text{m}$, H. Shim et al. (2022) found 67% with $\Delta\text{MS} < 0.5$ dex and 90% with $\Delta\text{MS} < 0.9$ dex. This finding that DSFGs are largely not dramatically above the main sequence—with apparently the majority even consistent with the SFMS—is not particularly surprising. As discussed by C. M. Casey et al. (2014a), the duty cycle of DSFGs in the starburst regime ($\Delta\text{MS} > 0.6$ dex) might be quite short, so that they spend most of their time on the main sequence.

We can use this upper limit in sSFR of 0.9 dex above the main sequence (computed according to J. S. Speagle et al. 2014), along with the total SFRs inferred from the IR, in order to derive lower limits in M_* . We also use a lower limit of sSFR 0.3 dex below the SFMS, giving the upper limits in M_* . By extension, these provides lower and upper limits, respectively, in the Ia supernova rate, R_{Ia} . Fortunately, as illustrated in Equation 8, the dependence on M_* is quite weak relative to SFR for galaxies on or above the main sequence, so these approximate limits contribute extremely minimally to the error budget in comparison with the uncertainties on SFR.

B. THE CONNECTION BETWEEN TYPICAL TIME DELAYS AND IMAGE SEPARATIONS

As noted by H. J. Witt et al. (2000) and M. Oguri (2007), a lens with an isothermal potential $\phi(r, \theta) = r \cdot F(\theta)$ for generalized angular structure $F(\theta)$ will result in time delays between arcs i and j

$$\Delta t_{ij} = \frac{1 + z_l}{2c} \frac{D_L D_S}{D_{LS}} (r_j^2 - r_i^2) \quad (\text{B1})$$

where r_i is the angular distance from arc i to the center of the lens. This produces the result that r_j and r_i can be arbitrarily large—and therefore θ_{Ein} as well—and still produce a small time delay, as long as $r_j \approx r_i$. Also, at the redshift of the lens, the physical separation between deflected light rays is $R_{\text{Ein}} = D_L \cdot \theta_{\text{Ein}}$. Considering the maximum possible time delays in this formulation (holding fixed the lens and source redshift),

$$\max(\Delta t_{ij}) \propto \max(r_j^2 - r_i^2) \propto (R_{\text{Ein}})^2. \quad (\text{B2})$$

In the left panel of Fig. 8, we modify Fig. 6 to show R_{Ein} (in kpc) on the horizontal axis and the median time delay, dilated to the redshift of the lens with a $(1 + z_l)^{-1}$ factor. The best-fit power-law slope for the *median* time delays is $\tilde{t}_d \propto (R_{\text{Ein}})^{1.53 \pm 0.16}$, slightly shallower than the prediction for the *maximum* time delays.

In at least the specific case of a singular isothermal spheroid (SIS) lens, the two images satisfy

$$r_j^2 - r_i^2 = (\theta_{\text{Ein}} + \beta)^2 - (\theta_{\text{Ein}} - \beta)^2 = 4\theta_{\text{Ein}}\beta \quad (\text{B3})$$

for source-plane offset β relative to the lens centroid (R. Narayan & M. Bartelmann 1996). By necessity, $\beta < \theta_{\text{Ein}}$, or else only a single image appears. Therefore,

$$\max(r_j^2 - r_i^2) = 4\theta_{\text{Ein}}^2 \quad (\text{B4})$$

and

$$\max(\Delta t_{ij}) = \frac{1+z_l}{2c} \frac{D_L D_S}{D_{LS}} \cdot 4\theta_{\text{Ein}}^2 \quad (\text{B5})$$

for an SIS lens, with θ_{Ein} in radians. The right panel of Fig. 8 plots this term on the horizontal axis, with the lens model-predicted maximum time delays (Table 2) on the vertical axis. A quasi-forbidden region is shaded in gray, representing model-predicted time delays that exceed the maximum from the H. J. Witt et al. (2000) and M. Oguri (2007) equation in the case of an SIS. We observe that the maximum model-predicted time delays t_d remain below $\max(\Delta t_{ij})$.

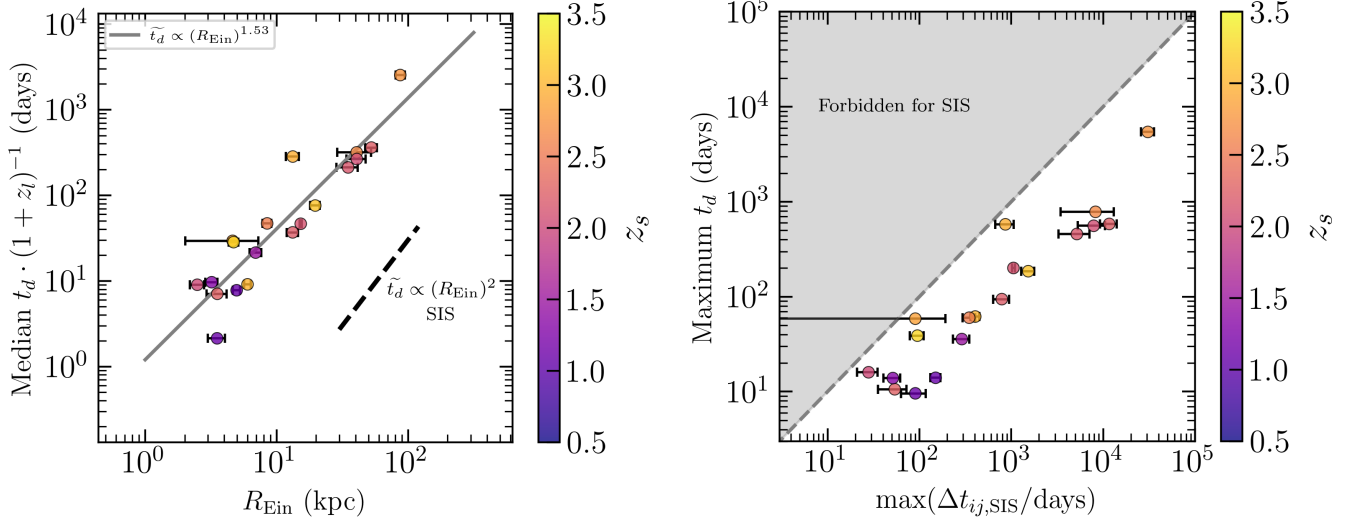


Figure 8. (Left) Fig. 6 is modified to now plot the median time delays t_d of PASSAGES at the redshift of the lens—i.e., including a dilation factor of $(1+z_l)^{-1}$ —vs. the physical Einstein radius $R_{\text{Ein}} = D_L \cdot \theta_{\text{Ein}}$. A gray line shows the best-fit power law, $\tilde{t}_d \propto (R_{\text{Ein}})^{1.53 \pm 0.16}$, while the dashed line segment shows the approximate scaling relation for an SIS with a power-law slope of 2. The colorscale shows source-plane redshift. (Right) Now, the *maximum* time delays vs. the predicted $\max(\Delta t_{ij})$ computed based on the redshift geometries and θ_{Ein} according to equation B5. The quasi-forbidden region (where lens model-predicted maximum time delays exceed the values allowed for an SIS lens at the respective lens/source redshifts with the respective Einstein radii), $\max(t_d) > \max(\Delta t_{ij,\text{SIS}})$ is shown shaded in gray.

Given the limiting assumptions implicit to this formulation (mainly that the lensing mass is consistent with a single SIS lens), this connection between time delays and Einstein radii will not hold in all cases. Still, it is reasonably useful for our purposes in identifying lenses that are more likely to have time delays of order months to years. By equation B5, for a fiducial SIS lens at $z_l = 0.5$ and source at $z_s = 2$, $\max(\Delta t_{ij}) < 30$ days for $\theta_{\text{Ein}} \lesssim 0.4''$, while $\max(\Delta t_{ij}) < 100$ days for $\theta_{\text{Ein}} \lesssim 0.8''$. Only $\sim 29\%$ of the PASSAGES subsample have $\theta_{\text{Ein}} < 0.8''$ (Table 2), while none considered have $\theta_{\text{Ein}} < 0.4''$, so their time delays are more likely to be longer, which generally yields improved H_0 precision.

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